

The Constituent Quark Model and beyond

**Diquarks, Tetraquarks, Pentaquarks
and no quarks**

Frank Close

How Quarks Behave

The meson landscape

Scalars and Glueballs

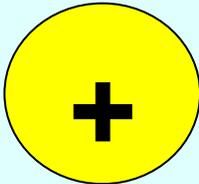
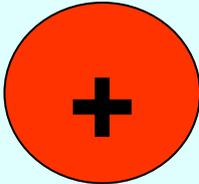
Beyond $q\bar{q}$

Weird charmonium and other things

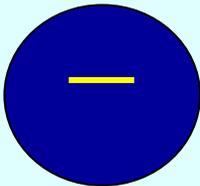
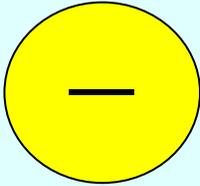
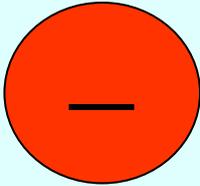
HOW QUARKS BEHAVE

CHROMOSTATICS

Quarks carry any of three “colour” charges



Antiquarks carry any of three “colour” charges but negative

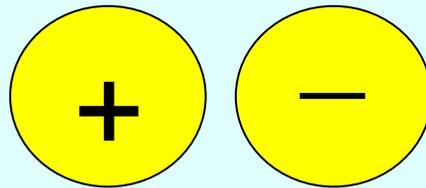
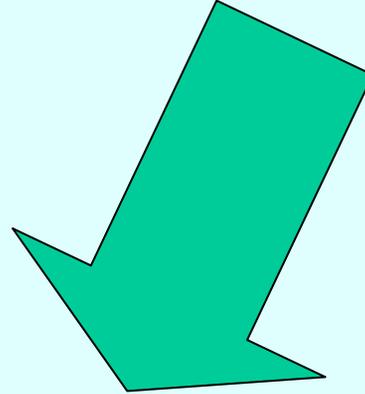


Now use familiar rules

“Like charges (colours) repel; opposite (colours) attract”

Now use familiar rules

“Like charges (colours) repel; opposite (colours) attract”



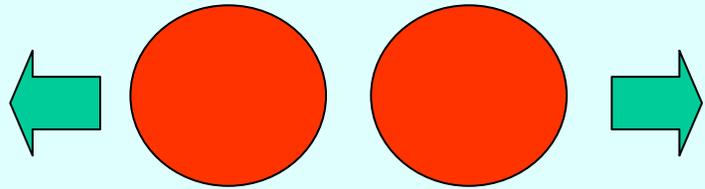
Makes a “meson”.

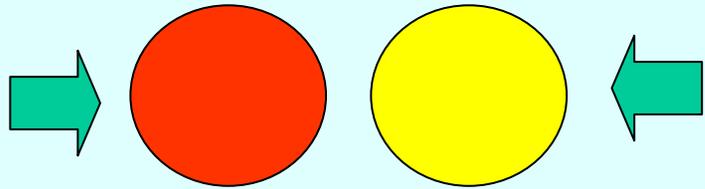
Simplest “chromostatic” analogue of electrostatic positronium

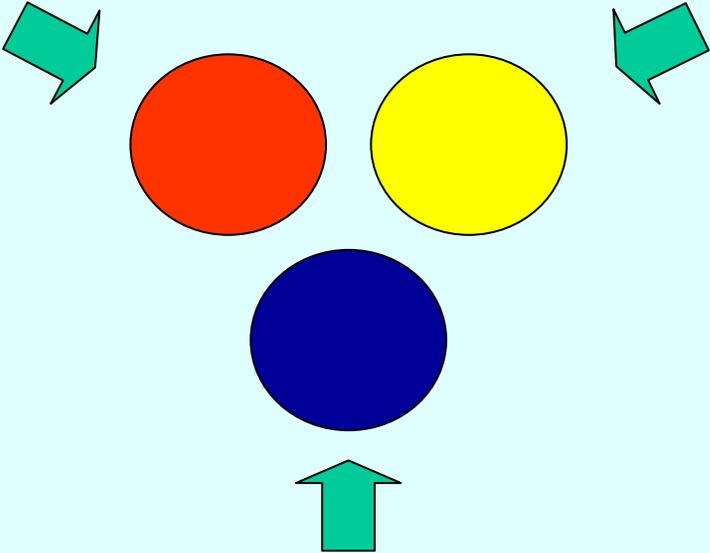
The **THREE** colours

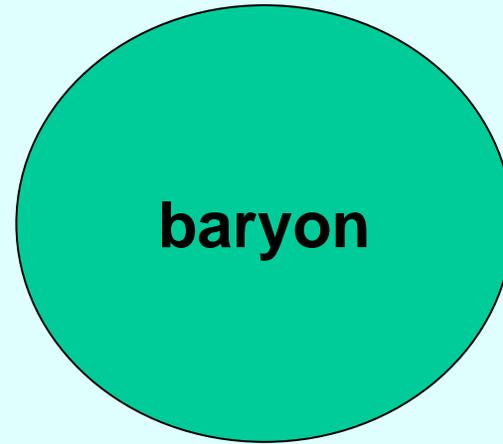
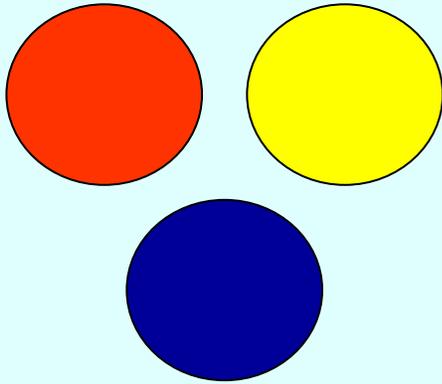
enable quarks to attract one another

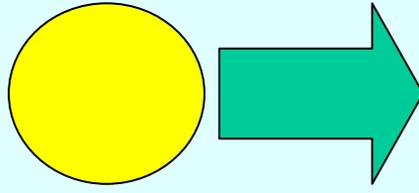
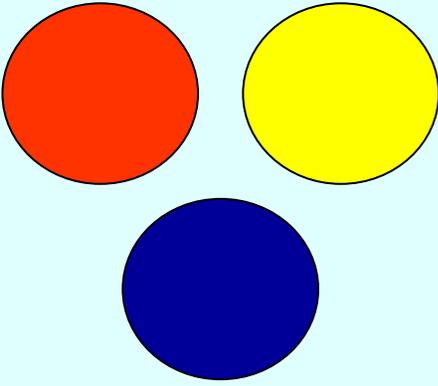
making **BARYONS** (e.g. the proton)

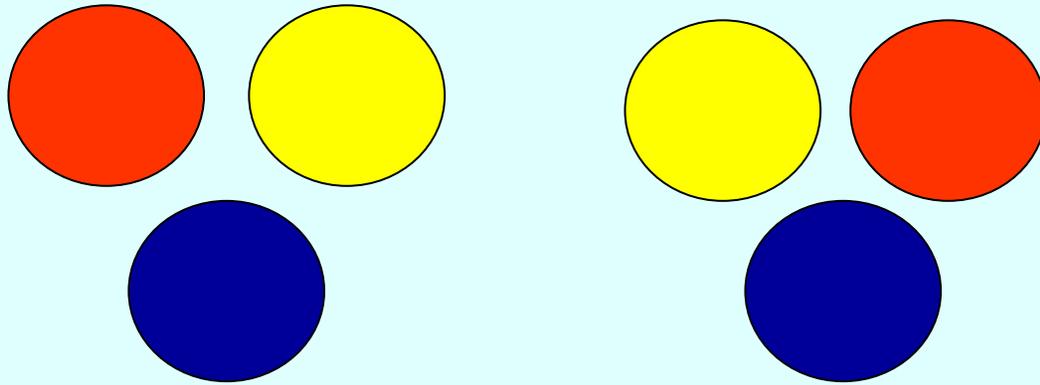




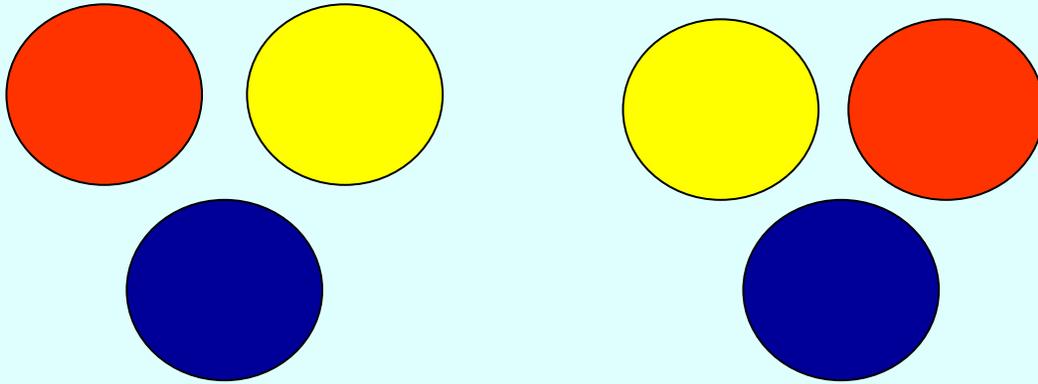








Simple nucleus (deuteron)

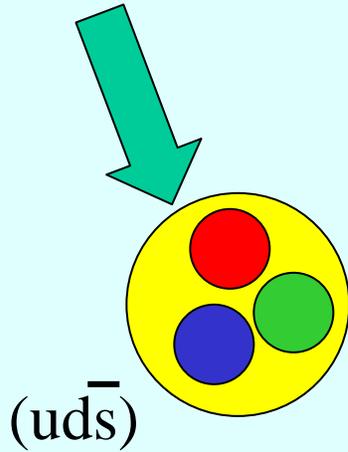


Colour charge → **Baryons** → **Nucleus**

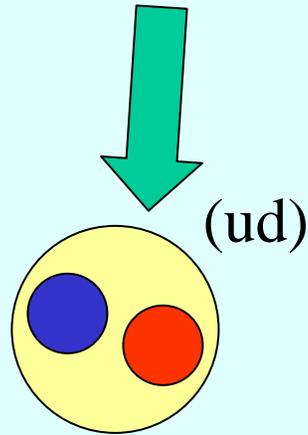
Electric charge → **Atoms** → **Molecules**

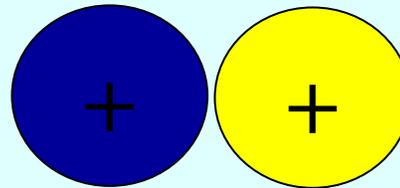
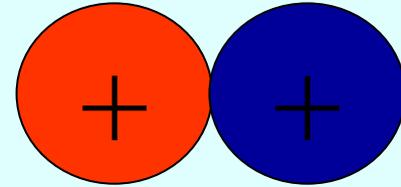
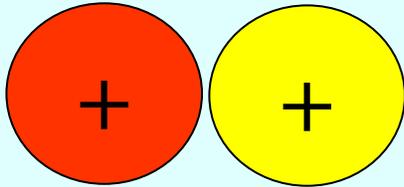
Two other ways that coloured q/q* can attract

J=1/2 triquark

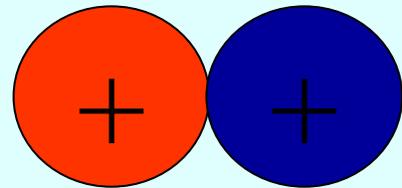
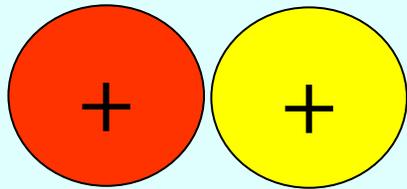


J=0 diquark

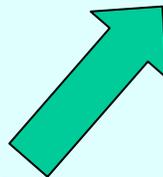
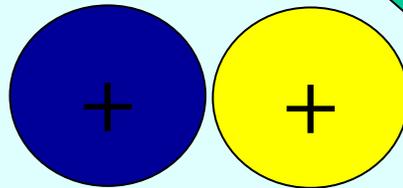
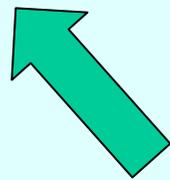


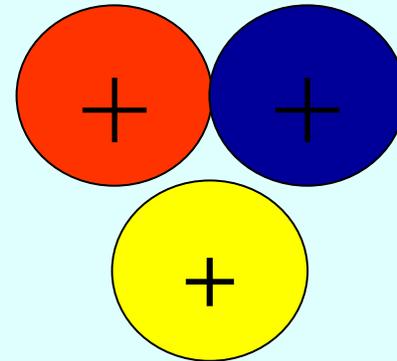
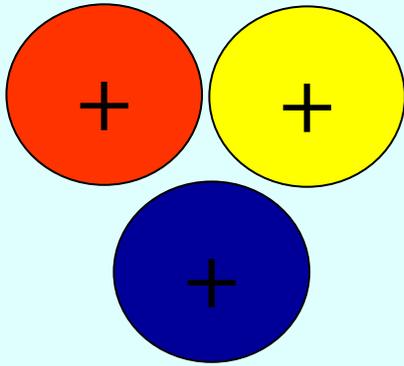


**Three different coloured diquarks
can mutually attract one another.....**



but

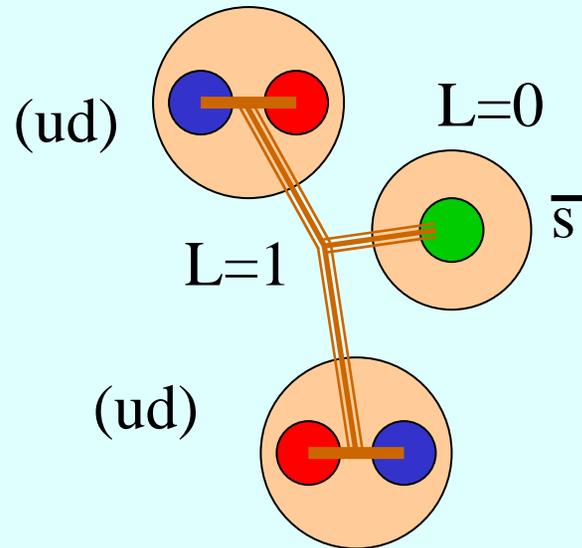




But rearrange to make...
e.g. a neutron and proton
Or even a deuteron

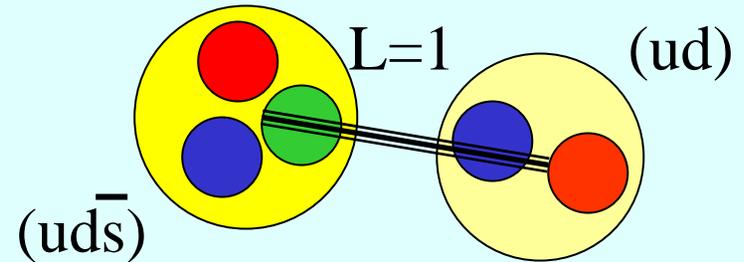
Can mutually attract forming a Pentaquark (...later)

(Jaffe, Wilczek)



$$J^P = 1/2^+$$

— Karliner, Lipkin)



$$J^P = 1/2^+$$

Quantum Electrodynamics: QED

Electric charge → Atoms → Molecules

Quantum Chromodynamics: QCD

Colour charge → Baryons → Nucleus

Quantum Electrodynamics: QED

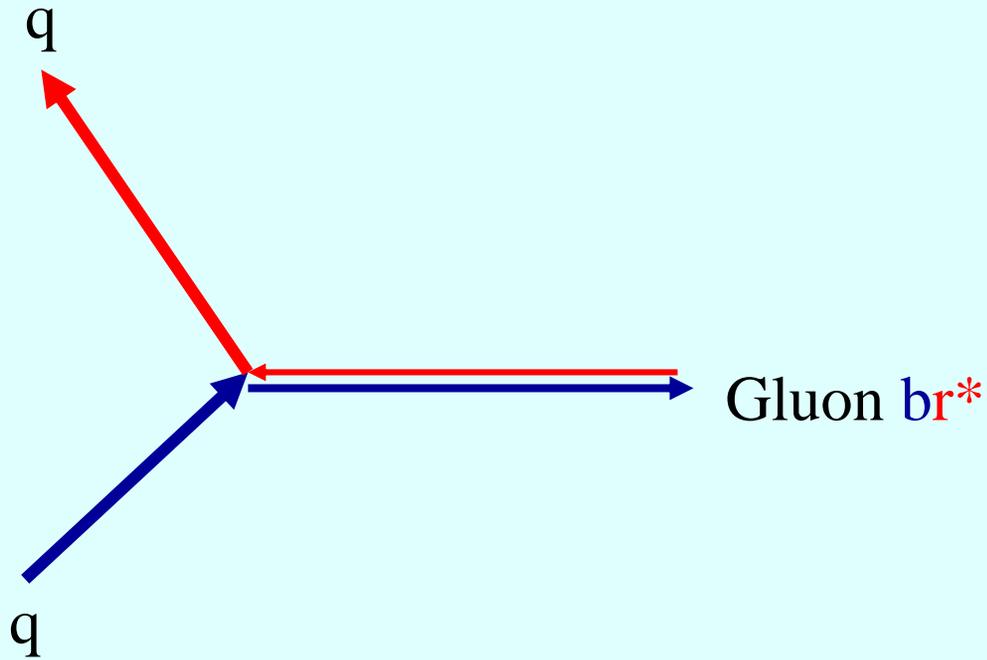
Electric charge → Atoms → Molecules

Interaction of electric charges and photons

Quantum Chromodynamics: QCD

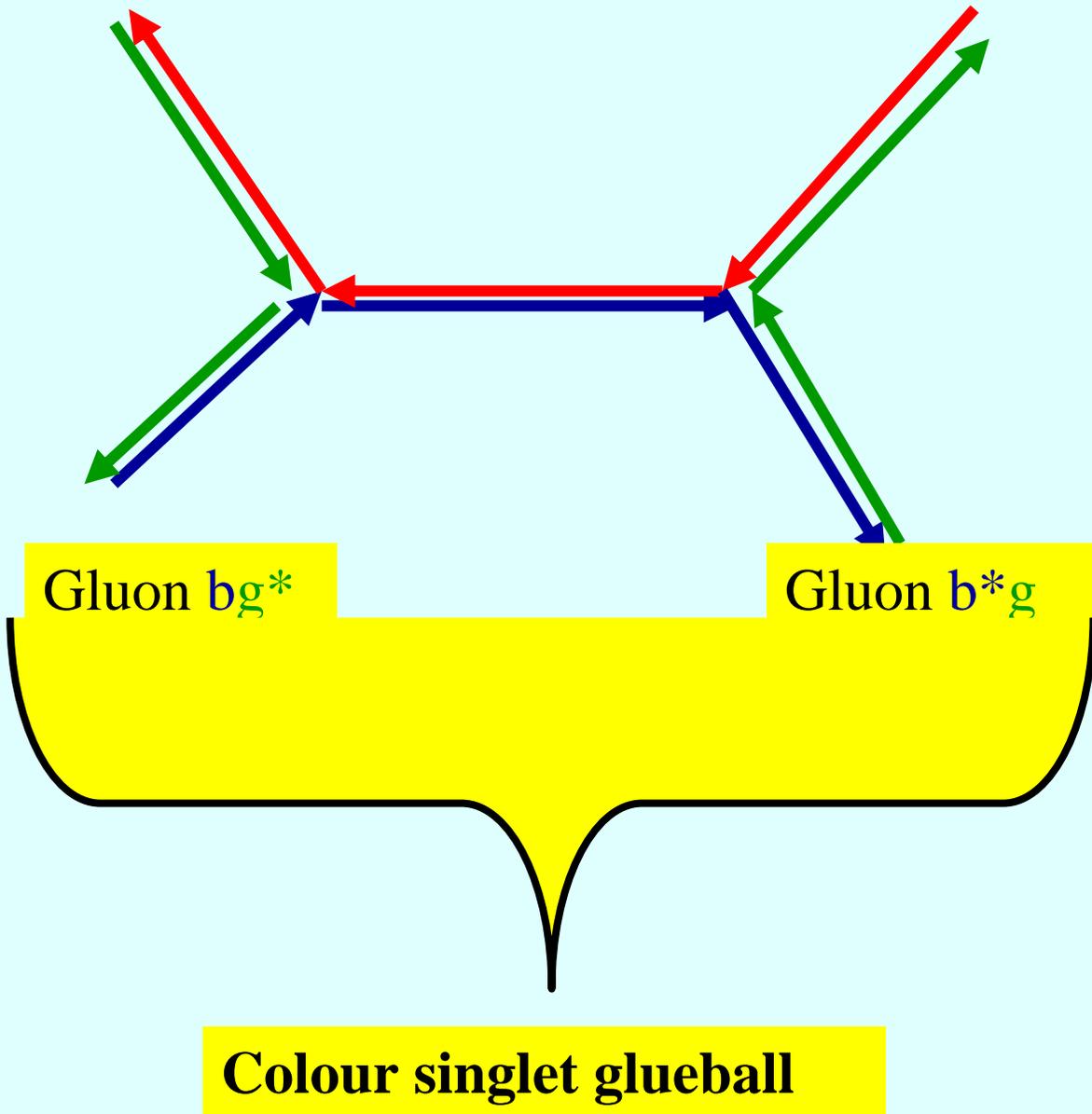
Colour charge → Baryons → Nucleus

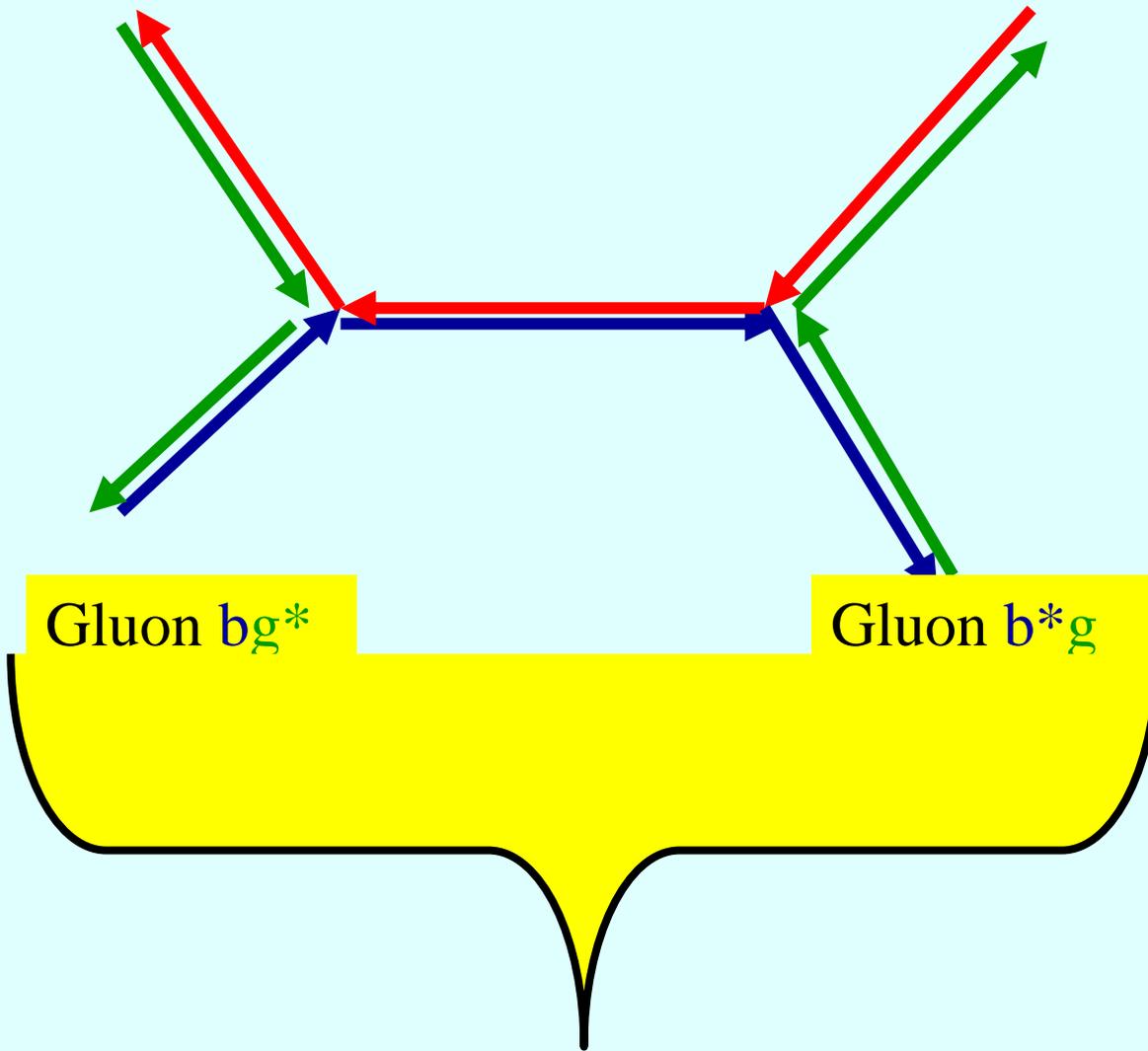
Interaction of colour charges and gluons



Gluon is coloured
Carries the “charge”

Like QED as far as pert theory concerned
Strong at long range/low energy
Need lattice QCD and models based on this





Lattice QCD

2_{++}	2.2 GeV
0_{-+}	2.2 GeV
0_{++}	1.5 GeV
All ± 0.2 GeV	

Colour singlet glueball

Folklore: where to look for glueballs

- **Get rid of the quarks**
- $\psi \rightarrow (\gamma gg) = (\gamma G) > (\gamma qq^*)$
- High energy production in central $PP \rightarrow PGP$
- Low energy $P-Pbar$ annihilation (LEAR)

Look at these phenomena later.

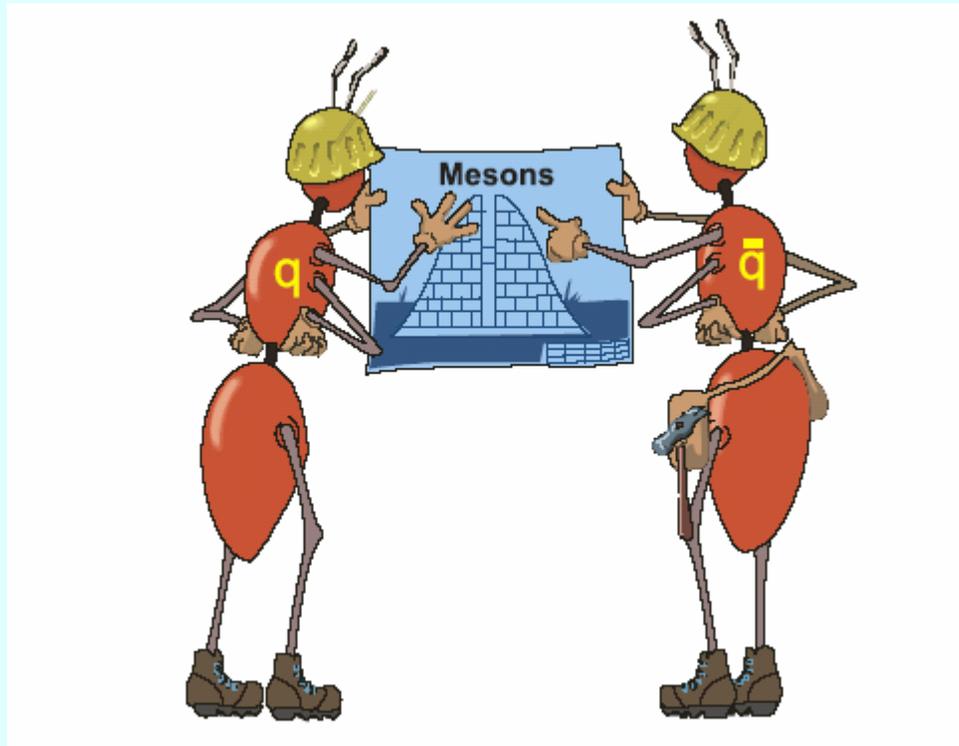
Chromostatics explains qq^* and baryons; but we expect also....

States outside the quark model

The reasons why



Mesons as quark antiquark: Heavy to Light Flavours



What do we know; what goes weird; what suggests glue?

Quarkonium template: qq^* $L + S (= 0,1) = J$

$1D: 1- 2- 3-$

 $2-$

$2S: 1- 0-$

$1P: 0+ 1+ 2+$

 $1+$

$1S: 1- 0-$

 $L=0$

$L=1$

$L=2$

Allowed $q\bar{q}$ quantum numbers:

$$\text{Spatial parity } P_{q\bar{q}} = (-1)^{(L+1)} \quad \text{C-parity } C_{q\bar{q}} = (-1)^{(L+S)}$$

The complete list of allowed $q\bar{q}$ J^{PC} quantum numbers has gaps!

The J^{PC} forbidden to $q\bar{q}$ are called “ J^{PC} -exotic quantum numbers”.

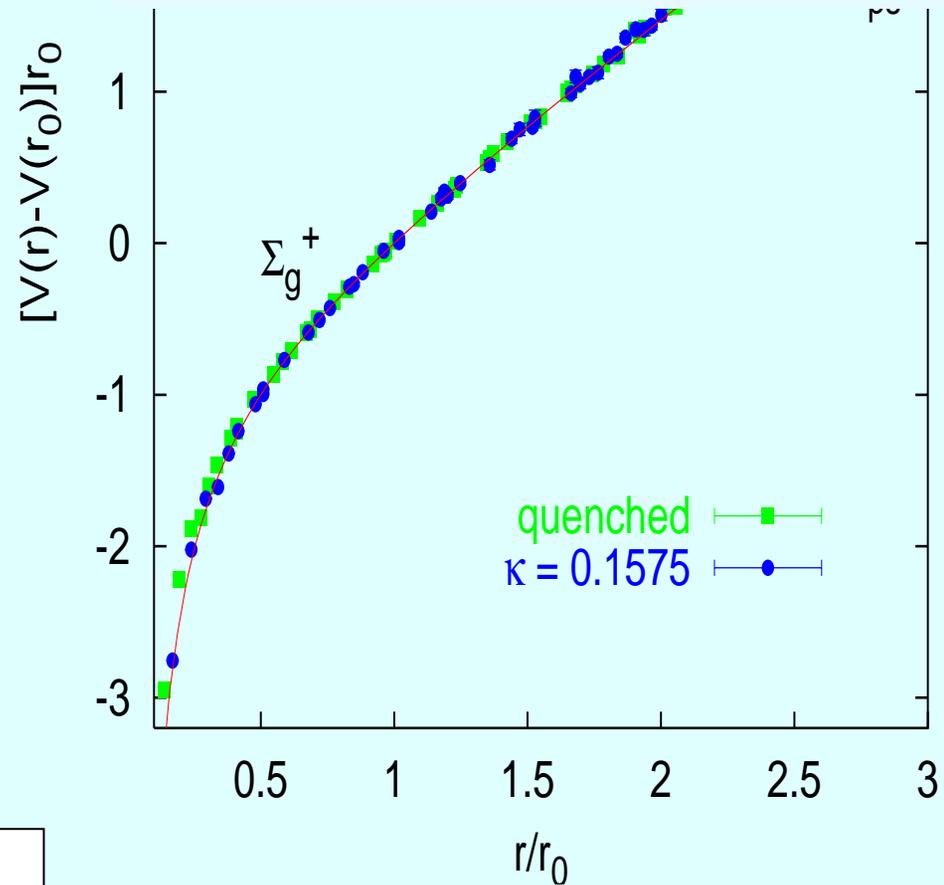
$$\text{Exotic } J^{PC} = 0^{--}; 0^{+-}, 1^{-+}, 2^{+-}, 3^{-+} \dots$$

PDG is (almost) full of conventional “non exotic” J^{PC}

Lattice Linear Potential

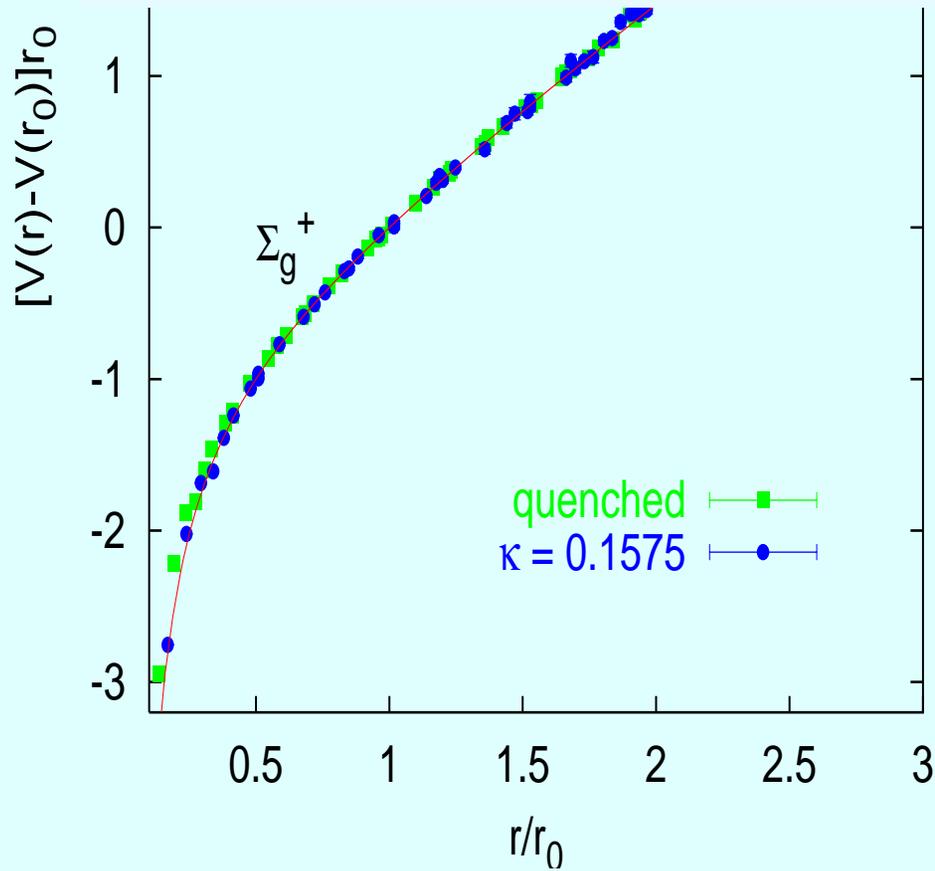
qq* spectrum
Empirically =
Linear potential
 $V(r) = kr$

Lattice QCD
predicts this too

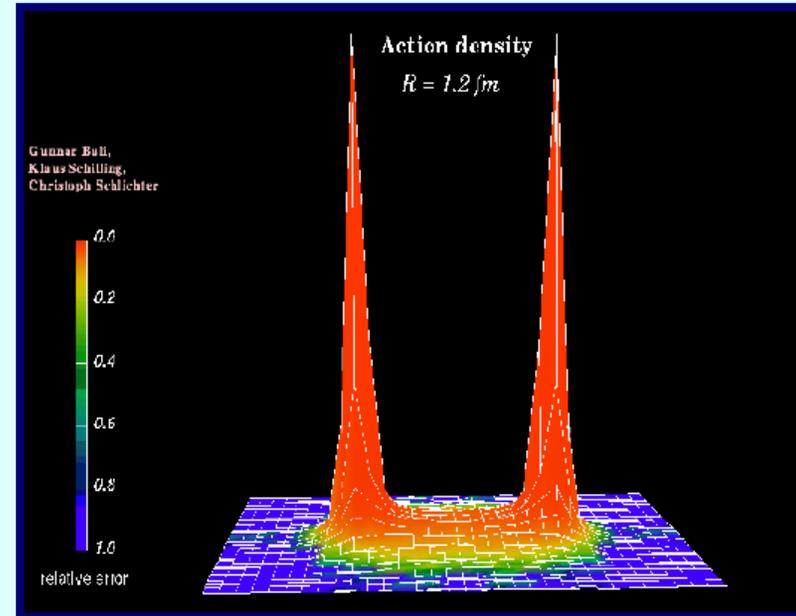


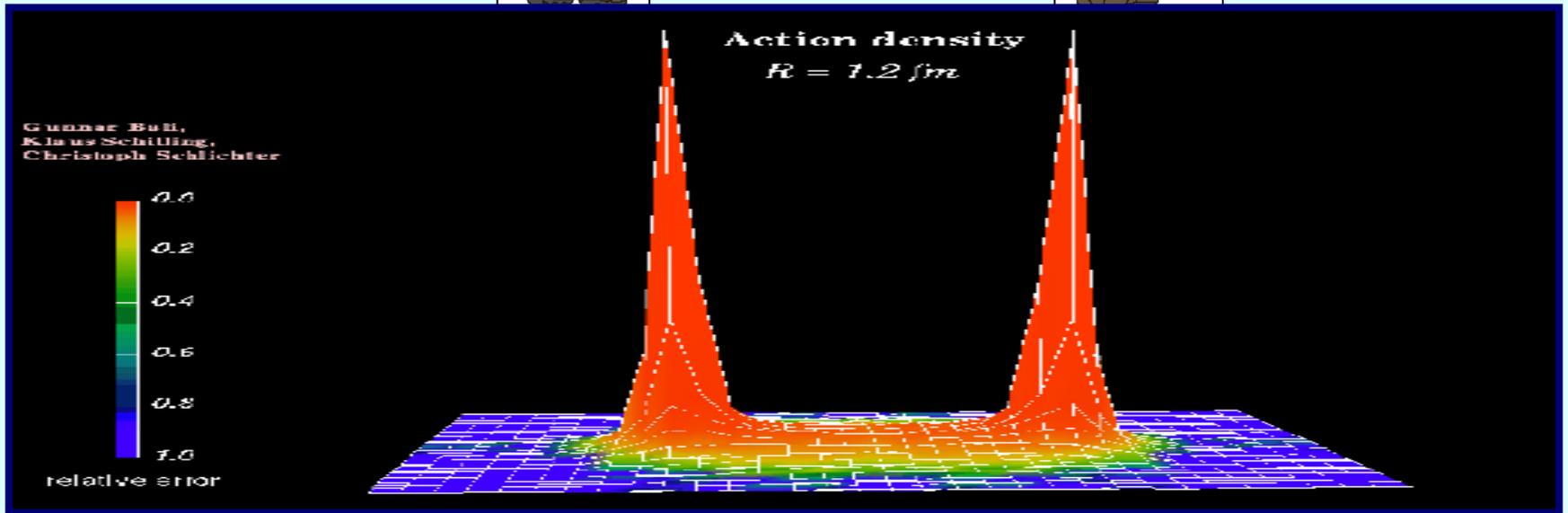
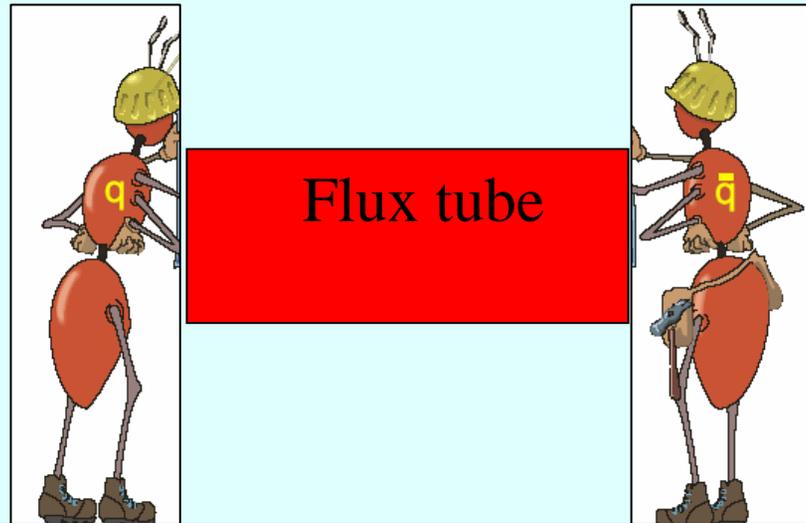
What does this imply for
force fields? Contrast $1/r$
Coulomb and 3D space.....

Lattice Linear Potential



Linear flux tube





Excite the gluonic flux tube = hybrid mesons (includes exotic JPC)

Allowed qq quantum numbers:

$$\text{Spatial parity } P_{qq} = (-1)^{(L+1)} \quad \text{C-parity } C_{qq} = (-1)^{(L+S)}$$

The complete list of allowed qq J^{PC} quantum numbers has gaps!

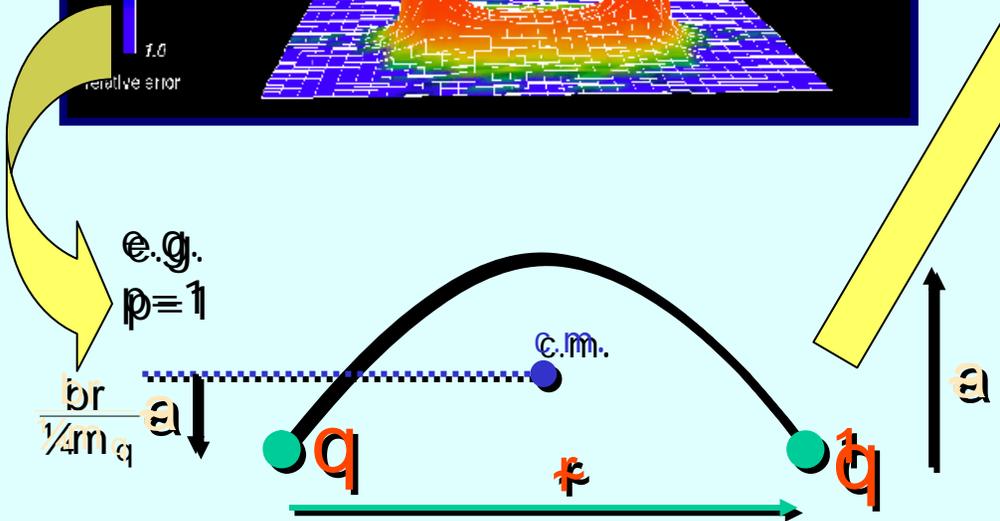
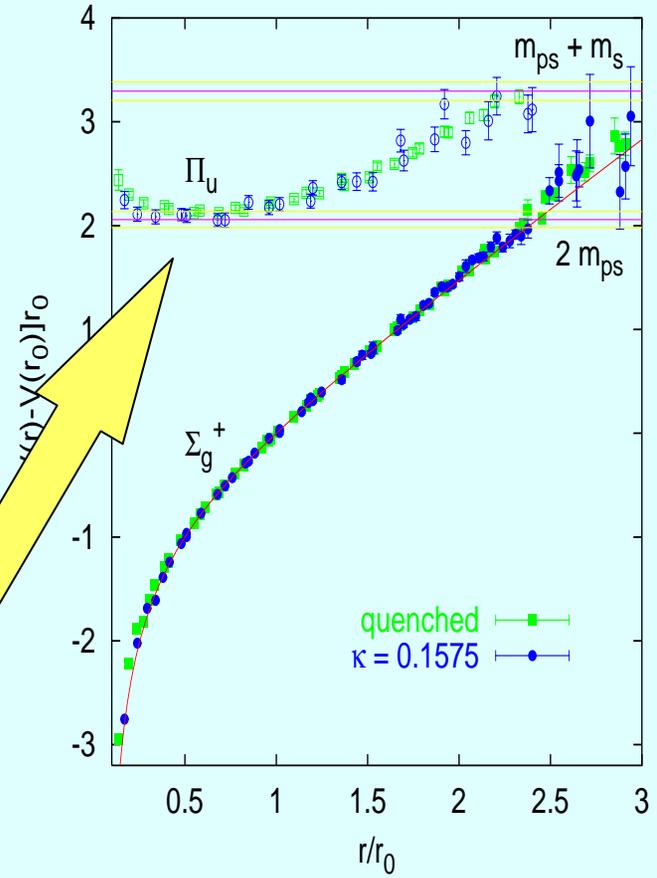
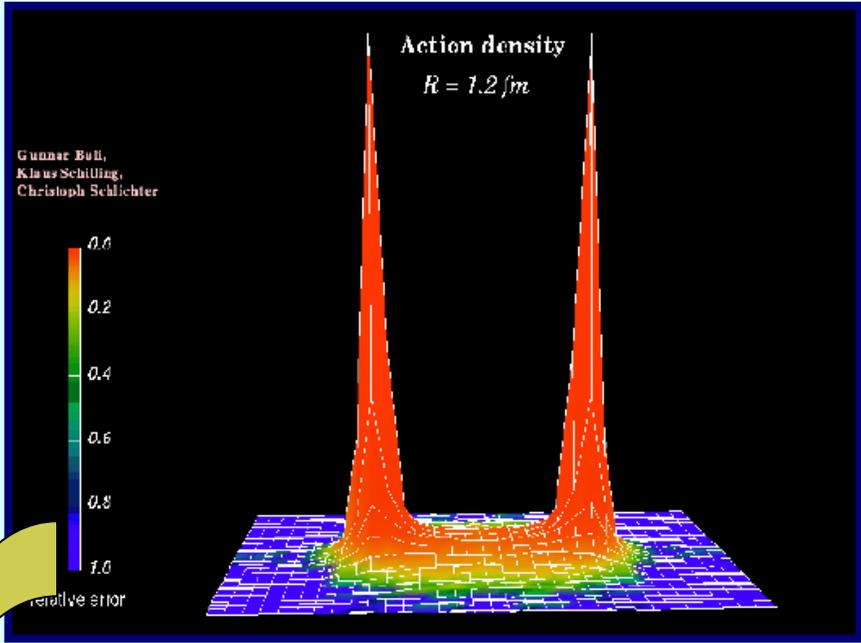
The J^{PC} forbidden to qq are called “ J^{PC} -exotic quantum numbers”.

$$\text{Exotic } J^{PC} = 0^{--}; 0^{+-}, 1^{-+}, 2^{+-}, 3^{-+} \dots$$

If you find a resonance with **exotic J^{PC}** ,
you are certainly beyond the naive qq quark model.

Plausible J^{PC} -exotic candidates =
hybrids, glueballs (high mass), maybe **multiquarks** (fall-apart decays).

Gluonic hybrid mesons



Exciting the flux tube

Lattice and model agree spectrum; and 2006 decays! (later)

1. Quarkonium for all flavors
.....and hints of glue

Quarkonium template: qq^* $L + S (= 0,1) = J$

$1D: 1- 2- 3-$

 $2-$

$2S: 1- 0-$

$1P: 0+ 1+ 2+$

 $1+$

$1S: 1- 0-$

 $L=0$

$L=1$

$L=2$

Quarkonium template: **Scalar qq*** is canonical

1D: 1- _____

2S: 1- _____

2+ _____

1+ _____

0+ _____

1S: 1- _____

$\Upsilon(b\bar{b})$

1D: 1- _____

2S: 1- **10023** _____

2+ **9913** _____

1+ **9893** _____

0+ **9860** _____

1S: 1- **9460** _____

1D: 1- 3770

2S: 1- 3686

2+ 3556

1+ 3510

0+ 3415

1S: 1- 3097

$\Upsilon(b\bar{b})$

$\psi(cc^*)$

1D: 1- 3772

2S: 1- 10023 3686

2+ 9913 3556

1+ 9893 3510

0+ 9860 3415

1S: 1- 9460 3097

Narrow below MM threshold

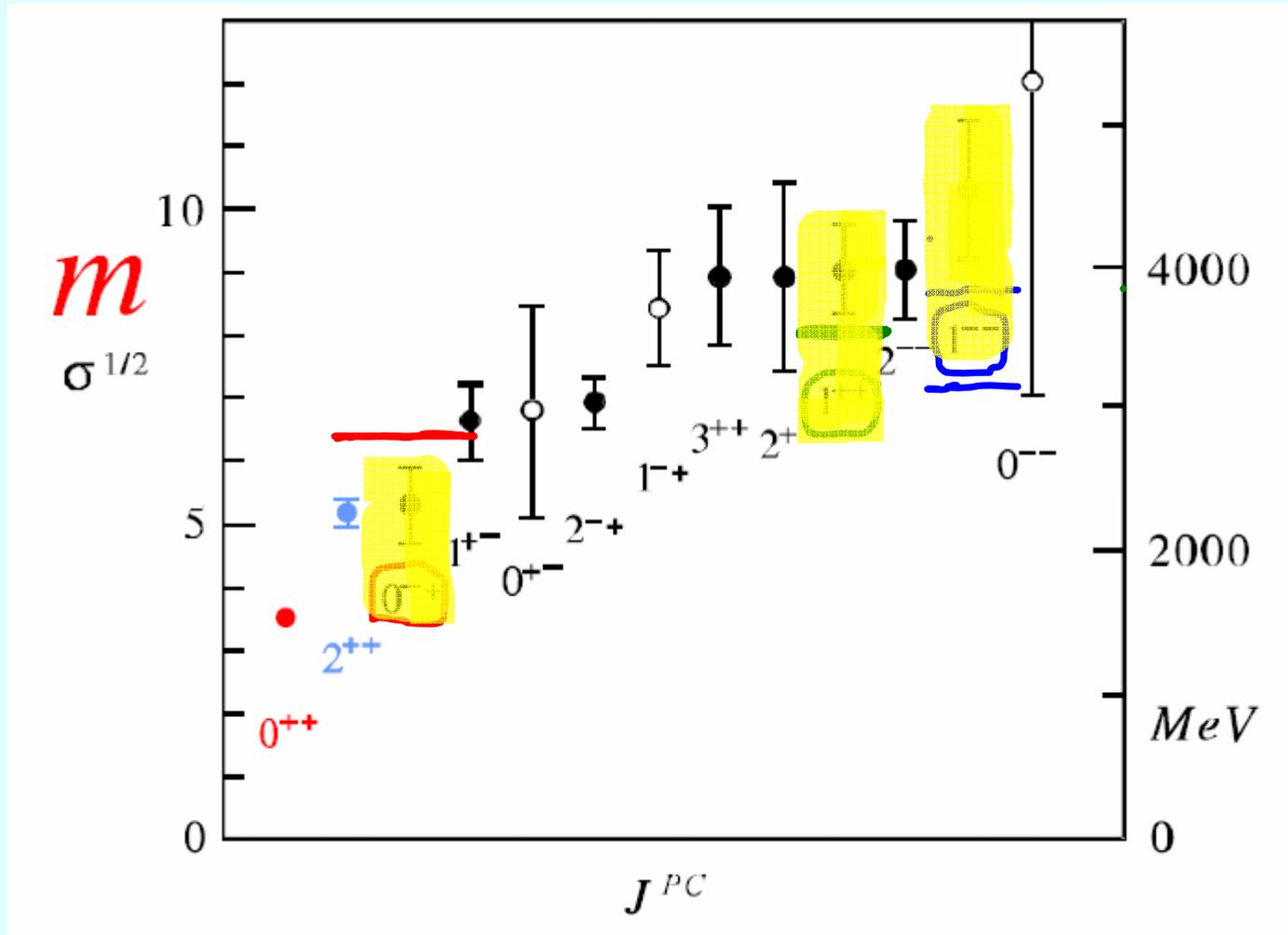
$\Upsilon (b\bar{b})$ $\psi (c\bar{c}^*)$ 1D: 1- 37722S: 1- 10023 3686

Either no G with these JPC in this region ($0^-+ 2.5 < \eta_c$) ($1^- - 3.8\text{Gev} \sim \psi\text{prime?}$) or don't couple strongly to G

2+ 9913 35561+ 9893 35100+ 9860 34151S: 1- 9460 3097

Narrow below MM threshold

Glueballs spectrum from Lattice



$D_s(c\bar{s})$ (Potential model prediction)

1D: 1- **2900**

2S: 1- **2730**

2+ **2590**

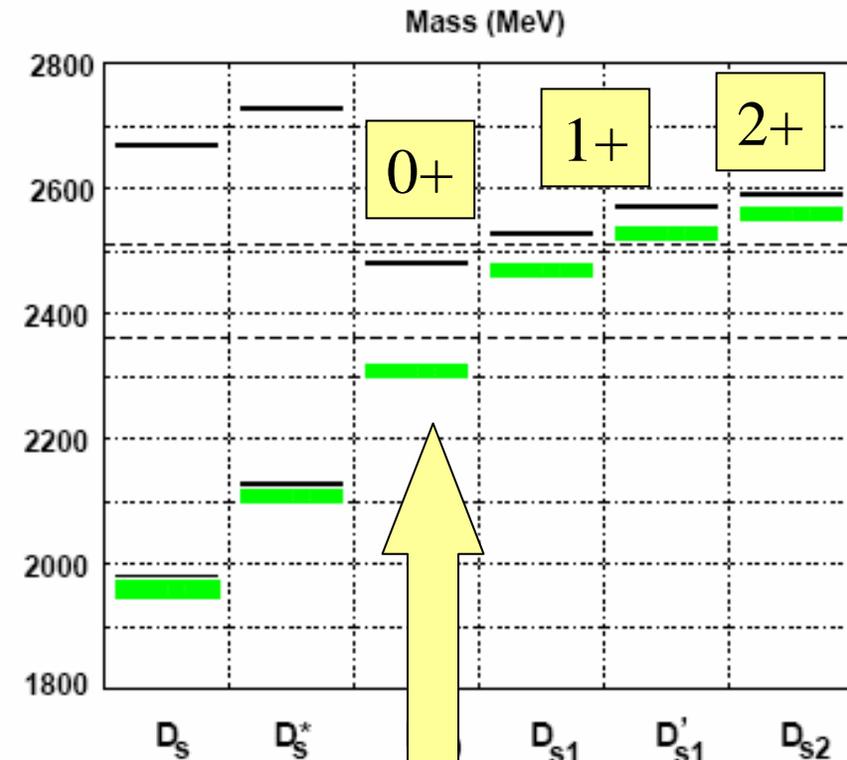
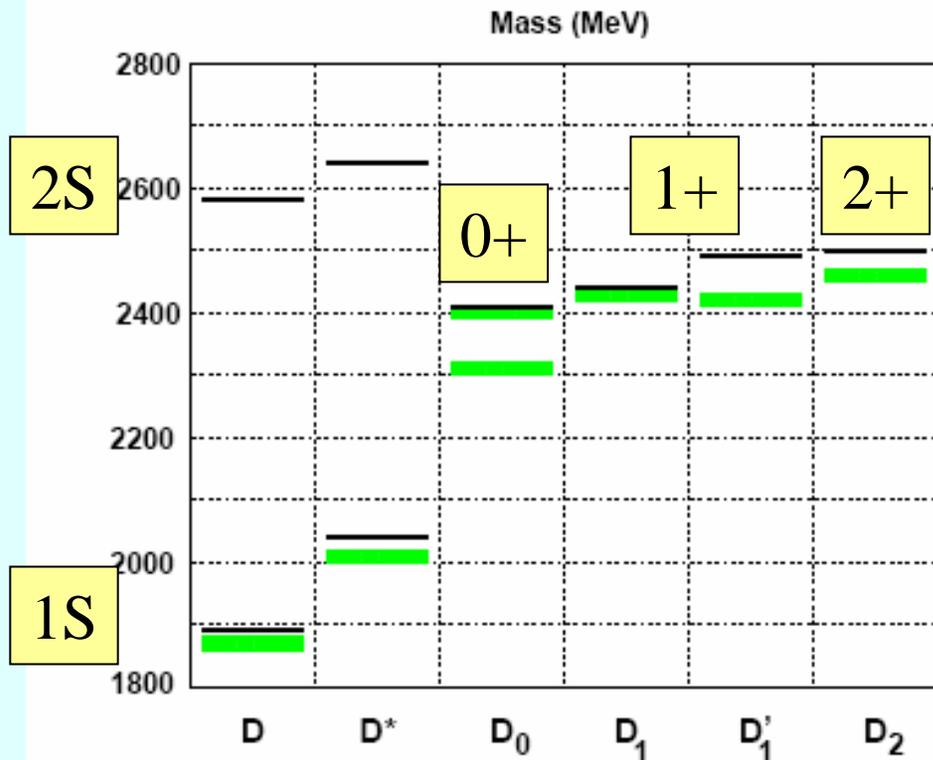
1+ **2550/2560**

0+ **2480**

1S: 1- **2130**

Charm.....and.....

Charm-Strange Mesons



0+ low
See later

$I=1$ vector :

$I=0$ nn^* ; ss^*

+ Problem of nn^* ss^* flavour mixing

1D: 1- 1700

2S: 1- 1460

2_+ 1320 1270/1525

1_+ 1300 1285/1530

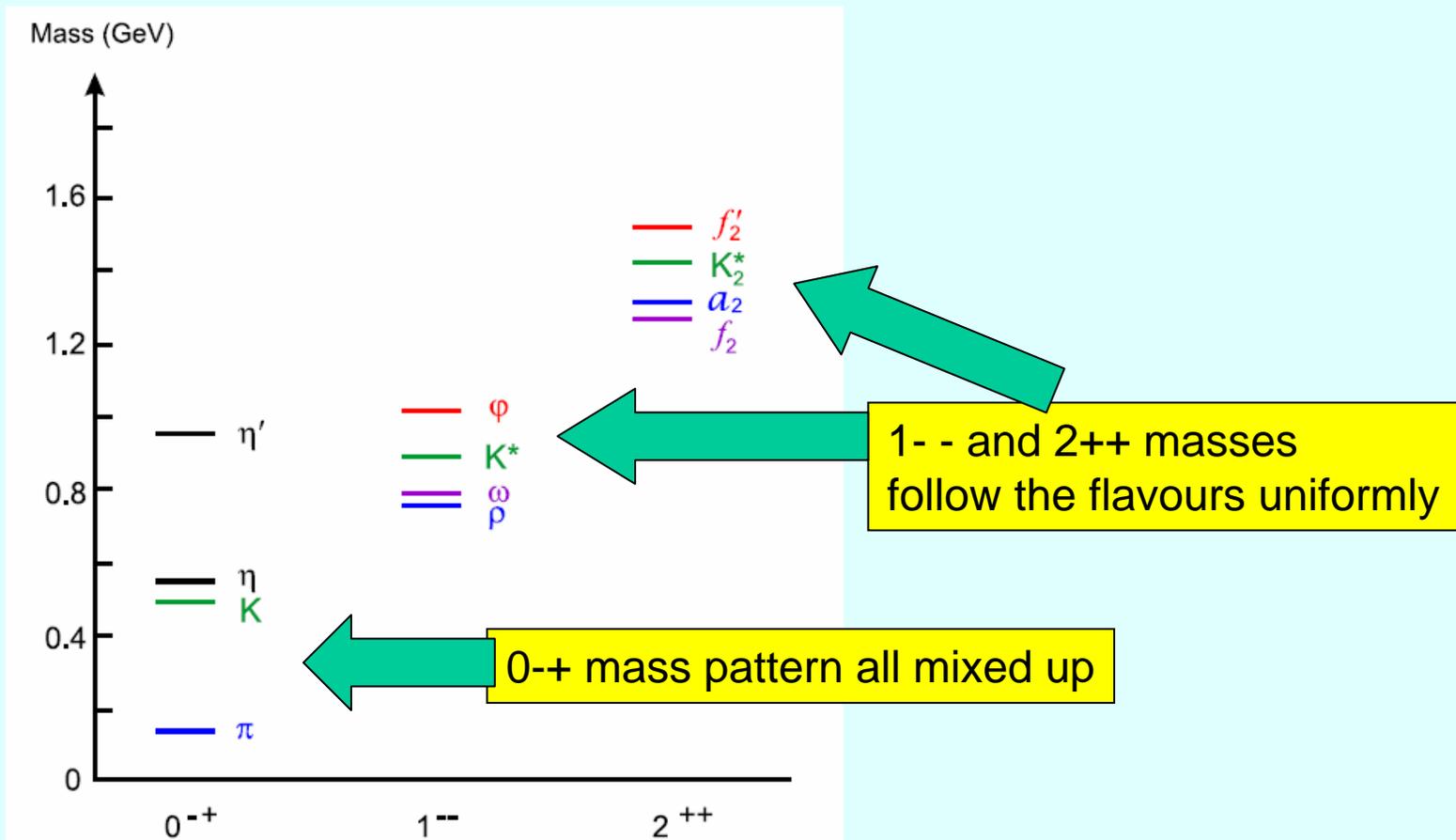
0_+ 1420

1S: 1- 770 780/1020

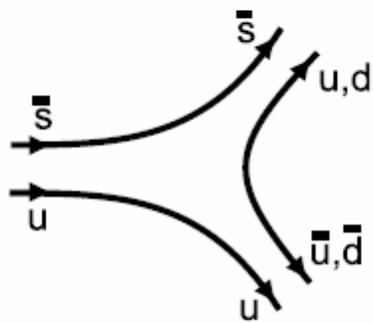
What do we know about flavours for
light qq^* nonets

Vector 1^{--} and tensor 2^{++} are flavour pure nonets

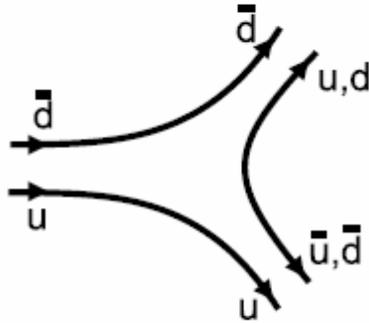
- Evidence:
1. masses of nn^* , K and ss^* states
 2. strong decays
 3. Electromagnetic transitions “weigh” the flavours



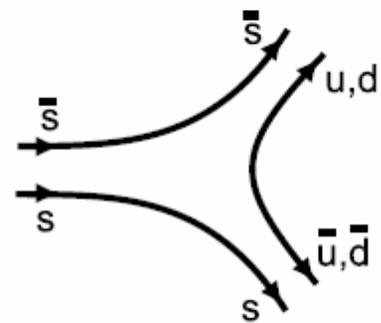
Strong decays “OZI rule” also fits



$$K^{*+} \rightarrow K^+ \pi^0, K^0 \pi^+$$



$$\rho^+ \rightarrow \pi^+ \pi^0$$



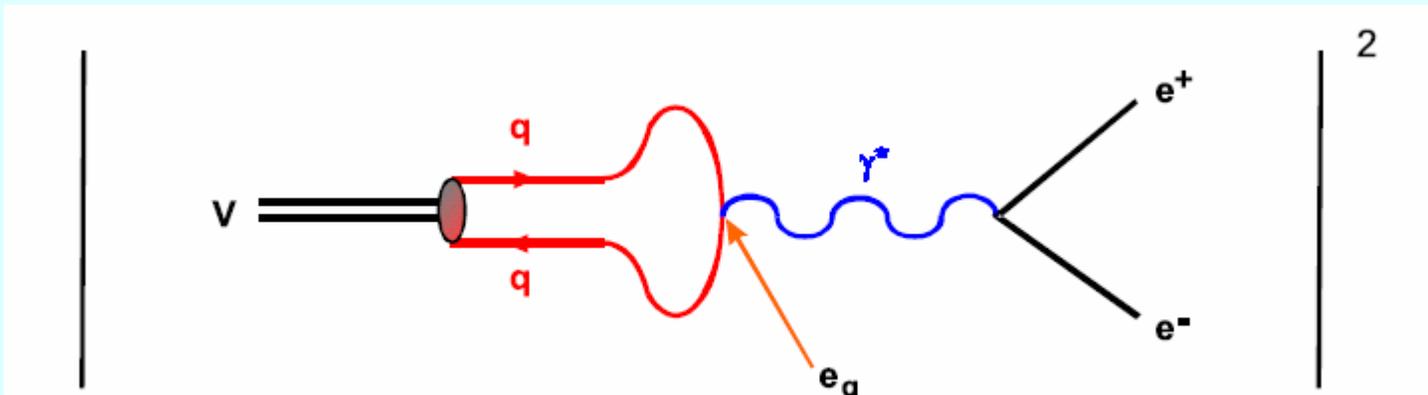
$$\phi \rightarrow K^+ K^-, K^0 \bar{K}_0$$

Mass: middle..... light..... ..heavy

Vector 1^{--} and tensor 2^{++} are flavour pure nonets

- Evidence:
1. masses of nn^* , K and ss^* states
 2. strong decays
 3. Electromagnetic transitions “weigh” the flavours

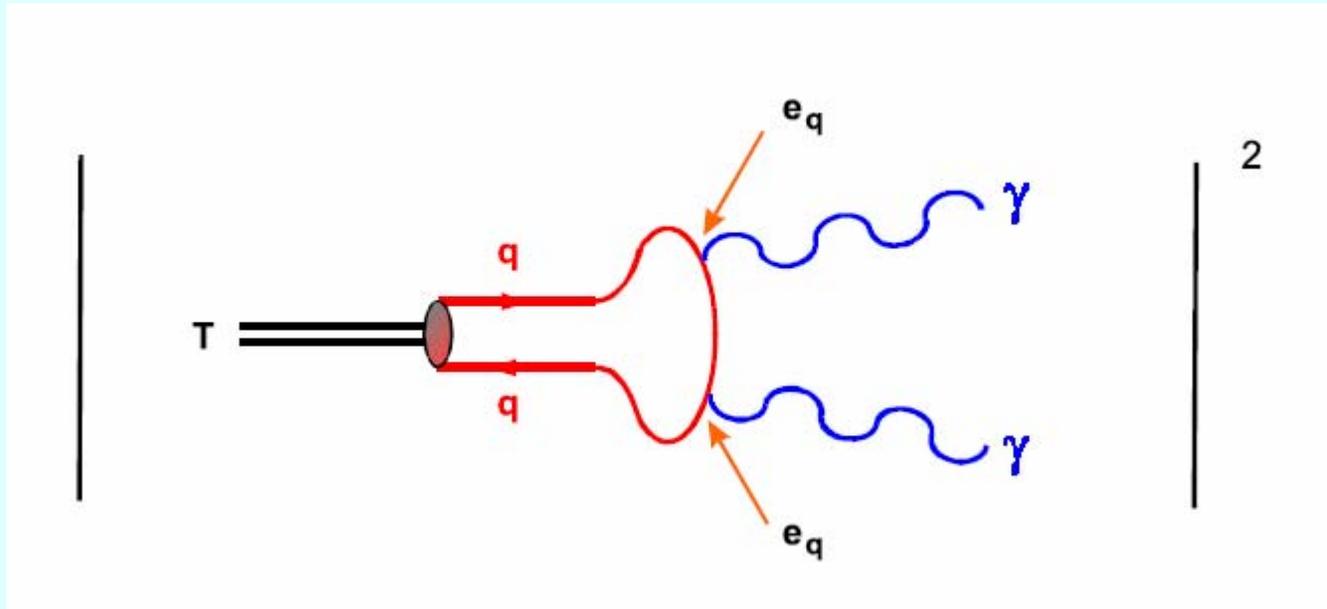
e.g. of electromagnetic: vector mesons



$$\Gamma(\rho^0 \rightarrow e^+e^-) : \Gamma(\phi \rightarrow e^+e^-) : \Gamma(\omega \rightarrow e^+e^-) =$$

$$\left[\frac{1}{\sqrt{2}} \left(\left(\frac{2}{3} \right) - \left(-\frac{1}{3} \right) \right) \right]^2 : \left(-\frac{1}{3} \right)^2 : \left[\frac{1}{\sqrt{2}} \left(\left(\frac{2}{3} \right) + \left(-\frac{1}{3} \right) \right) \right]^2 = 9 : 2 : 1$$

e.g of electromagnetic: tensor mesons

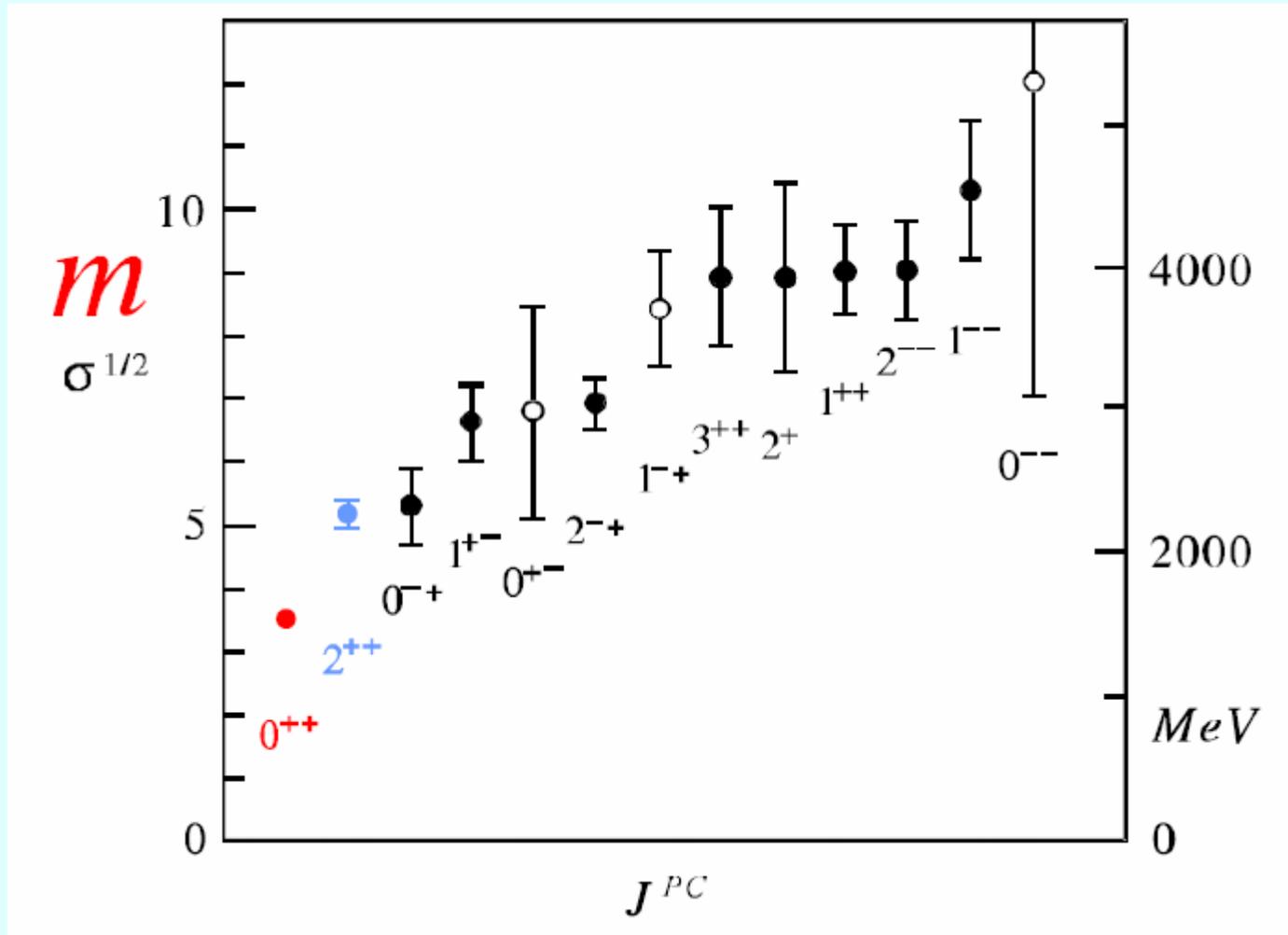


$$\Gamma(T \rightarrow \gamma\gamma) \sim \alpha^2 \langle e_q^2 \rangle^2$$

$$\Gamma(f_2(1270) \rightarrow \gamma\gamma) : \Gamma(a_2(1320) \rightarrow \gamma\gamma) : \Gamma(f_2'(1525) \rightarrow \gamma\gamma) = 25 : 9 : 2$$

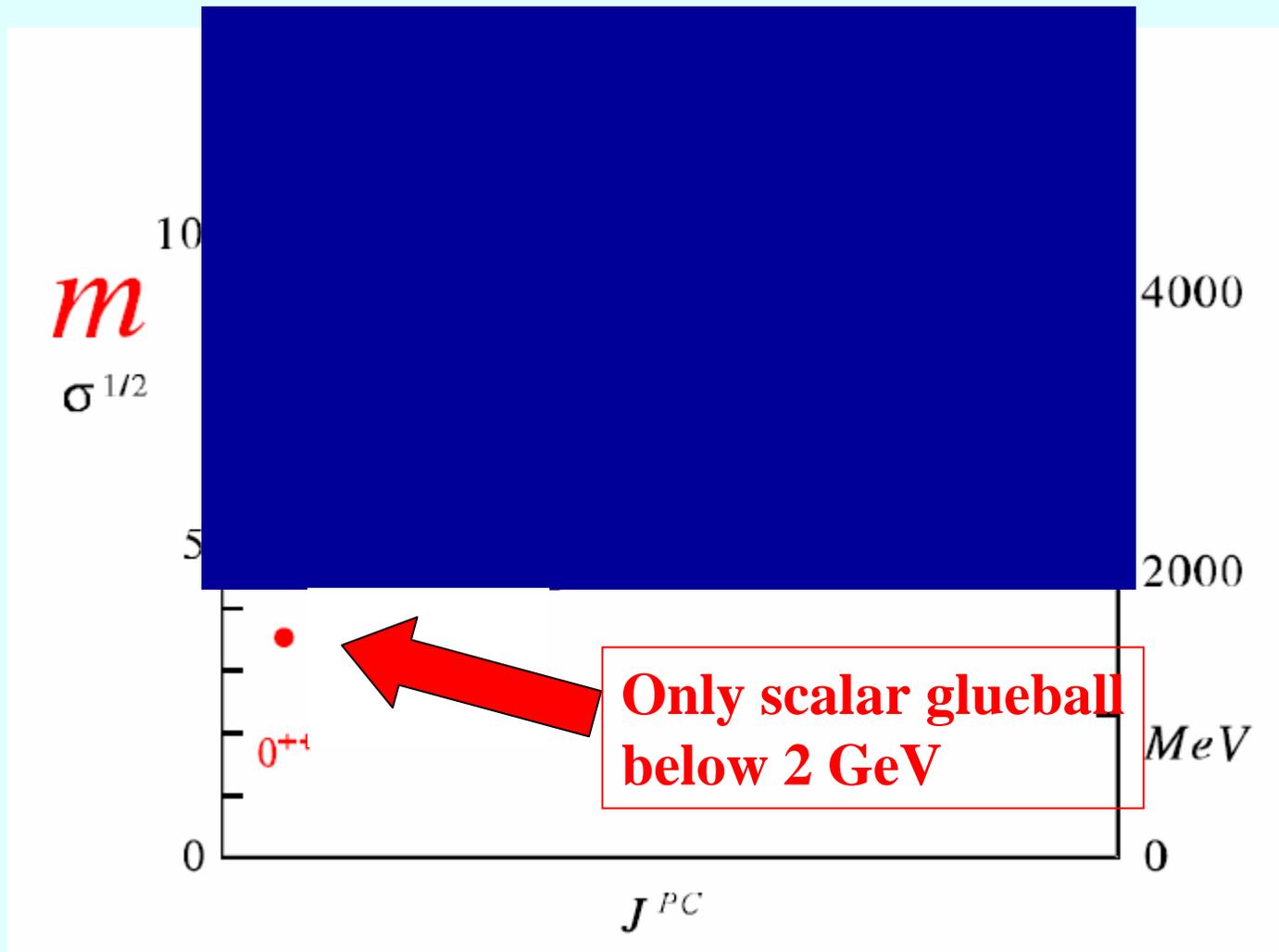
$$25 : (10 \pm 1) : (1 \pm 1)$$

Glueballs spectrum from Lattice



Far away from qq^* lowest multiplets... **except for 0^{++}**

Glueballs also predicted: Strong QCD spectrum from Lattice



Far away from qq^* lowest multiplets... **except for 0^{++}**

$l=1$ vector :

$l=0$ nn^* ; ss^*

+ Problem of nn^* ss^* flavour mixing

1D: 1- 1700

2S: 1- 1460

2+ 1320 1270/1525

1+ 1300 1285/1530

0+ 1420

1S: 1- 770 780/1020

Clean below S-wave MM thresholds
And no prominent G expected

$I=1$ vector :

$I=0$ nn^* ; ss^*

+ Problem of nn^* ss^* flavour mixing

1D: 1- 1700

2S: 1- 1460

2_+ 1320 1270/1525

1_+ 1300 1285/1530

0_+ 1420 1370/1500/1710

1S: 1- 770 780/1020

$l=1$ vector : $l=0$ $J^P = 2^+ 1^+ 0^+$

1D: 1- 1700

2S: 1- 1460

2_+ 1320 1270/1525

1_+ 1300 1285/1530

0_+ 1420 1370/1500/1710
980 980/600

1S: 1- 770

$l=1$ vector : **$l=0$ $J^P = 2^+ 1^+ 0^+$** (nn^* ss^*)

1D: 1- 1700

2S: 1- 1460

qq* seed dominates
If no S-wave meson
channels are open.

S-wave hadrons hide qq*

Production channels
give different impressions
of Fock state

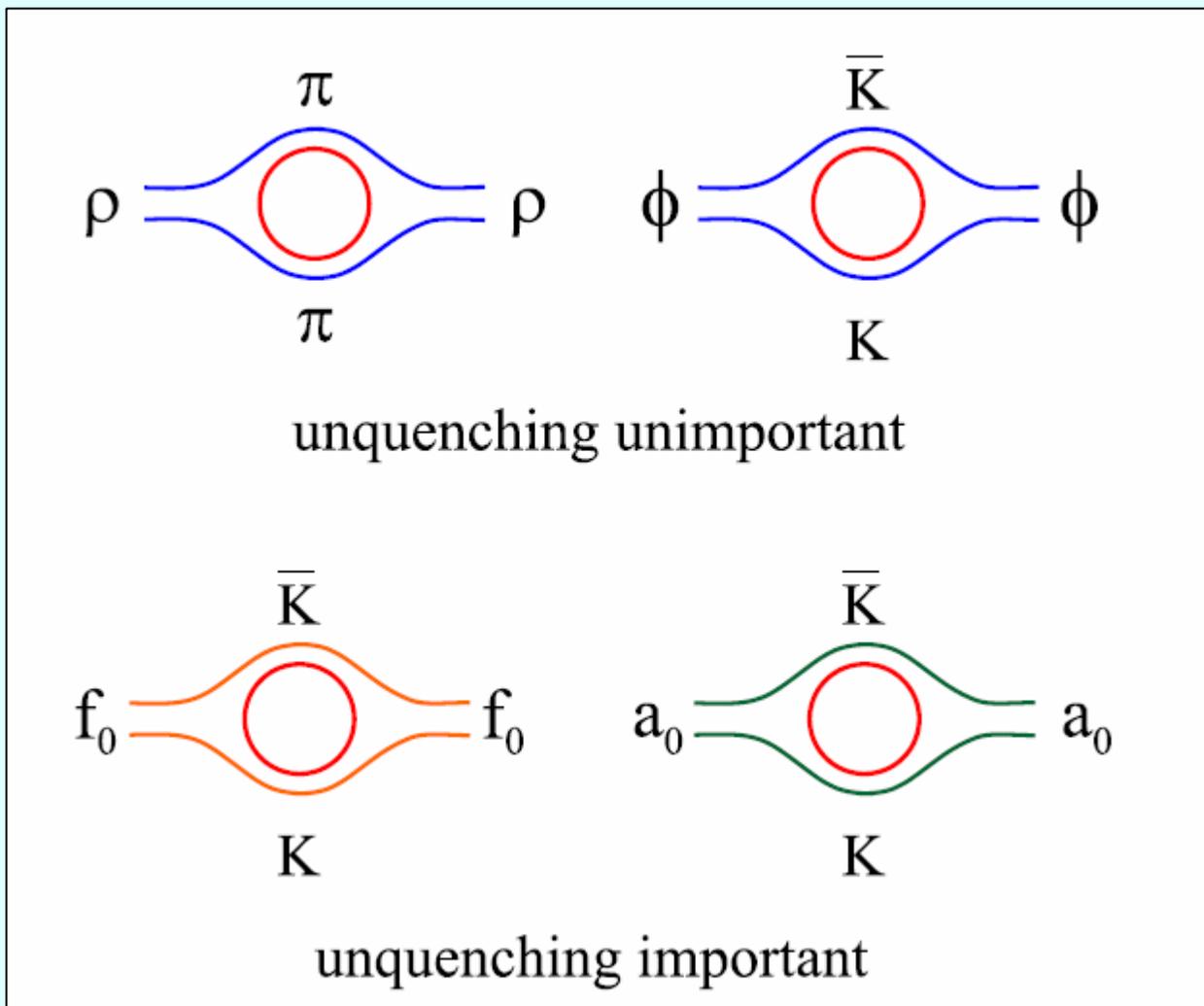
2+ 1270/1525

1+ 1285/1530

1S: 1- 770

Big problem for scalars
which couple to pi pi etc
in s-wave even though qq*
is in p-wave

Comment 1. Role of S-waves: multiquarks; especially scalars



This produces the scalars below 1 GeV (tetraquarks or molecules later)

Comment 2: Scalar glueball @ 1.6 GeV will affect scalars above 1 GeV

$l=1$ vector : $l=0$ $J^P = 2^+ 1^+ 0^+$

1D: 1- 1700

2S: 1- 1460

2^+ 1270/1525

? qq* + Glueball

Lattice G = 1.6 \pm

1^+ 1285/1530

0^+ 1370/1500/1710
980/600

1S: 1- 770

$l=1$ vector : $l=0$ $J^P = 2^+ 1^+ 0^+$

1D: 1- 1700

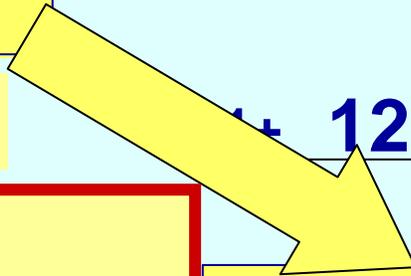
2S: 1- 1460

2^+ 1270/1525

? qq^* + Glueball

Lattice $G = 1.6$ μm

1^+ 1285/1530



**0^+ 1370/1500/1710
980/600**

Data do not imply G
But given lattice and qq^*
Does consistent pic emerge?

Can data eliminate it; or even make it robust?

