

Phenomenology at low Q^2

Lecture III

Barbara Badelek

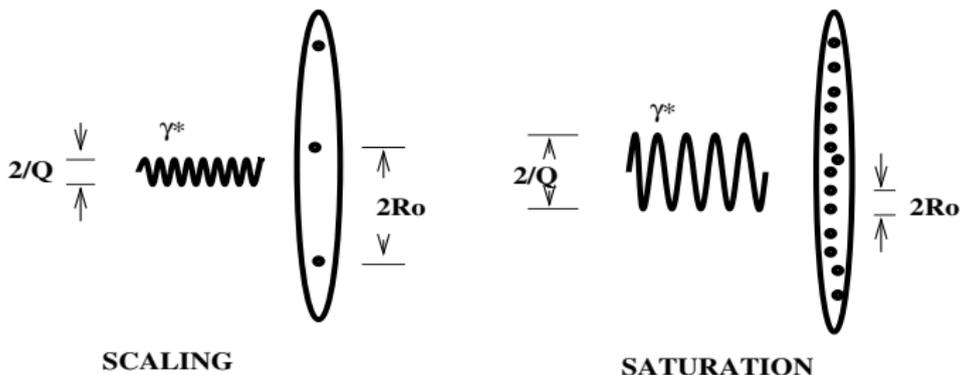
Warsaw University and Uppsala University

HUGS @ JLAB
June 2006

- 1 Parton shadowing at low x
- 2 Saturation and geometric scaling at low x
- 3 R and F_L in the low Q^2 , low x region
 - Introduction
 - F_L at HERA
 - BKS
 - R1999
- 4 F_2^γ in the low Q^2 , low x region
- 5 Summary

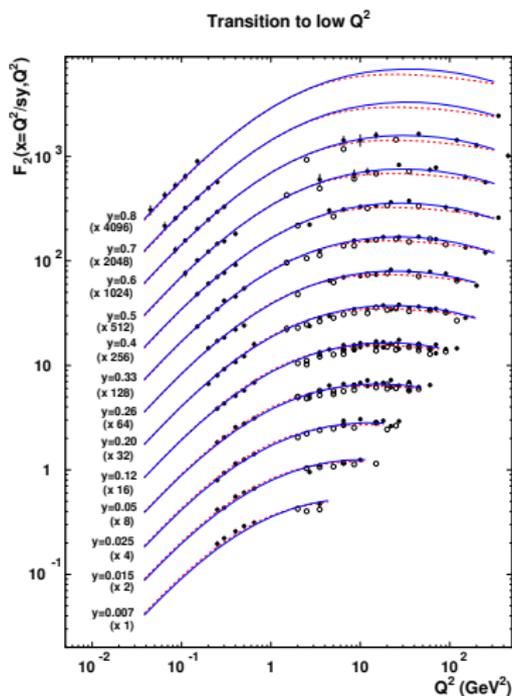
DIS in the **proton rest frame**: a clear separation in time between γ^* forming a $q\bar{q}$ dipole and dipole's interaction with proton.

Postulate dipole's cross section and fit its parameters.



Observe that 2 scales matter: dipole's size ($\sim 1/Q$) and separation between partons (R_0).

Gives good description of the electroproduction data **and** of the diffraction!



Data: H1 and ZEUS;

curves (plotted for $x < 0.01$): the saturation model of [Bartels, Golec-Biernat, Kowalski, Phys. Rev. D66 \(2002\) 014001](#).

Saturation and geometric scaling at low x

see e.g. Golec-Biernat, hep-ph/0109010

$$\tau = Q^2 R_0^2(x)$$

G.s. is a manifestation
of an internal saturation scale,

$$Q_s(x) \sim 1/R_0(x)$$

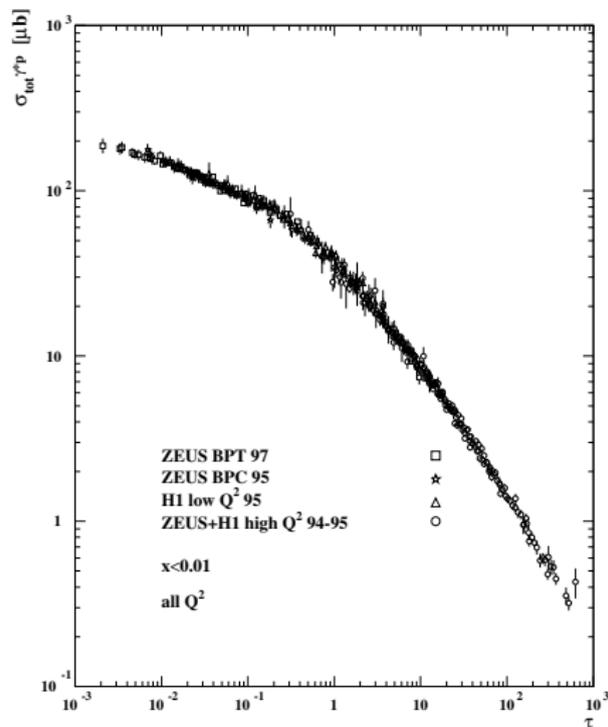
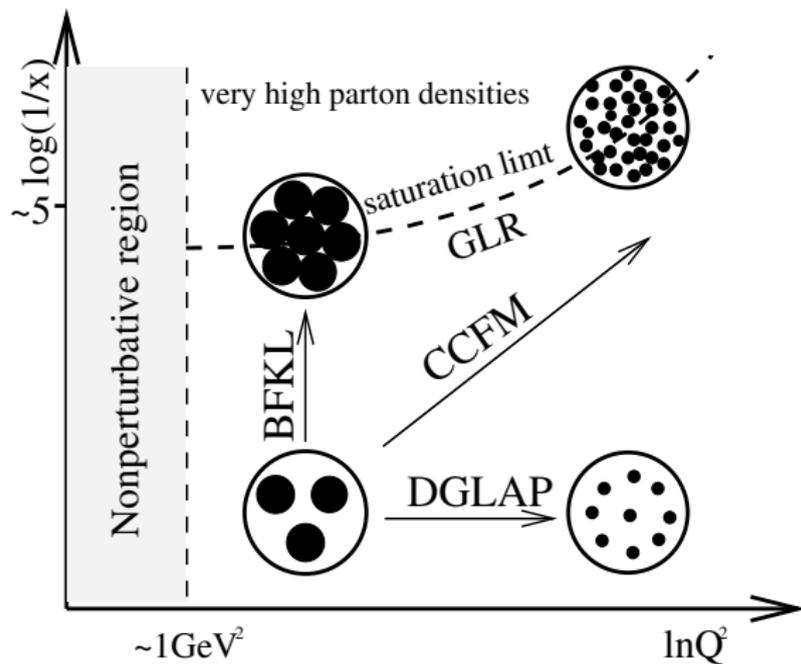


Figure 5. Experimental data on $\sigma_{\gamma,p}$ from the region $x < 0.01$ plotted versus scaling variable $\tau = Q^2 R_0^2(x)$. Q^2 values are between 0.045 and 450 GeV²

Saturation and geometric scaling at low x

see e.g. Golec-Biernat, hep-ph/0109010 ...cont'd



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R and F_L in the low Q^2 , low x region

Introduction

- Experimental determination of $F_L(x, Q^2)$ (or $R = F_L/F_T = F_L/(F_2 - F_L)$) difficult; needed measurements of the y (or energy) dependence of the cross section at fixed x and Q^2 since (neglecting m^2 and M^2 terms):

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4 x} Y_+ \left(\frac{1 + \epsilon R}{1 + R} \right) F_2(x, Q^2), \quad Y_{\pm} = 1 \pm (1 - y)^2 \quad (1)$$

- At low x dominant contribution to F_L comes from gluons \implies [learning about gluons!](#)
- In QPM, i.e. at $Q^2 \rightarrow 0$, $F_L \sim (\langle m_q^2 \rangle + \langle \kappa_T^2 \rangle)/Q^2$ where m_q and κ_T are quark's mass and transverse momentum (limited in QPM). This is \approx valid in the LL Q^2 QCD.
- In the NLO QCD, $\langle \kappa_T^2 \rangle$ grows as Q^2 with $Q^2 \nearrow \implies F_L$ acquires a LT contribution, $\sim \alpha_s(Q^2)$.
- For $Q^2 \rightarrow 0$, $F_L \sim Q^4$ (for fixed ν). Observe that $\sigma_L \sim F_L/Q^2$ vanishes at photoproduction.
- Measurements of R extend down to $Q^2 \approx 0.3 \text{ GeV}^2$ and $x \approx 0.01$. They come from different targets since $R^A - R^d$ is consistent with 0 (e.g. NMC, Nucl. Phys. B481 (1996) 23). Thus in the data analysis one usually assumes that $R(x, Q^2) = R(x, Q^2 = 0.5 \text{ GeV}^2)$ with 100% uncertainty for $Q^2 < 0.5 \text{ GeV}^2 \implies$ systematic errors. Models ?
- At large Q^2 and large x ($x \gtrsim 0.1$) data on R well described by the QCD. At moderate Q^2 , HT contribution $\sim 1/Q^2$ needed. Little known about R (or F_L) at low Q^2 .

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F_L Extraction - H1

$$\sigma_r = \left(\frac{2\pi\alpha^2 Y_+}{xQ^4} \right)^{-1} \frac{d^2\sigma}{dx dQ^2} = \left[F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \right]$$

Three techniques:

1. Subtraction method: $F_L = \frac{Y_+}{y^2} [F_2 - \sigma_r]$

- Extract F_2 in low y region, extrapolate to higher y (Q^2) using NLO DGLAP

2. Derivative Method: $\left. \frac{\partial \sigma_r}{\partial \ln y} \right|_{Q^2}$

- F_L dominates the derivative at large y . Subtract contribution from F_2

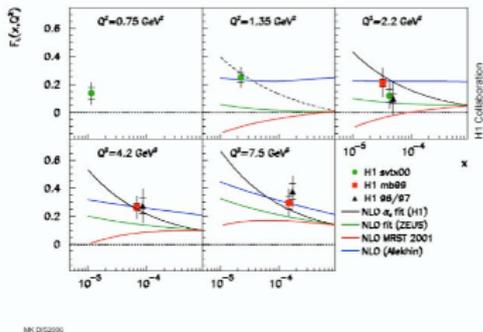
3. Shape Method: Fit σ_r assuming $F_2 = ax^{-\lambda}$ and $F_L = c$ at high y

R and F_L in the low Q^2 , low x region

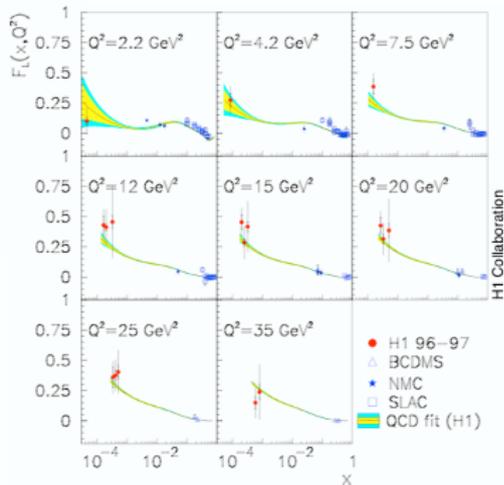
F_L at HERA...cont'd

F_L Extraction - H1

Results on extracting F_L at low Q^2 - H1 preliminary



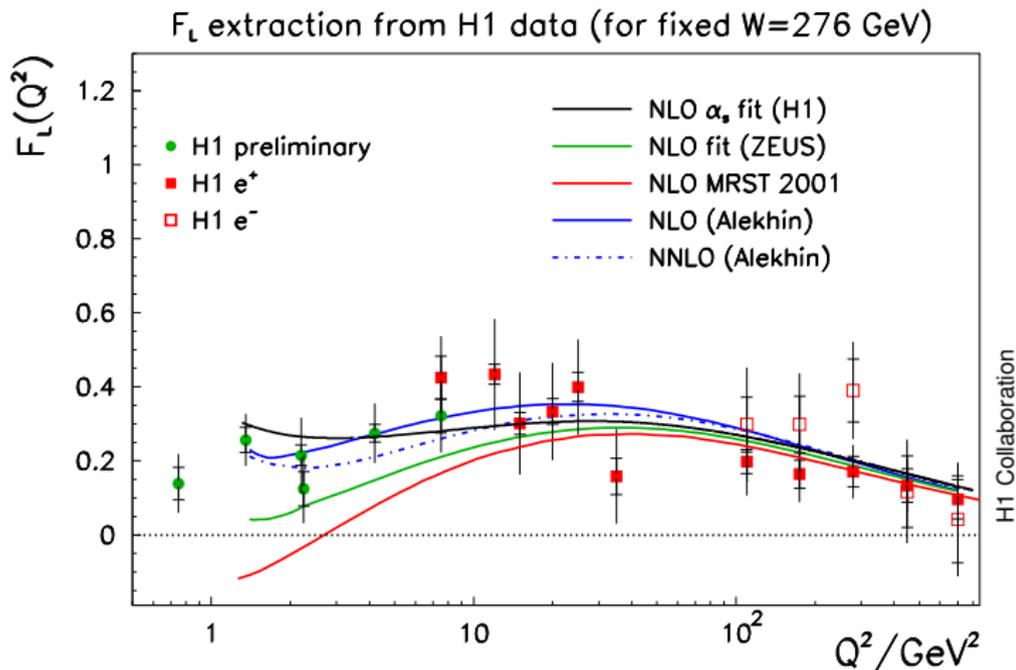
MR 02/2000



Extraction of F_L with assumptions about behavior of F_2 . Could be dangerous since small- x physics not well understood. Better - direct measurement of F_L by varying the CM energy.

R and F_L in the low Q^2 , low x region

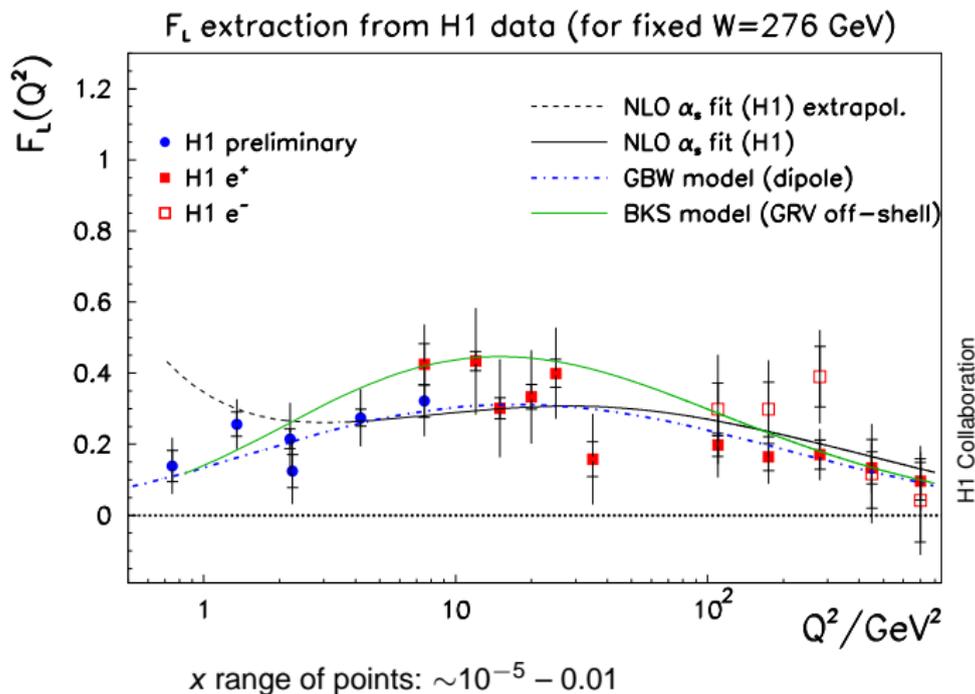
F_L at HERA...cont'd



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R and F_L in the low Q^2 , low x region

F_L at HERA...cont'd

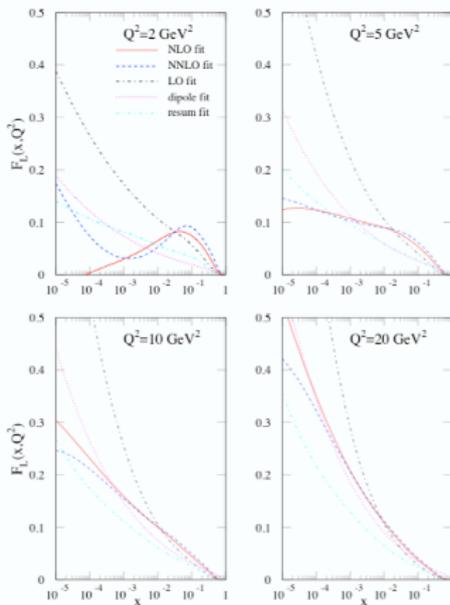


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R and F_L in the low Q^2 , low x region

F_L at HERA...cont'd

Predictions for F_L



F_L predictions from MRST group at different orders in DGLAP, a fit which resums the leading $\ln(1/x)$ and β_0 terms, and a dipole type model. Very large differences at small Q^2 where gluon uncertainty large.

R and F_L in the low Q^2 , low x region

F_L at HERA...cont'd

Predictions for the longitudinal structure function

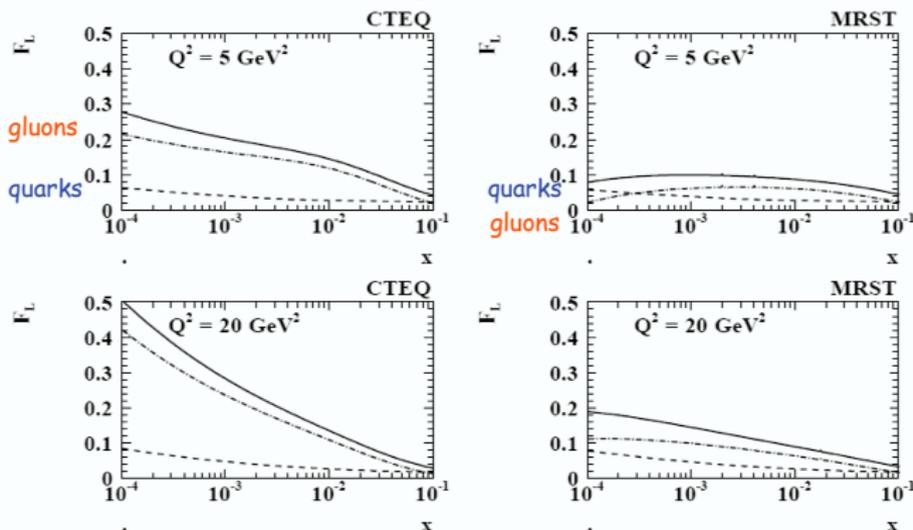


Figure 2. Calculation of the longitudinal structure function $F_L(x, Q^2)$ (solid lines) using the CTEQ6 (left) and the MRST2002 (right) parton distributions and Eq.2 for 4 flavours and α_s to NLO. Note that not only the predicted values for F_L differ but as well drastically the relative contributions from gluons (dashed dotted lines) and sea quarks (dashed lines). For MRST at low x , contrary to common belief, $F_L(x, Q^2)$ is not gluon dominated. Both sets of parton distributions describe the H1 data on F_2 well.

G. Altarelli and G. Martinelli, Phys.Lett. B76 (1978) 89.

MK DIS2006

$$F_L = \frac{\alpha_s}{4\pi} x^2 \int_x^1 \frac{dz}{z^3} \cdot \left[\frac{16}{3} F_2 + 8 \sum e_q^2 \left(1 - \frac{x}{z}\right) z g \right]$$

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R and F_L in the low Q^2 , low x region

BKS (Badelek, Kwicinski, Stasto, Z. Phys. C74 (1997) 297)

- A model for F_L , valid at low x and low Q^2 ; based on the photon–gluon fusion, essential at low x and extended to low Q^2 . Similar approach in Nikolaev, Zakharov, Z. Phys. C49 (1991) 607, C53 (1992) 331
- The model embodies the constraint $F_L \sim Q^4$ at $Q^2 \rightarrow 0$.

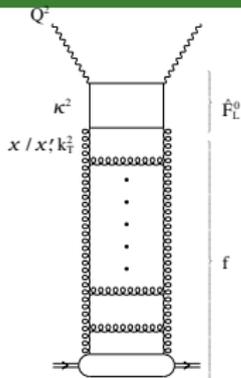
$$F_L = \int_x^1 \frac{dx'}{x'} \int \frac{dk_T^0}{k_T^0} F_L^0(x', Q^2, k_T^0) f\left(\frac{x}{x'}, k_T^2\right)$$

where F_L^0 comes from $\gamma^* g$ fusion, is a longitudinal structure function of the off-shell gluon of virtuality k_T^2 and is calculated perturbatively; f is an unintegrated gluon distribution related to the “ordinary” $g(y, \mu^2)$ by:

$$yg(y, \mu^2) = \int^{\mu^2} \frac{dk_T^2}{k_T^2} f(y, k_T^2)$$

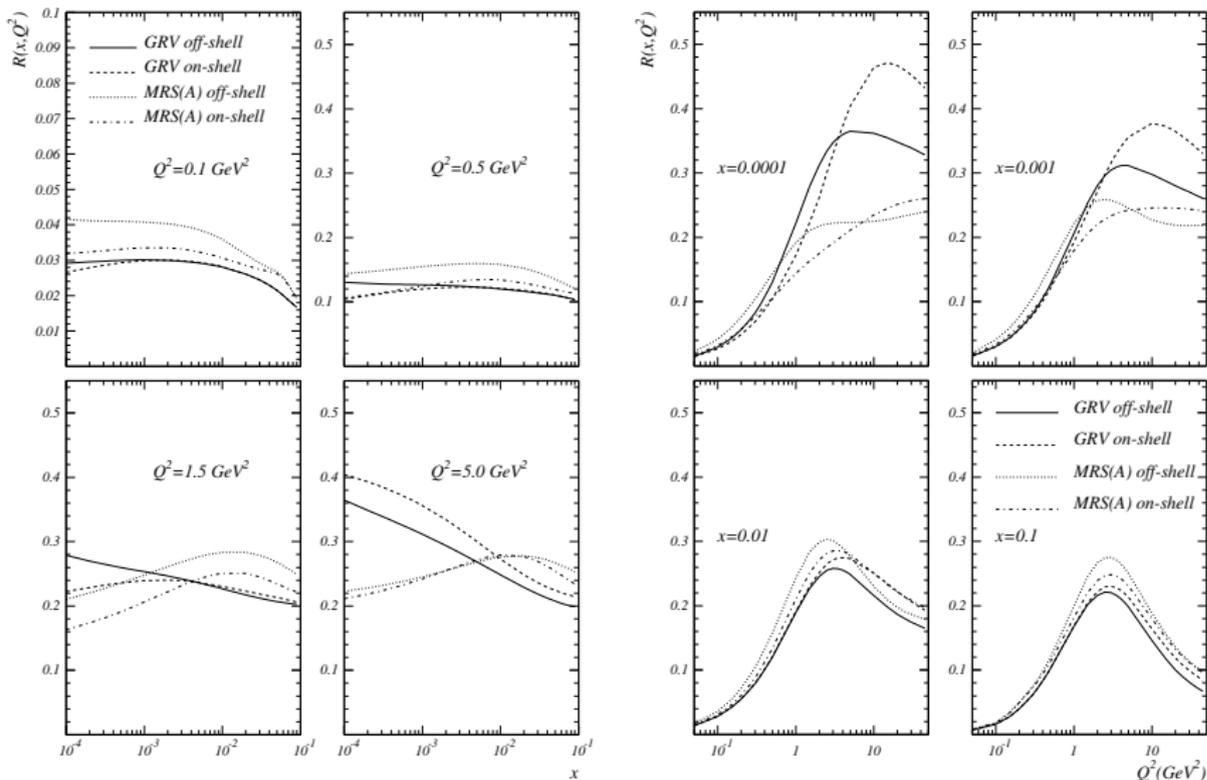
Its evolution is controlled by (approximate) BFKL.

- To extrapolate F_L to low Q^2 and to $Q^2 = 0$, evolution of $g(y, Q^2)$ and argument of $\alpha_s(Q^2)$ was frozen *via* $Q^2 \rightarrow Q^2 + 4m_q^2$.
- HT contribution needed at moderate Q^2 , i.e. terms vanishing as $1/Q^2$ for $Q^2 \rightarrow \infty$. They were assumed to originate from low values of the quark transverse momenta and interpreted as coming from soft pomeron exchange (intercept = 1). Such HT has a proper behaviour both at $Q^2 \rightarrow \infty$ and $Q^2 \rightarrow 0$.



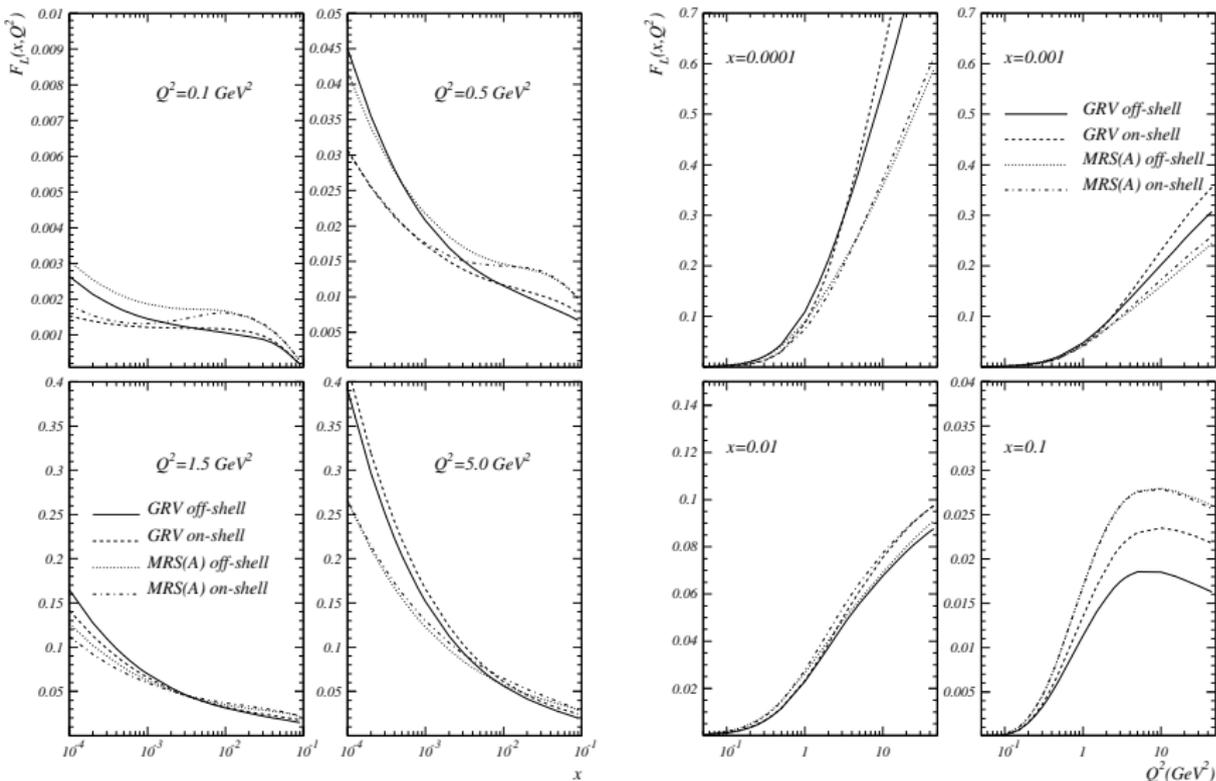
R and F_L in the low Q^2 , low x region

BKS (Badelek, Kwiecinski, Stasto, Z. Phys. C74 (1997) 297)...cont'd



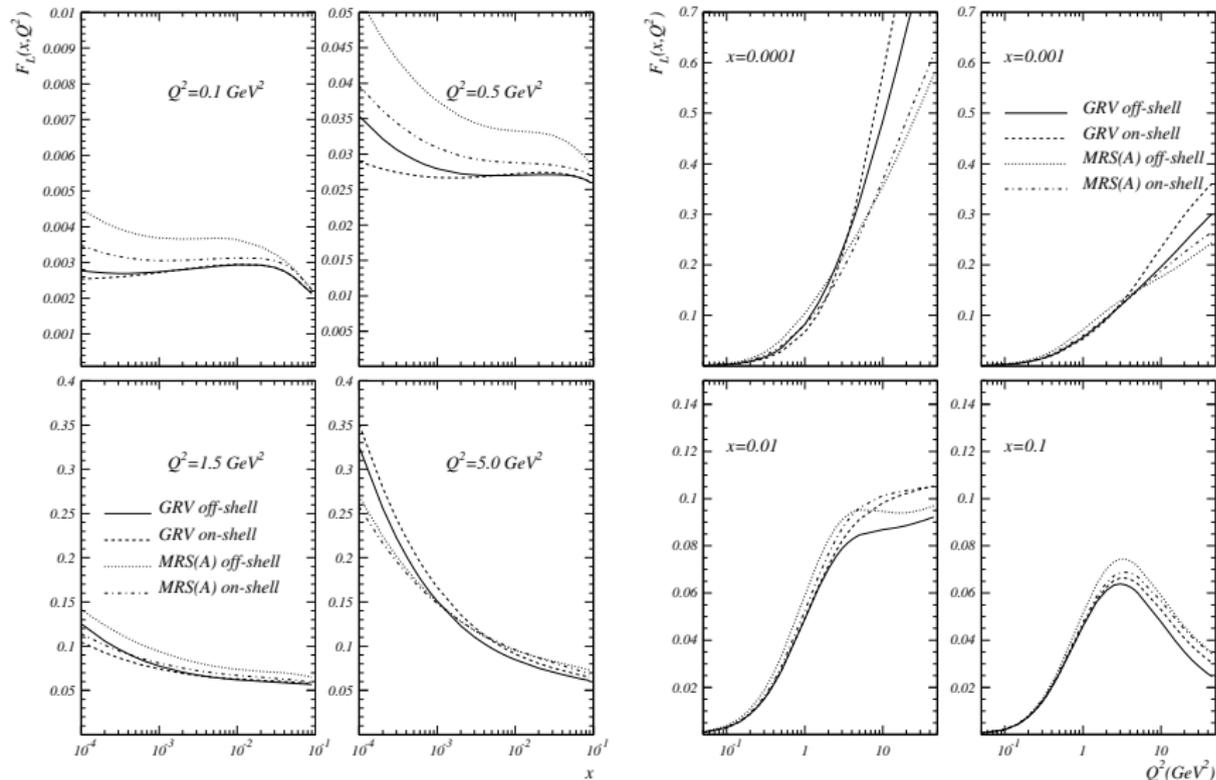
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BKS (Badelek, Kwicinski, Stasto, Z. Phys. C74 (1997) 297)...cont'd



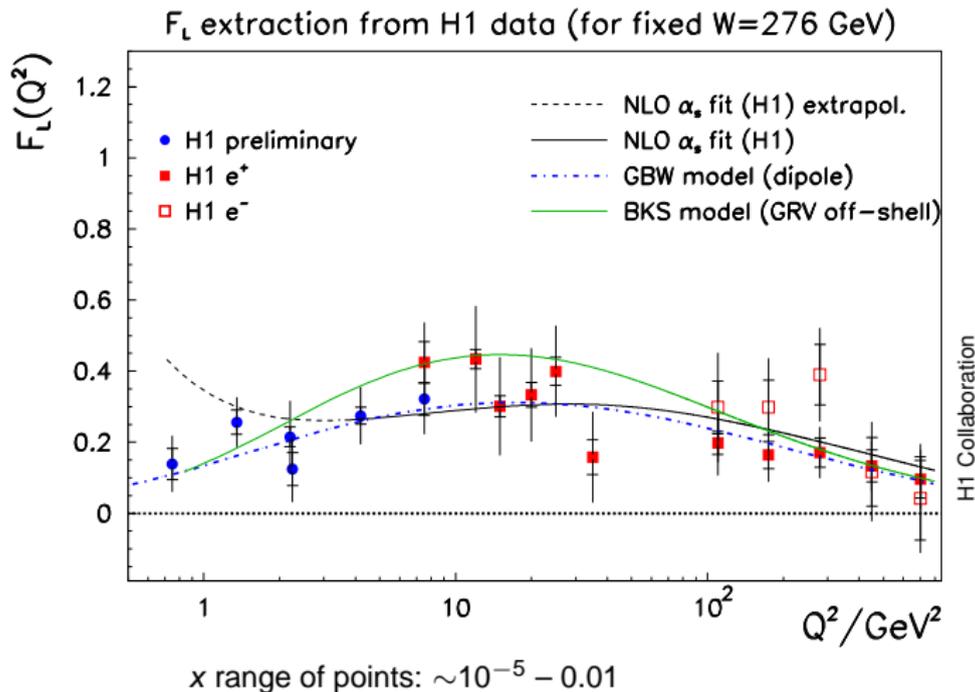
R and F_L in the low Q^2 , low x region

BKS (Badelek, Kwicinski, Stasto, Z. Phys. C74 (1997) 297)...cont'd



R and F_L in the low Q^2 , low x region

BKS ...cont'd

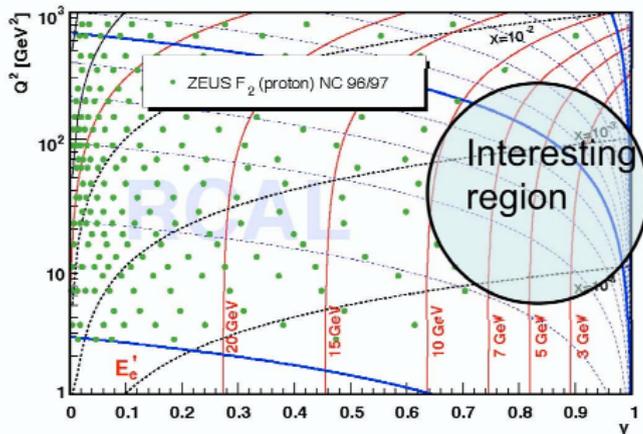


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R and F_L in the low Q^2 , low x region

F_L at HERA...cont'd

Measuring F_L



Need to go to lowest possible scattered electron energy:

- lower E_p rather than E_e
- trigger efficiency
- electron finder efficiency
- electron finder purity (photoproduction background, wrong candidate)

A. Caldwell, DIS2006

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R1999 (SLAC, Phys. Lett. B452 (1999) 194)

Data in the range $0.005 \leq x \leq 0.86$, $0.5 \leq Q^2 \leq 130 \text{ GeV}^2$ were fitted by 6-parametr fits (3 indep. models).

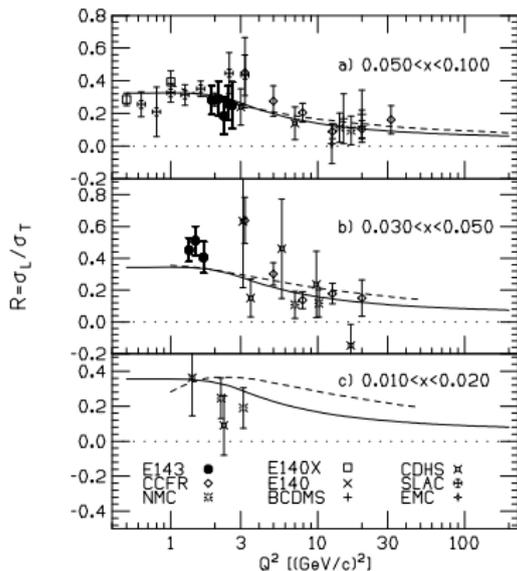


FIG. 3. R as a function of Q^2 for: a) $0.05 \leq x \leq 0.10$; b) $0.03 \leq x \leq 0.05$; c) $0.01 \leq x \leq 0.02$. The solid curve is the average of the new fits, R1998, and the dashed curve is the NNLO pQCD calculation described in the text.

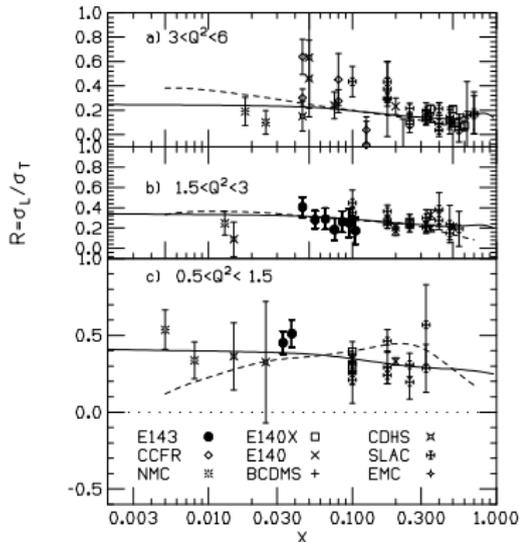


FIG. 4. R as a function of x for: a) $3 \leq Q^2 \leq 6 (\text{GeV}^2/c^2)$; b) $1.5 \leq Q^2 \leq 3 (\text{GeV}^2/c^2)$; c) $0.5 \leq Q^2 \leq 1.5 (\text{GeV}^2/c^2)$. The solid curve is the average of the new fits, R1998, and the dashed curve is the NNLO pQCD calculation described in the text.

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F_2^γ in the low Q^2 , low x region

(Badelek, Krawczyk, Kwieciński, Stasto, Phys.Rev. D62 (2000) 074021)

In a full analogy with the BBJK formulation of the F_2^p :



$$F_2^\gamma(x, Q^2) = F_2^{\text{VMD}}(x, Q^2) + F_2^{\text{partons}}(x, Q^2) \quad (2)$$

where

$$F_2^{\text{VMD}}(x, Q^2) = \frac{Q^2}{4\pi} \sum_V \frac{M_V^4 \sigma_{V\gamma}(W^2)}{\gamma_V^2 (Q^2 + M_V^2)^2},$$

$$F_2^{\text{partons}}(x, Q^2) = \frac{Q^2}{Q^2 + Q_0^2} F_2^{\text{QCD}}(\bar{x}, Q^2 + Q_0^2),$$

$$\bar{x} = \frac{Q^2 + Q_0^2}{W^2 + Q^2 + Q_0^2}.$$

- F_2^{QCD} is taken from the QCD analysis, valid in the large Q^2 region.
- Modifications of the QCD contribution (\bar{x}, Q_0^2) introduce power corrections which vanish as $1/Q^2$ (i.e. are negligible at large Q^2).
- Q_0^2 is set to 1.2 GeV^2 as in the F_2^p .
- Sum over V in F_2^{VMD} is for $M_V^2 < Q_0^2$ only, i.e. over ρ, ω, ϕ .
- The model is valid at low x and any value of Q^2
- At $Q^2 \rightarrow \infty$, $F_2^\gamma(x, Q^2) \rightarrow F_2^{\text{QCD}}(x, Q^2)$

- A total $\gamma^*\gamma$ cross-section in the high energy limit:

$$\sigma_{\gamma^*\gamma}(W, Q^2) = \frac{4\pi^2\alpha}{Q^2} F_2^\gamma(x, Q) \quad (3)$$

with $x = Q^2/(Q^2 + W^2)$. Its $Q^2 = 0$ (for fixed W) limit of gives the total cross-section $\sigma_{\gamma\gamma}(W^2)$ corresponding to the interaction of two real photons:

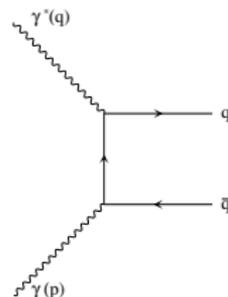
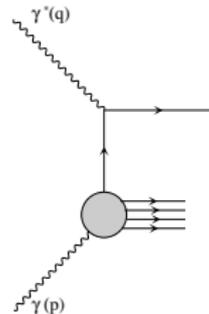
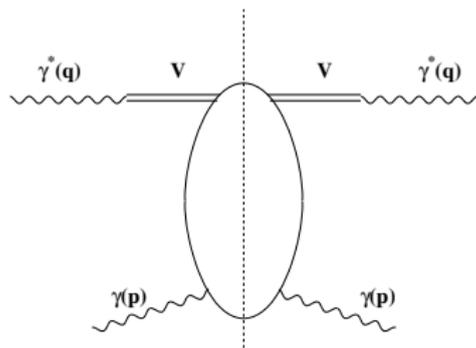
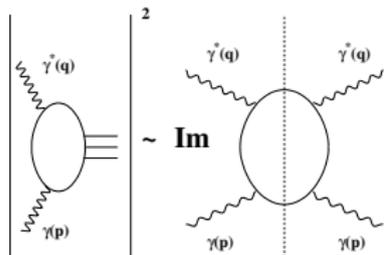
$$\sigma_{\gamma\gamma}(W) = \alpha\pi \sum_{V=\rho,\omega,\phi} \frac{\sigma_{V\gamma}(W^2)}{\gamma_V^2} + \frac{4\pi^2\alpha}{Q_0^2} F_2^{\text{QCD}}(Q_0^2/W^2, Q_0^2). \quad (4)$$

- Data on $\sigma_{\gamma\gamma}(W)$ and on $\sigma_{\gamma^*\gamma}(W, Q^2)$ and on F_2^γ at low Q^2 are fairly well reproduced.
- Natural explanation of the fact that the increase of the total $\gamma\gamma$ cross-section with increasing CM energy W is stronger than that implied by soft Pomeron exchange: the latter describes the VMD part ($W^{2\lambda}$, $\lambda=0.0808$) while the partonic component increases faster with energy ($F_2^{\text{QCD}}(\bar{x}, Q^2)$ increase with decreasing \bar{x} from the QCD evolution).
- $\sigma_{\gamma\gamma}(W) \sim (W^2)^{\lambda_{\text{eff}}}$ with λ_{eff} slowly increasing with energy: $\lambda_{\text{eff}} \sim 0.1 - 0.12$ for $30 \text{ GeV} < W < 10^3 \text{ GeV}$.

F_2^γ in the low Q^2 , low x region

(Badelek, Krawczyk, Kwieciński, Stasto, Phys.Rev. D62

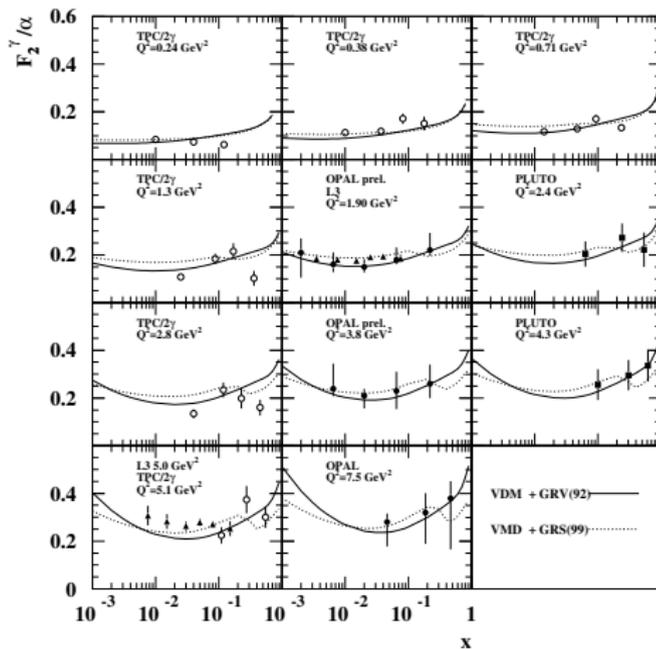
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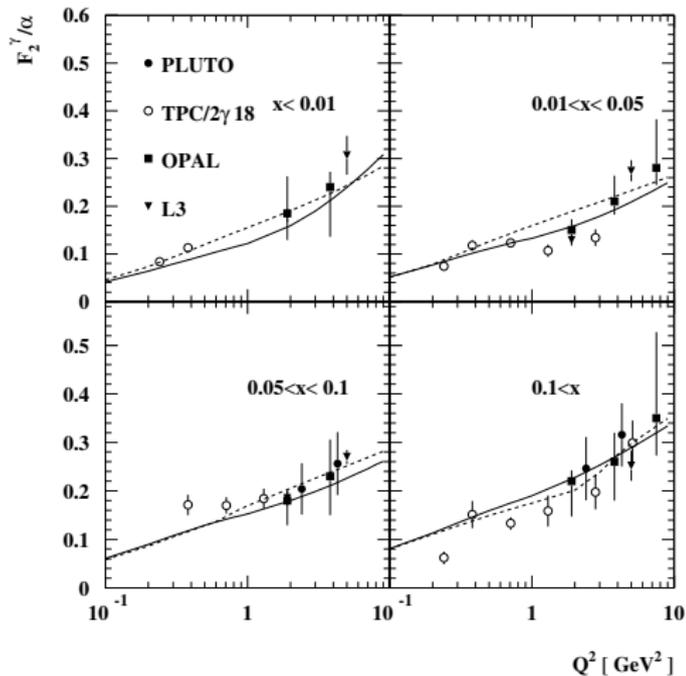
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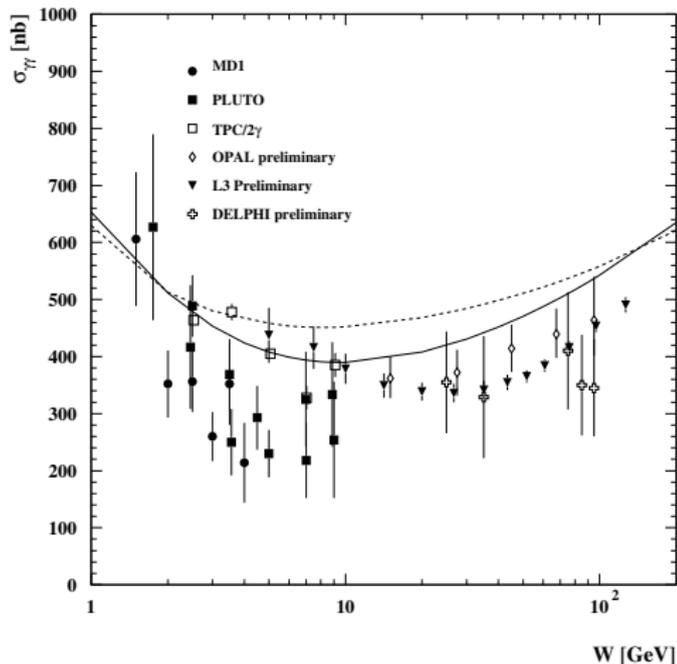
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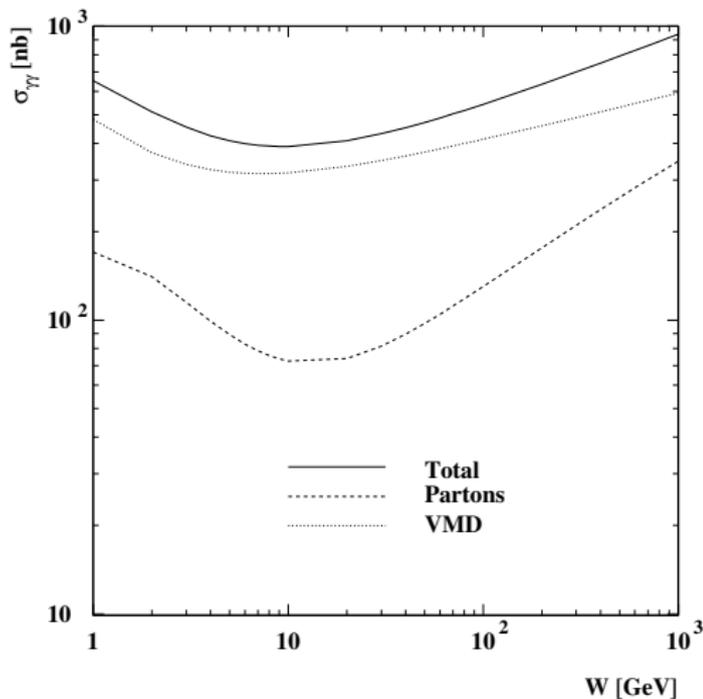
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- R and F_L poorly measured – especially at low Q^2
- Only one dynamical parametrization of the transition region exists: BKS
- Only one data fit exists: R1999 (SLAC).
- Plans to measure F_L at low x at HERA.