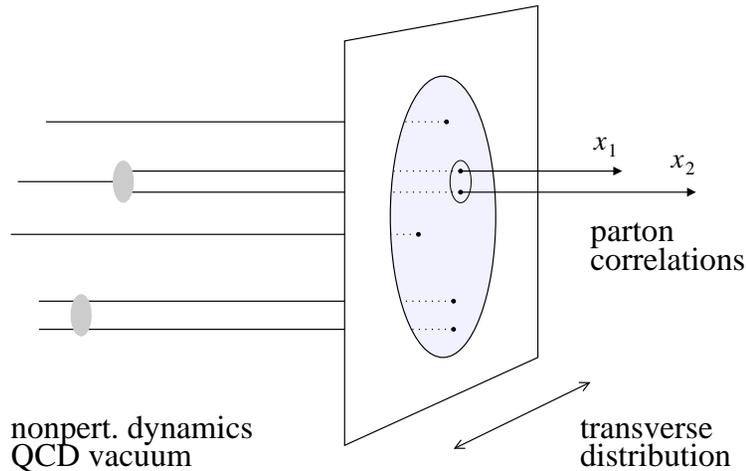
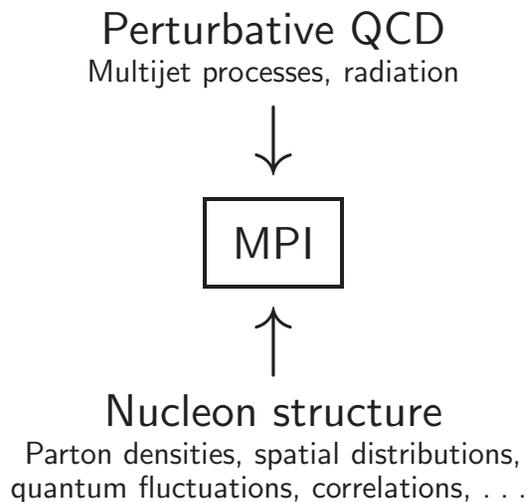


# Nonperturbative nucleon structure and MPI

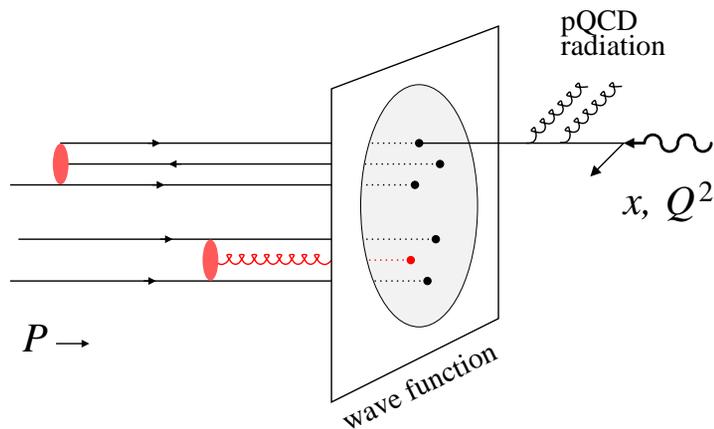
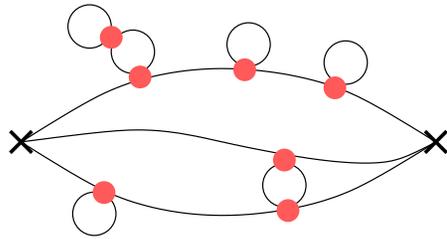
C. Weiss (JLab), MPI@TAU, Tel Aviv University, 15–Oct–12



- Partonic wave function of nucleon
  - Non-perturbative QCD vacuum
  - Physical properties: Spatial distributions, fluctuations, correlations
- Transverse distribution of partons
  - GPDs from exclusive  $ep/\gamma p$   
HERA, COMPASS, HERMES, JLab12
  - Hard vs. soft  $pp$  interactions
  - Importance for MPI
- Quantum fluctuations
  - Gluon dispersion from diffractive  $ep$  HERA
- Parton correlations
  - Short-distance scale  $\rho \sim 0.3$  fm
  - Effect on MPIs
  - Connections: Intrinsic  $p_T$  in  $ep/pp$ , higher twist, exclusive mesons



# Nucleon structure: Parton picture



- QCD vacuum not empty

Strong gluon fields of size  $\rho \ll 1$  fm

$\bar{q}q$  pair condensate,  $\pi$  as collective excitation

- Nucleon at rest

$t \rightarrow i\tau$  statistical mechanics    Lattice, analytic methods  
 $\langle N|O|N \rangle$  from correlation functions

No concept of “particle content!”

- Fast-moving nucleon  $P \gg \rho^{-1}$

Closed system: Wave function description

Gribov, Feynman. Alt: Light-front quantization

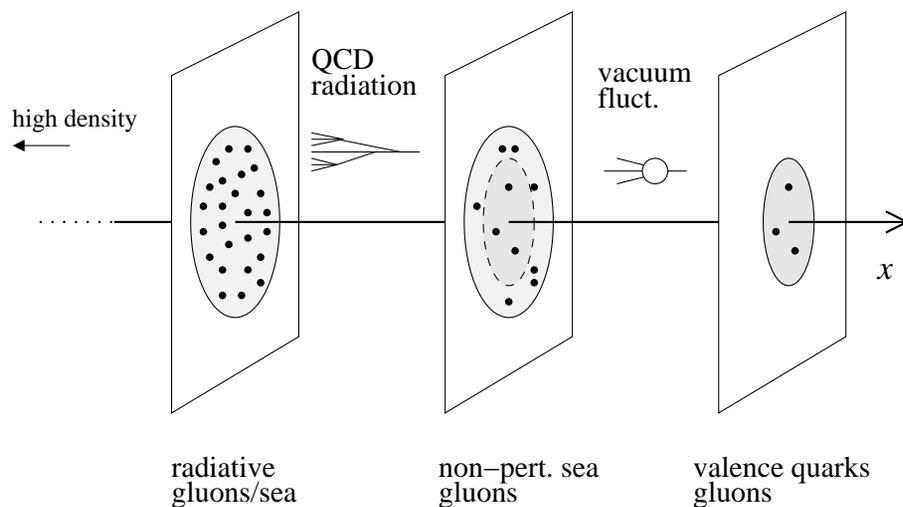
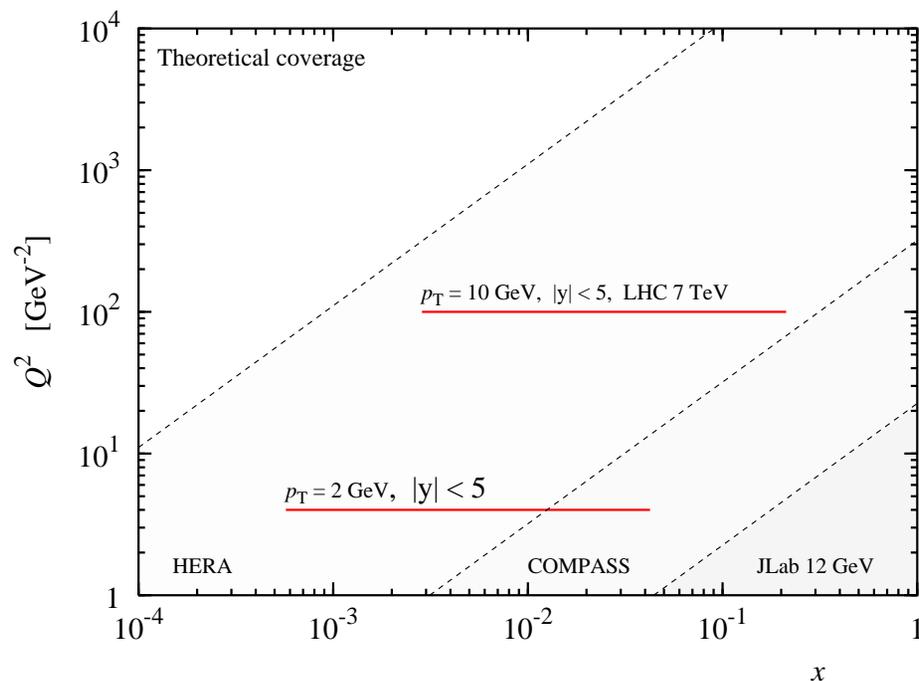
Components with different particle number

Many-body system: Constituents, interactions, spatial structure, orbital motion, . . .

Hard process “snapshot” w. resolution  $1/Q^2$

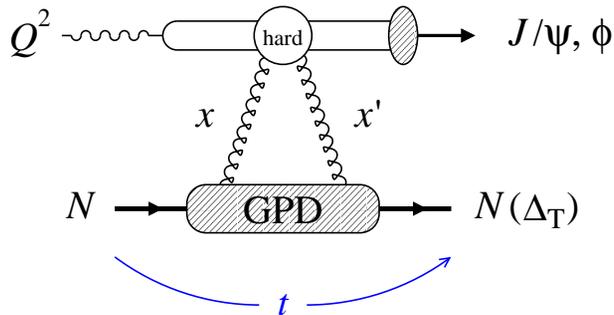
Separation of short- and long-distance interactions: Factorization  
 pQCD radiation in leading-log approximation: Scale dependence

# Nucleon structure: Many-body system



- Components probed predominantly
  - $x > 0.1$  Valence quarks: Source, quantum numbers  
Also gluons!
  - $\sim 10^{-1..2}$  Sea quarks, gluons: Quantum numbers  
Generated by non-pert. interactions
  - $x < 10^{-2}$  Gluons, singlet sea: Radiatively generated
- Physical properties
  - Particle number densities, incl. spin/flavor PDFs
  - Transverse spatial distributions GPDs
  - Orbital motion, ang. momentum TMDs
  - Quantum fluctuations: Dispersion
  - Multiparton correlations MPDs, GPDs
  - Densities with operator definition  $\langle N | \text{QCD-Op} | N \rangle$   
Calculable with non-perturbative methods  
Scale dependence from RNG equation.

# Transverse distributions: Exclusive processes



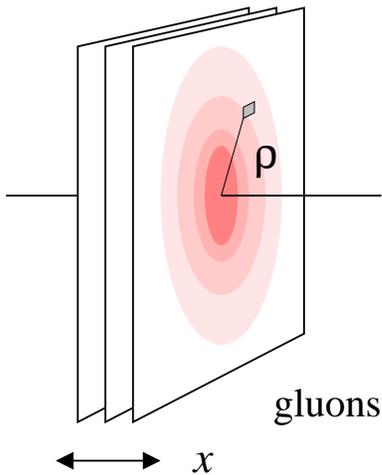
- Hard exclusive meson production

Meson produced in small-size  $q\bar{q}$  configuration

QCD factorization theorem  $Q_{\text{eff}}^2 \gg |t|$   
 Collins, Frankfurt, Strikman 96

GPDs: Partonic form factor of nucleon,  
 universal, process-independent Ji 96, Radyushkin 96

Operator definition  $\langle N' | \text{twist-2} | N \rangle$ ,  
 renormalization, non-pert. methods



- Transverse spatial distribution of gluons  $x' = x$

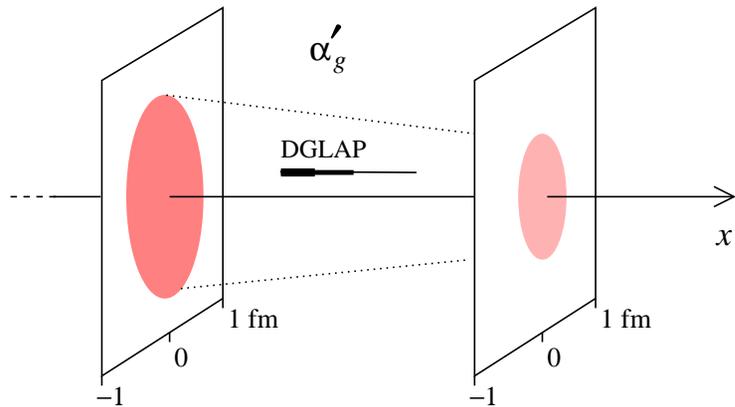
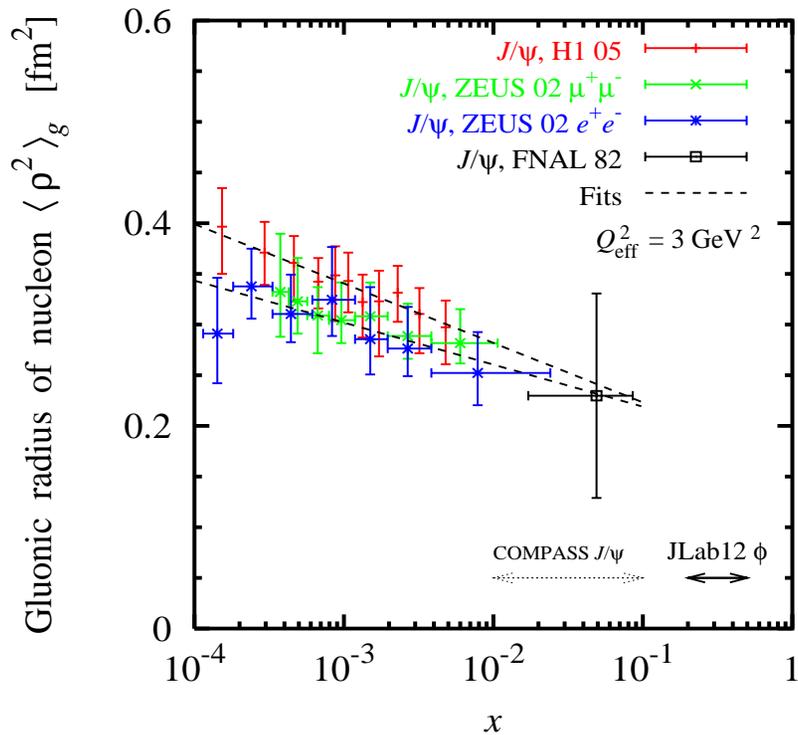
$$G(x, \rho) = \int \frac{d^2 \Delta_T}{(2\pi)^2} e^{-i\rho\Delta_T} \text{GPD}(x, t) \quad \text{2D Fourier}$$

Tomographic image of nucleon at fixed  $x$ ,  
 changes with  $x$  and  $Q^2$

- Large  $x$ : Quark GPDs, polarization,  
 longitudinal momentum transfer  $x' \neq x$

JLab12: DVCS, meson production

# Transverse distributions: Gluons



- Transverse distribution of gluons

Exclusive  $J/\psi$  photo/electroproduction  
 FNAL, HERA also  $\phi, \rho$ . Large  $x$  JLab12  $\phi$

Transverse profile from relative  $t$ -dep.

Average size from slope  $\langle \rho^2 \rangle_g = 2B_{J/\psi}$   
 Finite-size corrections

- Important observations

Average gluonic size  $\langle \rho^2 \rangle_g$  much smaller  
 than soft nucleon size  $\sim 1 \text{ fm}^2$

Grows with effective Regge slope  
 $\alpha'_g \approx 0.14 \text{ GeV}^{-2} < \alpha'_{\text{soft}}$

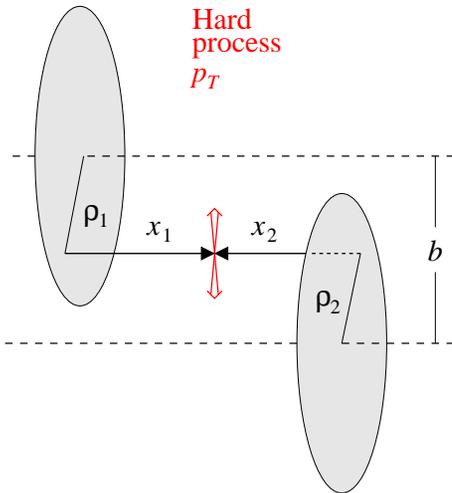
Parametrization available: Frankfurt, Strikman, CW 10

- $Q^2$  dep. from DGLAP evolution FSW04

Partons decay locally in transverse space

Size changes because initial partons at  
 $x_0 > x$  sit at smaller transv. distances  
 Small effect at  $Q^2 > \text{few GeV}^2$

# Transverse distributions: Applications to $pp$

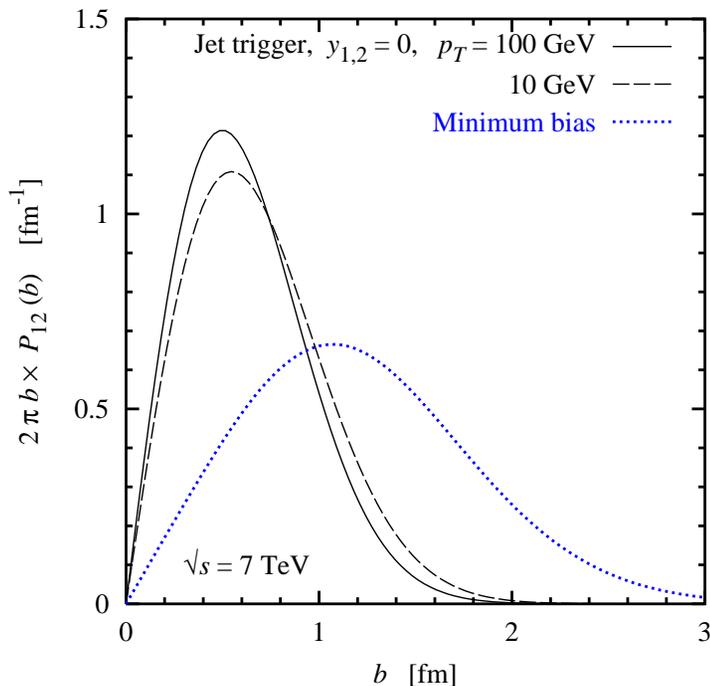


- Hard process from parton-parton collision  
Local in transverse space  $p_T^2 \gg (\text{transv. size})^{-2}$
- Cross section as function of  $pp$  impact param

$$\sigma_{12}(b) = \int d^2\rho_1 d^2\rho_2 \delta(\mathbf{b} - \boldsymbol{\rho}_1 + \boldsymbol{\rho}_2) \times G(x_1, \rho_1) G(x_2, \rho_2) \sigma_{\text{parton}}$$

Calculable from known transverse distributions  
Integral  $\int d^2b$  reproduces inclusive formula

Normalized distribn  $P_{12}(b) = \sigma_{12}(b) / [\int \sigma_{12}]$



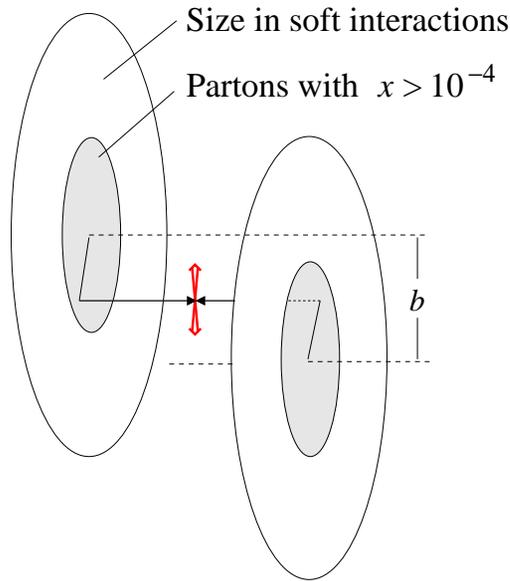
- New information available

Model spectator interactions depending on  $b$   
Underlying event

Predict probability of multiple hard processes  
Dynamical correlations? FSW04

Diffraction: Gap survival probability  
Determined largely by transverse geometry FHSW 07

# Transverse distributions: Hard vs soft interactions



- Transverse size in soft interactions from  $pp$  elastic amplitude + unitarity

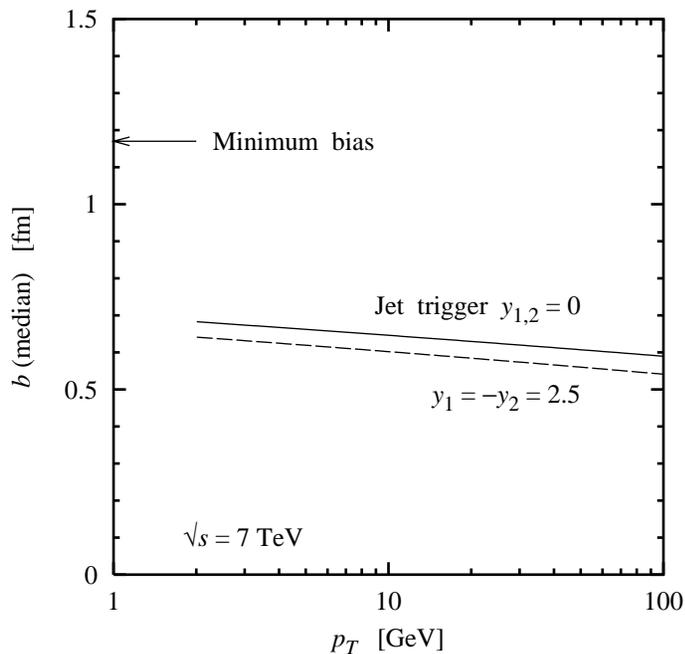
$$\sigma_{\text{soft inel}}^{pp}(b) = 1 - |1 - \Gamma(s, b)|^2$$

$$R^2(\text{soft}) \gg \langle \rho^2 \rangle_g(x > 10^{-4}) \quad \text{“Two-scale picture”}$$

- Two classes of  $pp$  collisions

Peripheral: Most of inelastic cross section

Central: High probability for hard process



- Hard processes select central collisions

→ Talk Strikman

Underlying event very different from min. bias

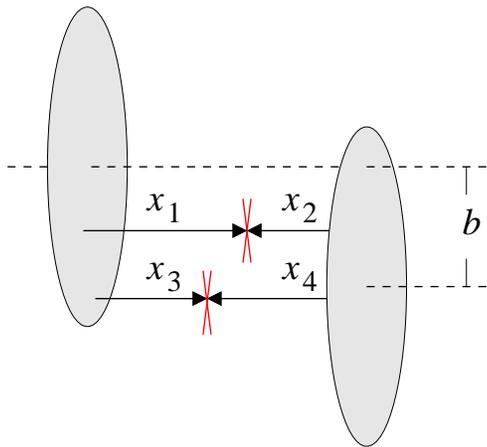
Geometric correlations:

Hard process → centrality → event chars

E.g. transverse multiplicity

New tests of dynamical mechanisms in particle production

# Transverse distributions: MPIs



- Double collision rate parametrized by  $\sigma_{\text{eff}}^{-1}$

Mean field  $\sigma_{\text{eff}} = \pi R_{13}^2$  avg distance btw collisions  
 Calculable from transverse distributions

$$\sigma_{\text{eff}}^{-1} (\text{mean field}) = \int d^2b P_{12}(b) P_{34}(b)$$

Numerically stable. Convolution becomes simple product of  $t$ -dependent gluon form factors measured in exclusive  $ep/\gamma p$

Mean field as reference prediction

- Observed enhancement

CDF/D0 3jet +  $\gamma$  rate two times larger than mean field with  $\langle \rho^2 \rangle (x \sim 0.1)$

LHC results → Talks at this meeting

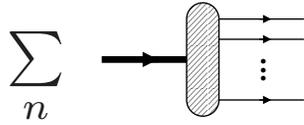
Dynamical explanation? Substantial correlations?

$$\frac{\sigma(12; 34)}{\sigma(12)\sigma(34)} = \frac{1}{\sigma_{\text{eff}}} \times \frac{f(x_1, x_3)f(x_2, x_4)}{f(x_1)f(x_2)f(x_3)f(x_4)}$$

Transverse spatial distribution determines basic mean-field expectation of MPI rate

# Quantum fluctuations: Parton densities

- Nucleon quantum many-body system

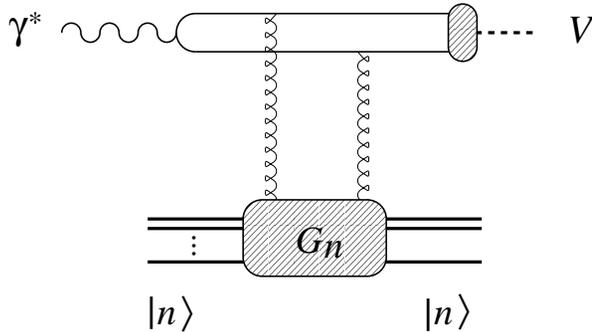


Partonic wave function has components with different particle number, transverse size, etc.

High-energy processes intercept instantaneous configurations "interactions frozen"

Fluctuations well-known in soft interactions:  
Cross section distribution  $P(\sigma)$ , diffractive dissociation

Fluctuations of parton density and transverse size?  
Frankfurt, Strikman, Treleani, CW, PRL **101**:202003, 2008  
Fundamental interest, affects MPI

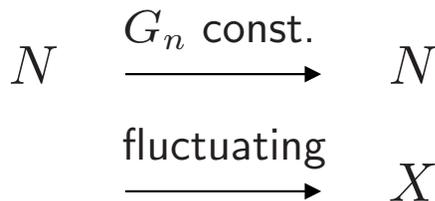


- Fluctuations of gluon density

Hard diffractive processes at small  $x$

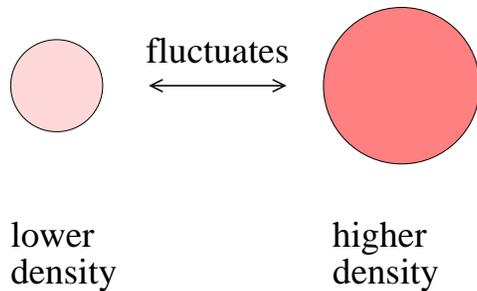
Amplitude diagonal in partonic states  $|n\rangle$ ,  
proportional to configurations's gluon density  $G_n$

Fluctuations of  $G_n$  lead to dissociation  
cf. soft diffraction: Good, Walker 60, Miettinen, Pumplin 78



$$\omega_g \equiv \frac{\langle G^2 \rangle - \langle G \rangle^2}{\langle G \rangle^2} = \frac{d\sigma/dt (\gamma^* N \rightarrow V X)}{d\sigma/dt (\gamma^* N \rightarrow V N)} \Big|_{t=0}$$

# Quantum fluctuations: Sizes and MPI



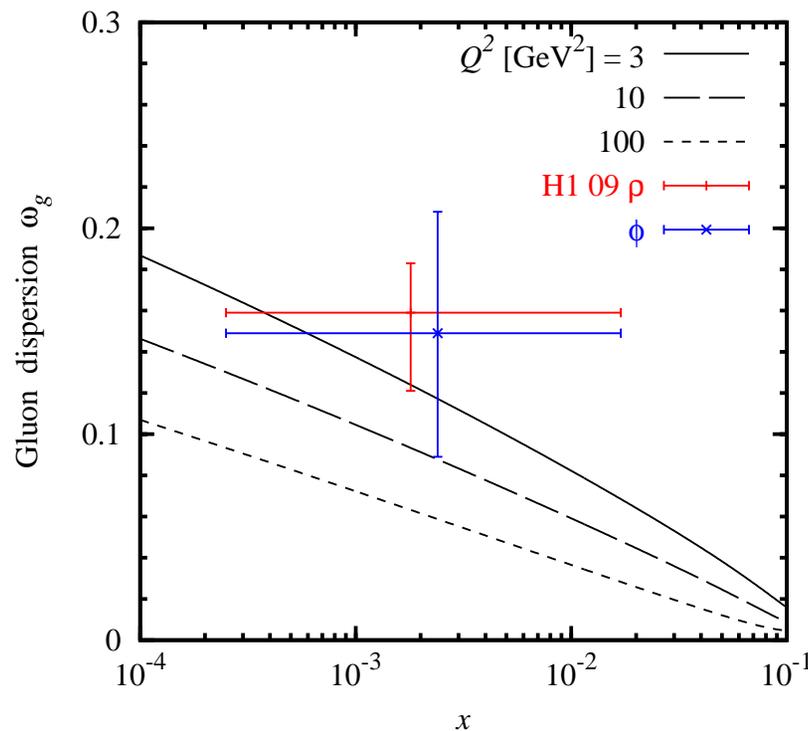
- Scaling model Close et al. 83: EMC effect

Fluctuations of nucleon size change effective scale of non-perturbative gluon density  
 $\mu^2(\text{gluon}) \propto R^{-2}$

Size distribution from soft cross section fluctuations  $\omega_\sigma \sim 0.25$  at  $\sqrt{s} = 20 \text{ GeV}$

Gluon density fluctuations change with  $x, Q^2$   
 DGLAP evolution

Consistent with HERA data  
 Large uncertainties



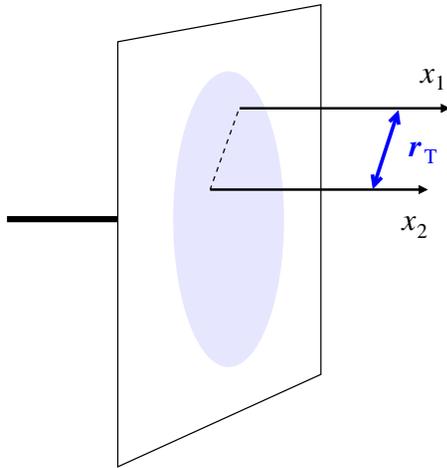
- Fluctuations in MPI

Small effect of gluon density fluctuations  
 $\omega_g < 0.1$  at Tevatron

Moderate enhancement from size fluctuations  
 $\sigma_{\text{eff}}(\text{fluct}) \approx (1 - \omega_\sigma/2) \sigma_{\text{eff}}(\text{mean field})$

Fluctuations cause moderate enhancement of MPI,  $\sim 10\text{-}15\%$  at Tevatron

# Parton correlations: QCD vacuum structure



- Parton correlations in nucleon

How is the probability to find a parton influenced by having other parton nearby?

Fundamental property of many-body system: Condensed matter, nuclei

## Multiparton distributions

Blok, Dokshitzer, Frankfurt, Strikman 10; Diehl, Ostermeier, Schafer 11  
Subtleties: UV divergences, renormalization, mixing with higher-twist ops

$$\langle N | O_{\text{tw}2}(x_1, \mathbf{r}_{1T}) O_{\text{tw}2}(x_2, \mathbf{r}_{2T}) | N \rangle_{\mathbf{r}_{1T} - \mathbf{r}_{2T} = \mathbf{r}_T}$$

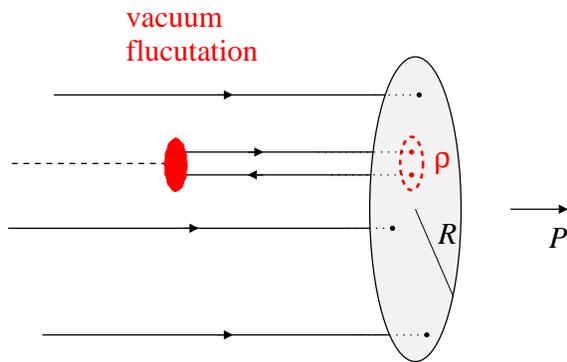
- Non-perturbative QCD vacuum

Short-distance scale  $\rho \sim 0.2-0.3$  fm  
from dynamical chiral symmetry breaking

Shuryak 82; Diakonov, Petrov 84. Size of  $q\bar{q}$  pairs in vacuum condensate, measured in Lattice QCD. Euclidean  $\rightarrow$  Minkowski?

Parton short-range correlations: Sea quarks in correlated pairs + nonperturbative gluon field

Schweitzer, Strikman, CW, arXiv:1210.1267



- Enhancement of MPI

Non-pert. correlations could account for Tevatron results

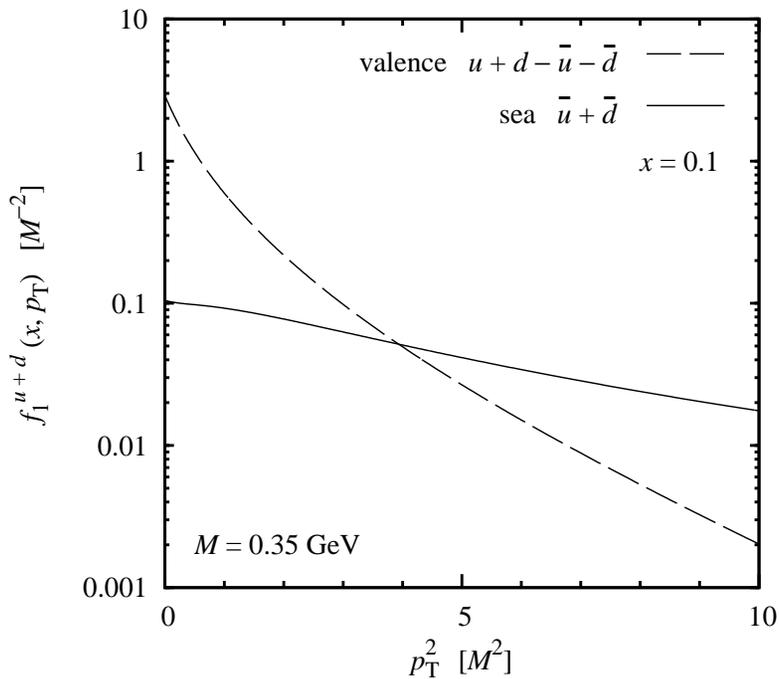
Frankfurt, Strikman, CW04

Primordial vs. DGLAP-induced correlations?

Challenge to separate!  $\rightarrow$  Discussion



# Parton correlations: Dynamical model



- Model of nonperturbative correlations  
Schweitzer, Strikman, CW 12

Chiral constituent quarks as effective degrees of freedom at momenta  $|p^2| < \rho^{-2}$   
Dynamical mass  $M \sim 0.3\text{--}0.4$  GeV. Diakonov, Eides 83

Large- $N_c$  limit: Semiclassical approximation  
Chiral quark-soliton model. Diakonov, Petrov, Polybitsa 88

Sea quark transverse momenta up to  $p_T \sim \rho^{-1}$   
Qualitatively different from valence quarks  $p_T \sim R^{-1}$

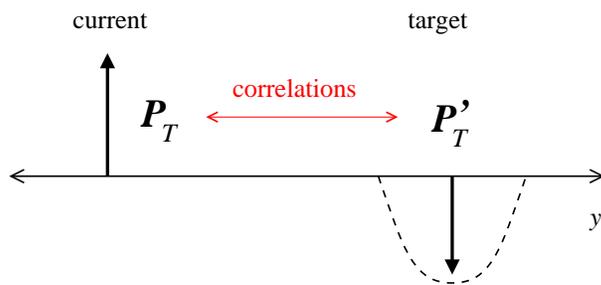
Correlated  $q\bar{q}$  pairs in nucleon wave function:  
Spin/flavor structure,  $\sigma/\pi$  quantum numbers

- Signals in deep-inelastic lepton scattering

$P_T$  distributions in semi-inclusive DIS  
incl. spin asymmetries, particle correlations. JLab12, COMPASS

Particle correlations between current and target fragmentation regions  
Moderate energies  $\bar{W} \sim \text{few GeV}$  avoid DGLAP radiation.  
COMPASS, EIC

Exclusive meson production at large  $x$   
Knockout of correlated  $q\bar{q}$  pair. JLab12



Quark correlations from DIS . . . new field!

# Summary

- Partonic wave function encodes non-perturbative QCD

Dynamical system, not MC generator!

Much information from  $ep/\gamma p$  and non-perturbative theoretical approaches

- Nucleon properties determining MPI rates

Transverse distributions	reasonably well known, more data expected COMPASS, JLab12, EIC	mean-field expectation
Density/size fluctuations	rough estimates	moderate enhancement $\sim 20\%$ at Tevatron
Parton correlations	theoretical models, future tests in $ep$	possibly substantial enhancement, perturbative $\leftrightarrow$ non-perturbative?

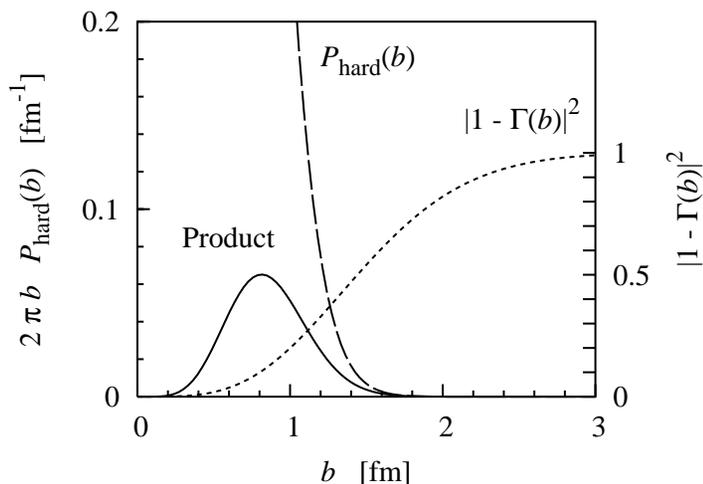
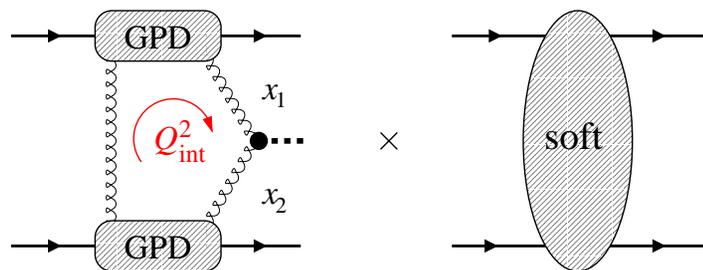
- Great potential interest in nucleon structure community

Connections to exclusive processes (GPDs), semi-inclusive DIS (TMDs), higher twist

Parton correlations “next step” after one-body densities

Supplementary material

# Diffraction: Rapidity gap survival



$$S^2 = \int d^2b P_{\text{hard}}(b) |1 - \Gamma(b)|^2$$

- Central exclusive diffraction → Talk Martin

Heavy system produced in hard two-gluon exchange

Concurrent soft spectator interactions must not produce particles

Khoze, Martin, Ryskin 97+

- Survival probability  $S^2$

Mean-field  $S^2$  calculable from transverse gluon distn and  $pp$  elastic amplitude

Model-independent, pure transverse geometry FHSW06

Basic suppression by factor  $\sim 30 - 40$  from elimination of scattering at small  $b$   $\sqrt{s} = 14$  TeV

Additional suppression by factor  $> 2 - 3$  from dynamical correlations, black-disk regime

Requires detailed modeling

- Diffraction pattern in  $p_{T1}, p_{T2}$

Experimental tests: CMS/TOTEM or LHC420

STAR pp2pp @  $\sqrt{s} = 500$  GeV