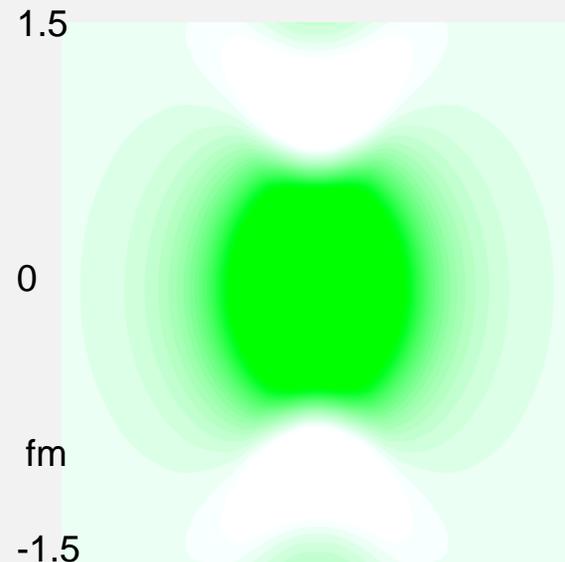


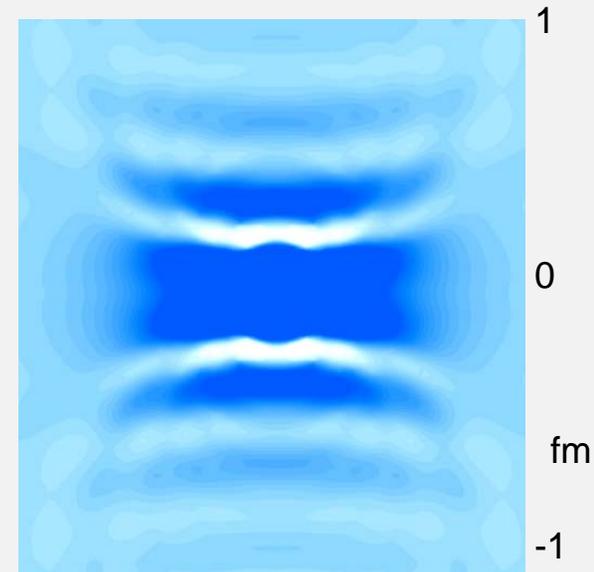
Generalized Parton Distributions and the Structure of the Nucleon

$x=0.4$



Volker D. Burkert
Jefferson Lab

$x=0.9$



April Meeting

Fundamental questions in hadron physics?

1950-1960: Does the proton have finite size and structure?

- Elastic scattering
 - ⇒ the proton is not a point-like particle
 - charge and current distribution in the proton, F_1/F_2

1960-1990: What is the internal structure of the proton?

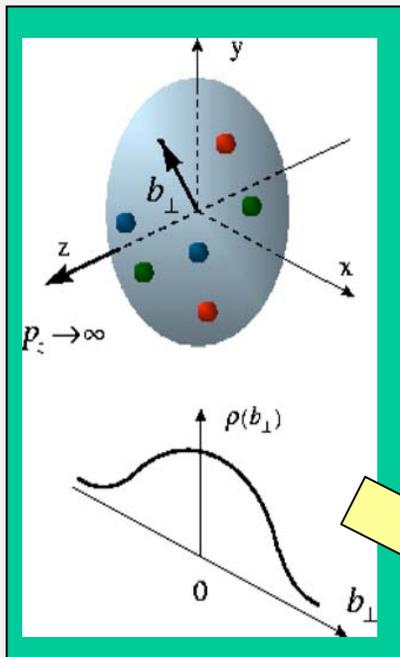
- Deep inelastic scattering
 - ⇒ discover quarks
 - quark momentum and spin distributions $q(x)$, $\Delta q(x)$

Today: How are these representations of the proton, charge/current distributions and quark momentum/spin distributions fundamentally connected?

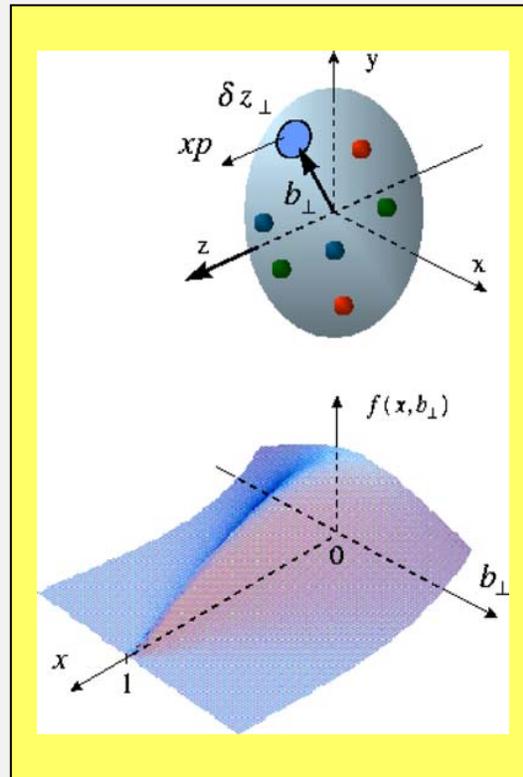
Beyond charge and quark distributions - Generalized Parton Distributions (GPDs)

X. Ji, D. Mueller, A. Radyushkin (1994-1997), ...
M. Burkardt, A. Belitsky (2000) ...

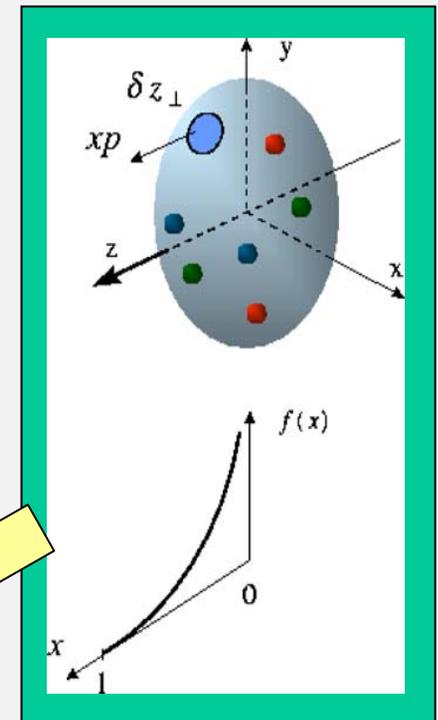
Infinite momentum frame



Transverse charge &
current densities



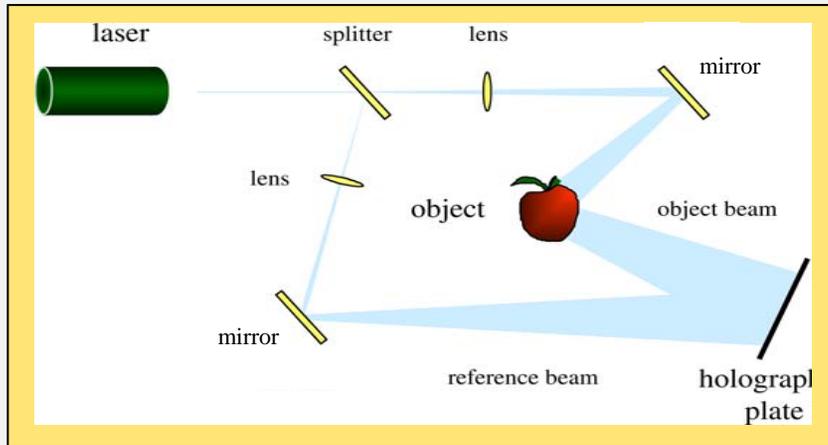
Correlated distributions in
transverse space - GPDs



Quark longitudinal
momentum & helicity
distributions

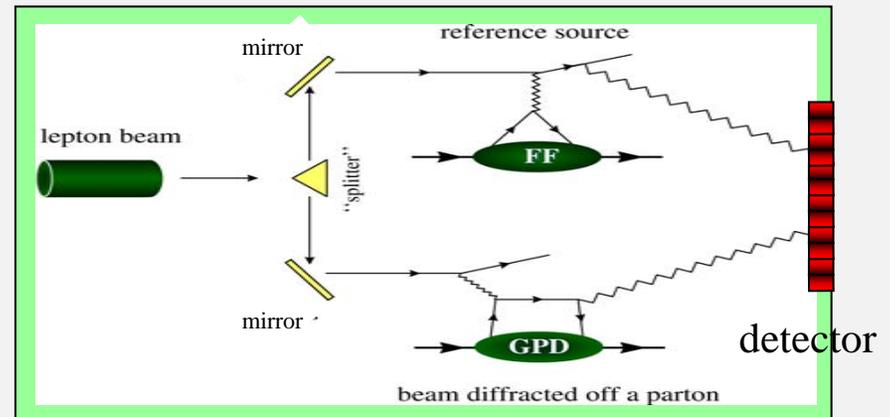
From Holography to Tomography

A. Belitsky, B. Mueller, NPA711 (2002) 118



An Apple

A Proton

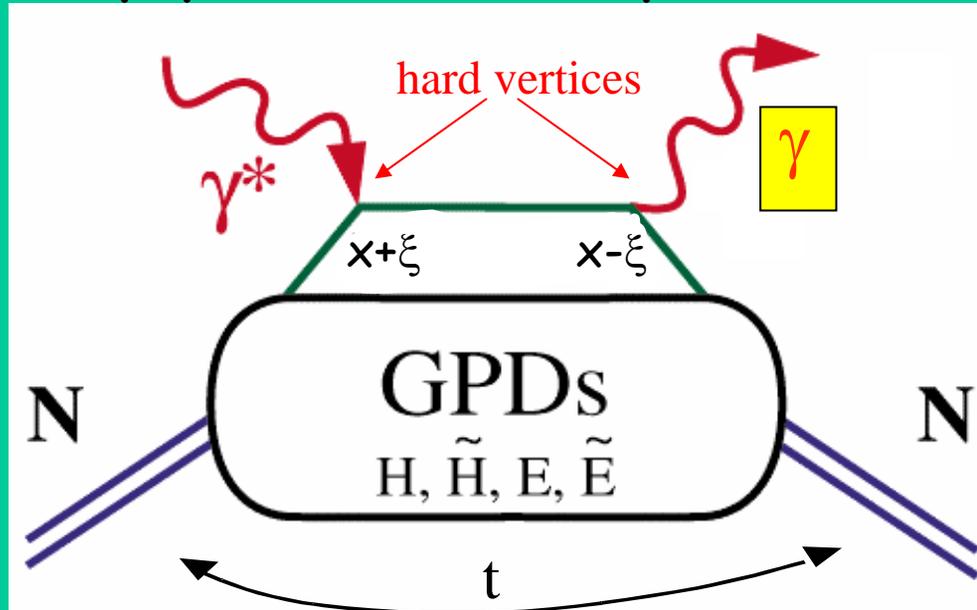


By varying the energy and momentum transfer to the proton we probe its interior and generate tomographic images of the proton (“femto tomography”).

Deeply Virtual Exclusive Processes & GPDs

"handbag" mechanism

Deeply Virtual Compton Scattering (DVCS)



x - longitudinal quark momentum fraction

2ξ - longitudinal momentum transfer

$\sqrt{-t}$ - Fourier conjugate to transverse impact parameter

$H(x, \xi, t), E(x, \xi, t), \dots$

$$\xi = \frac{x_B}{2-x_B}$$

Link to DIS and Elastic Form Factors

DIS at $\xi=t=0$

$$H(x,0,0) = q(x), \quad -\bar{q}(-x)$$

$$\tilde{H}(x,0,0) = \Delta q(x), \quad \Delta \bar{q}(-x)$$

Form factors (sum rules)

$$\int_{-1}^1 dx [H(x, \xi, t)] = F_1(t) \text{ Dirac f.f.}$$

$$\int_{-1}^1 dx [E(x, \xi, t)] = F_2(t) \text{ Pauli f.f.}$$

$$\int_{-1}^1 dx \tilde{H}(x, \xi, t) = G_{A,q}(t), \quad \int_{-1}^1 dx \tilde{E}(x, \xi, t) = G_{P,q}(t)$$



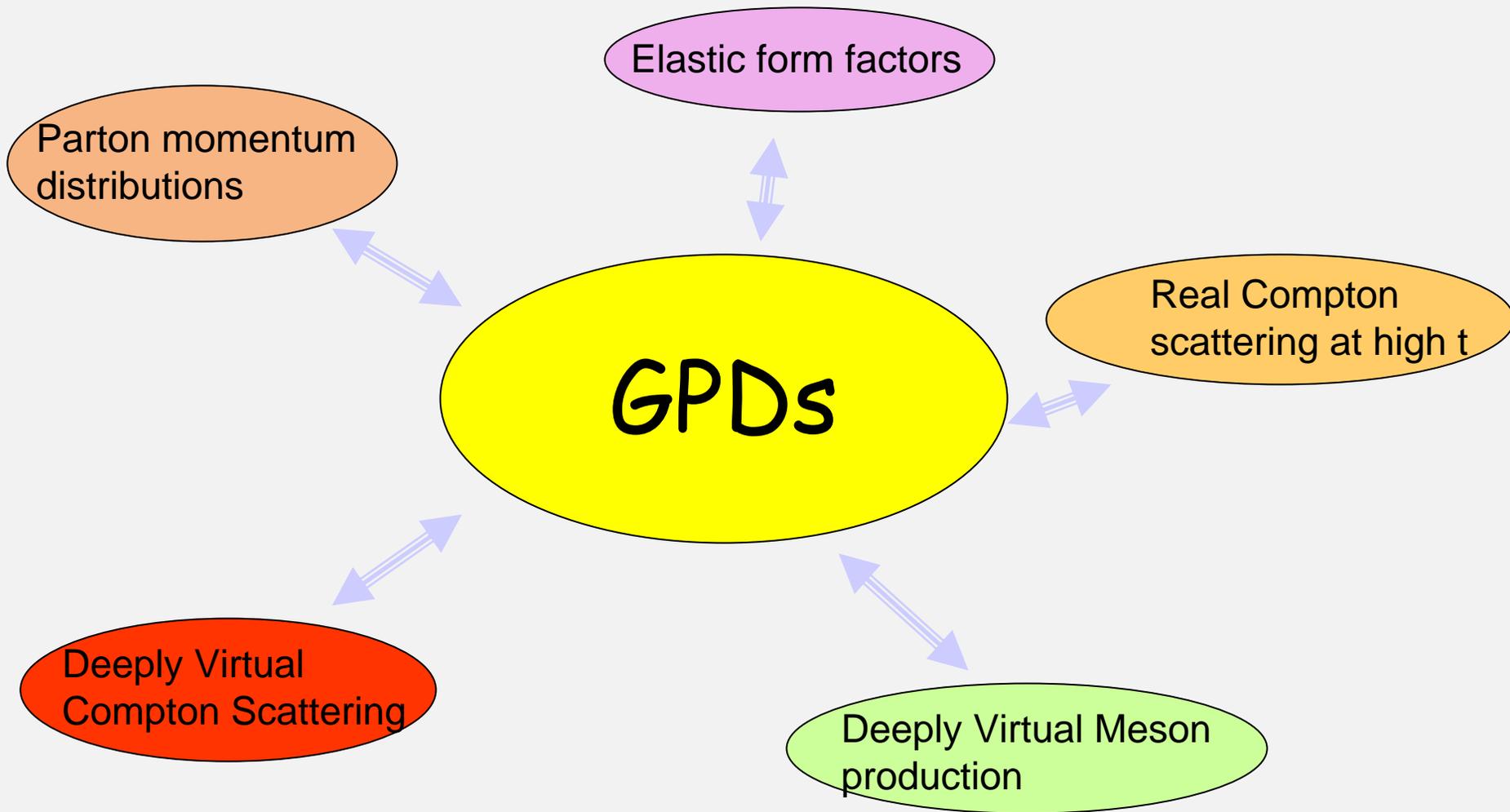
$H, E, \tilde{H}, \tilde{E}(x, \xi, t)$



Quark angular momentum (Ji's sum rule)

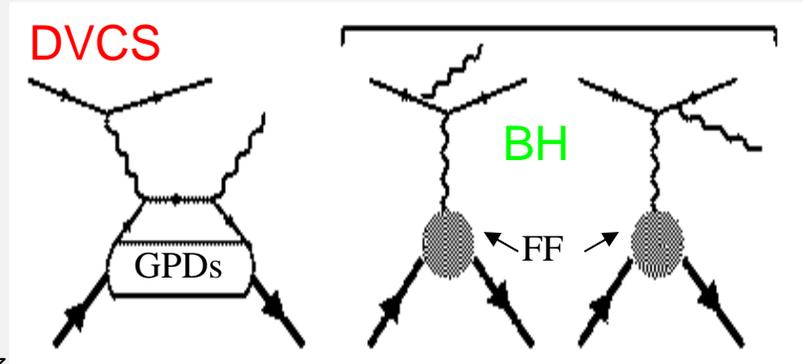
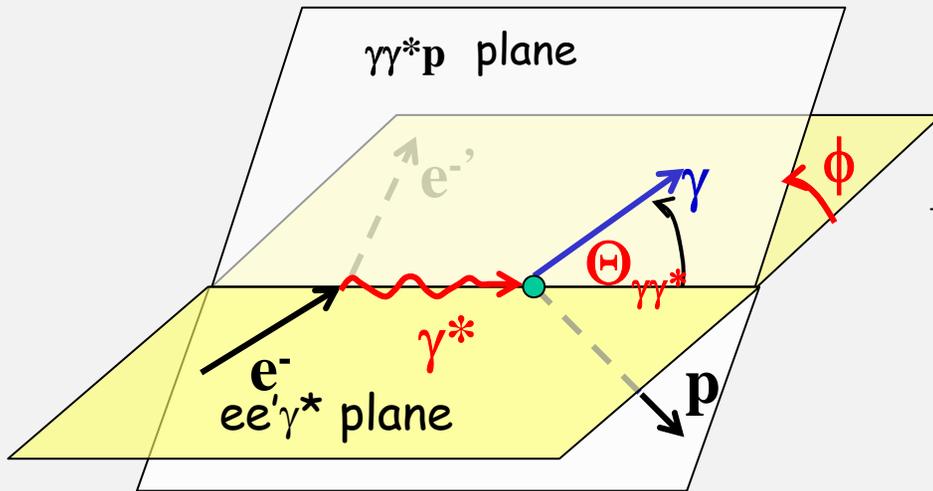
$$J^q = \frac{1}{2} - J^G = \frac{1}{2} \int_{-1}^1 x dx [H^q(x, \xi, 0) + E^q(x, \xi, 0)]$$

A Unified Description of Hadron Structure



Accessing GPDs through DVCS

$$\vec{e}p \rightarrow ep\gamma$$



$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} \sim |\text{DVCS} + \text{BH}|^2$$

$$\sim |\text{DVCS}|^2 + |\text{BH}|^2 + \text{BH}^* \text{Im}(\text{DVCS})$$

BH: given by elastic form factors
DVCS: determined by GPDs

$$\Delta\sigma_{LU} \sim \text{BH} \text{Im}(\text{DVCS}) \sin\phi + \text{higher twist.}$$

Separating **GPDs** through polarization

$$\mathbf{A} = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma}{2\sigma}$$

$$\xi = x_B / (2 - x_B)$$

$$k = t / 4M^2$$

Polarized beam, unpolarized target:

$$\Delta\sigma_{LU} \sim \sin\phi \{ F_1 \mathbf{H} + \xi(F_1 + F_2) \tilde{\mathbf{H}} + kF_2 \mathbf{E} \} d\phi$$

↑ ↑
Kinematically suppressed



$\mathbf{H}, \tilde{\mathbf{H}}, \mathbf{E}$

Unpolarized beam, longitudinal target:

$$\Delta\sigma_{UL} \sim \sin\phi \{ F_1 \tilde{\mathbf{H}} + \xi(F_1 + F_2) (\mathbf{H} + \dots) \} d\phi$$



$\mathbf{H}, \tilde{\mathbf{H}}$

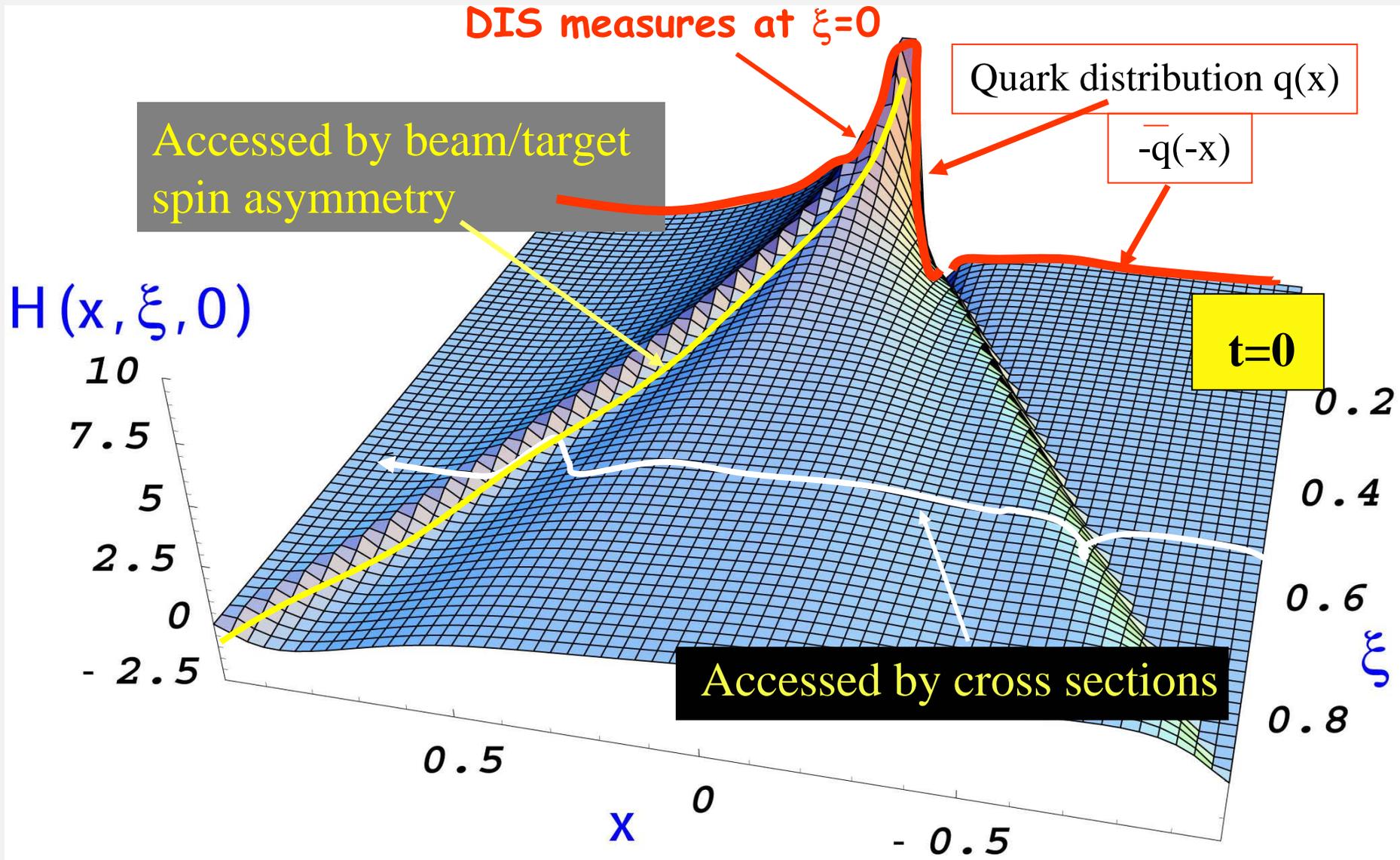
Unpolarized beam, transverse target:

$$\Delta\sigma_{UT} \sim \sin\phi \{ k(F_2 \mathbf{H} - F_1 \mathbf{E}) + \dots \} d\phi$$



\mathbf{H}, \mathbf{E}

Access $GPDs$ through x-section & asymmetries

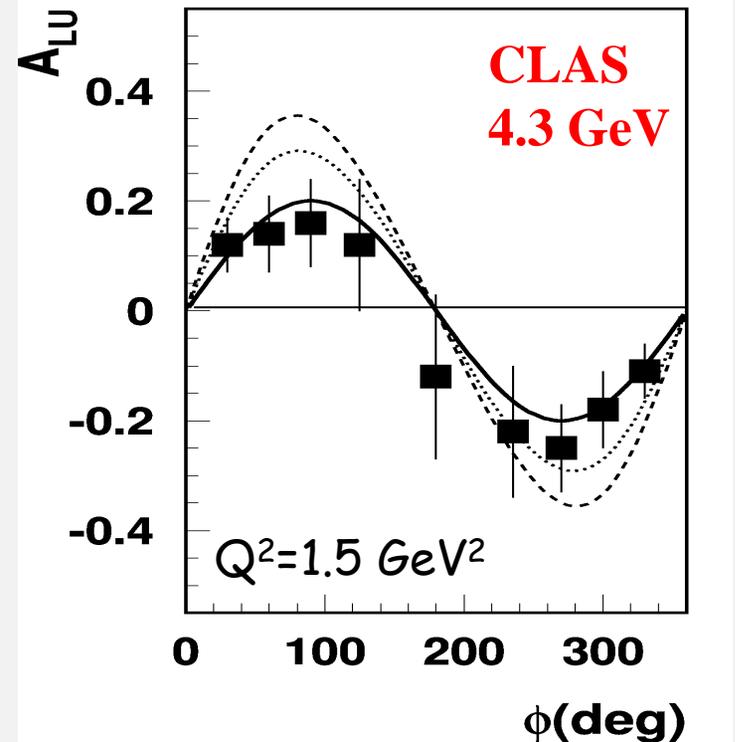
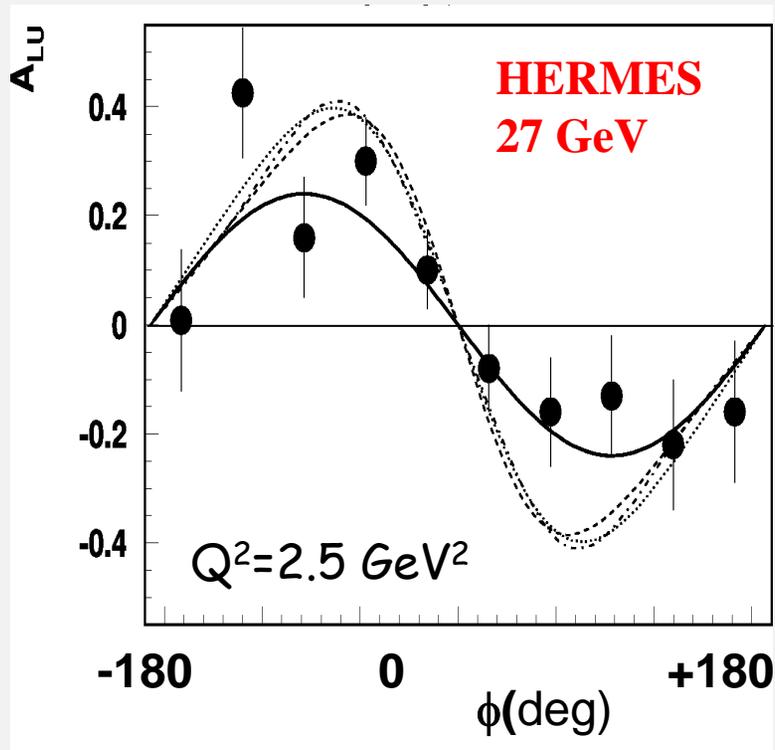


First observation of DVCS/BH beam asymmetry

$e^+p \rightarrow e^+\gamma X$

2001

$e^-p \rightarrow e^-pX$



GPD analysis of CLAS/HERMES/HERA data in LO/ NLO shows results consistent with handbag mechanism and lowest order pQCD
A. Freund, PRD 68,096006 (2003), A. Belitsky, et al. (2003)

$$A(\phi) = \alpha \sin\phi + \beta \sin 2\phi$$

$$\beta/\alpha \ll 1 \rightarrow \text{twist-3} \ll \text{twist-2}$$

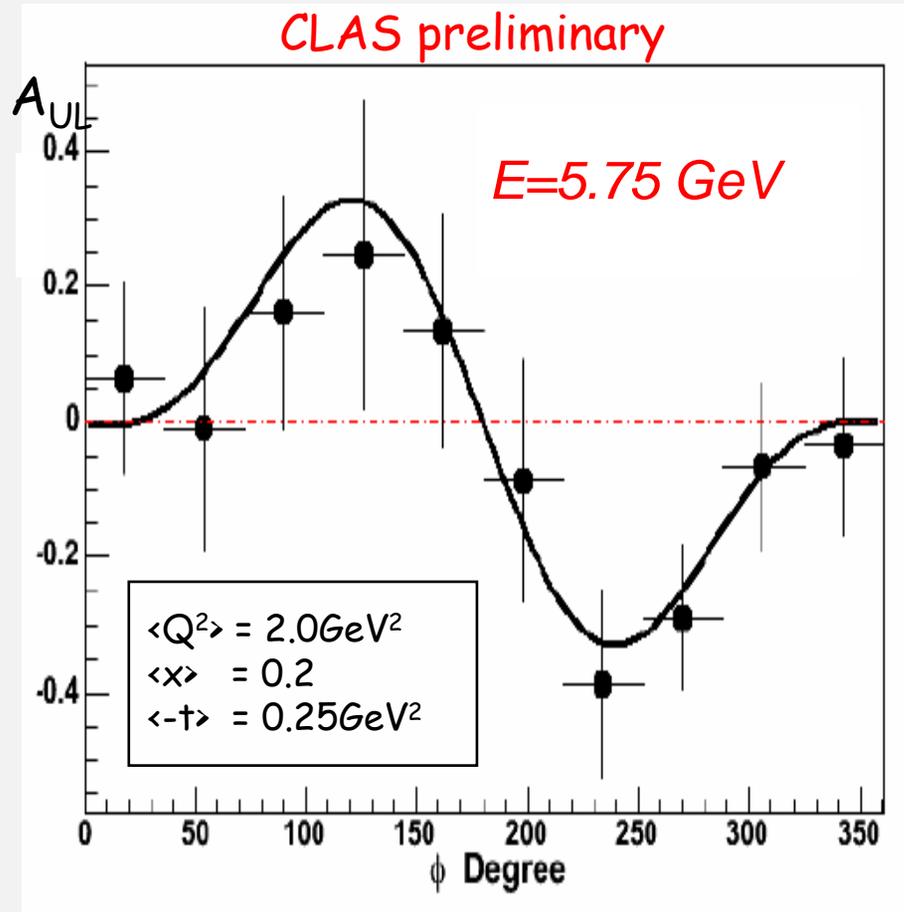
DVCS/BH target asymmetry

$$e \vec{p} \rightarrow e p \gamma$$

Longitudinally polarized target

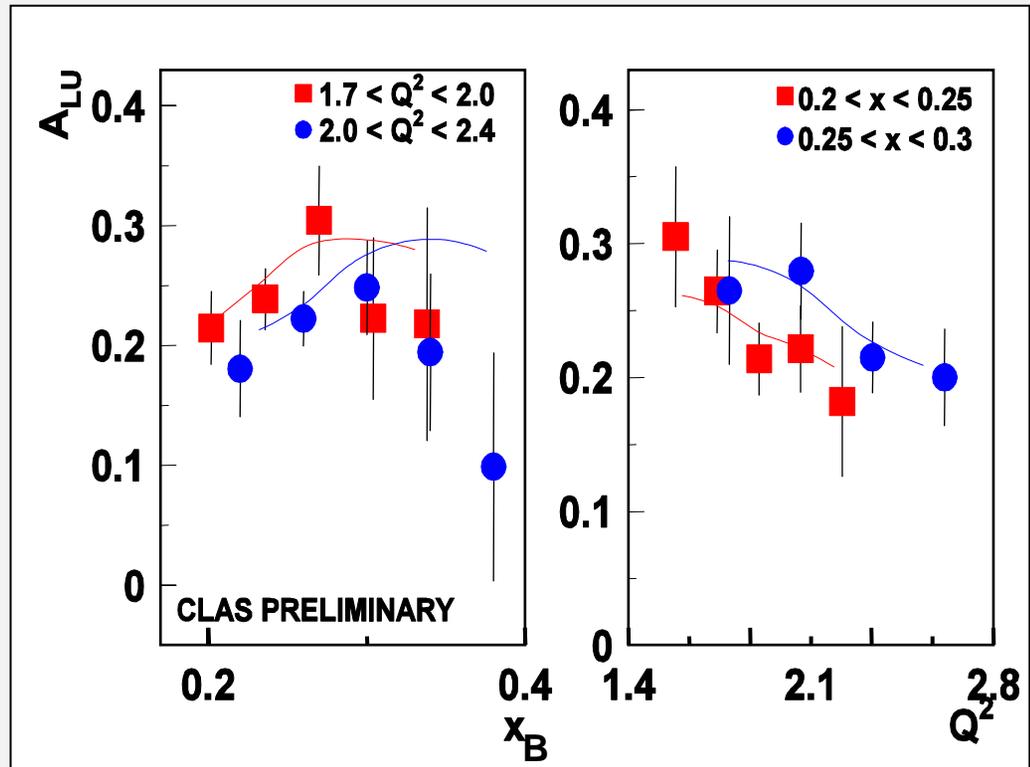
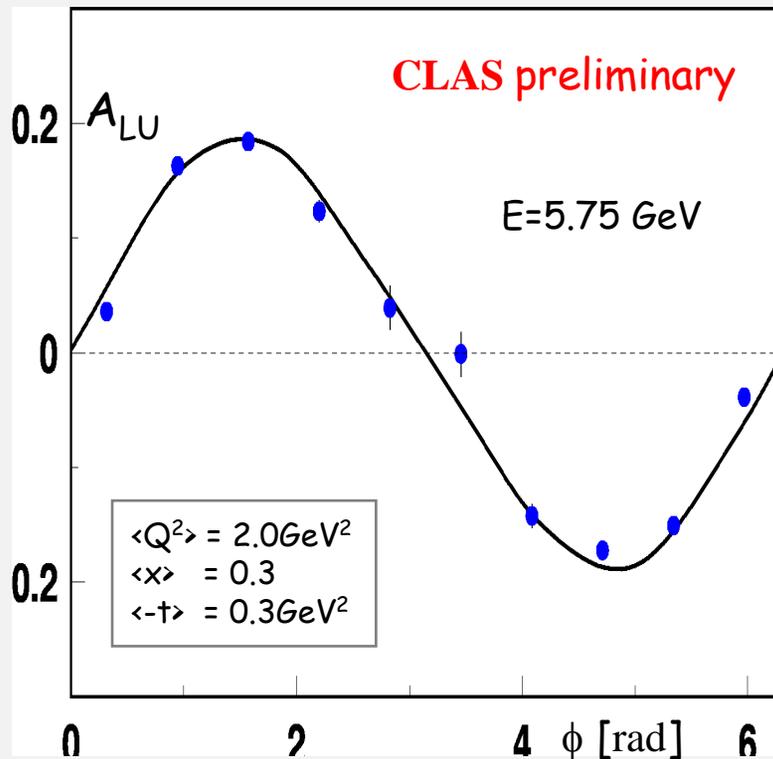
$$A_{UL} \sim \sin\phi \{ F_1 \tilde{H} + \xi (F_1 + F_2) H \dots \} d\phi$$

Asymmetry observed at about the expected magnitude. Much higher statistics, and broad kinematical coverage are needed.



HERMES data on deuterium target

First DVCS experiment with GPDs in mind



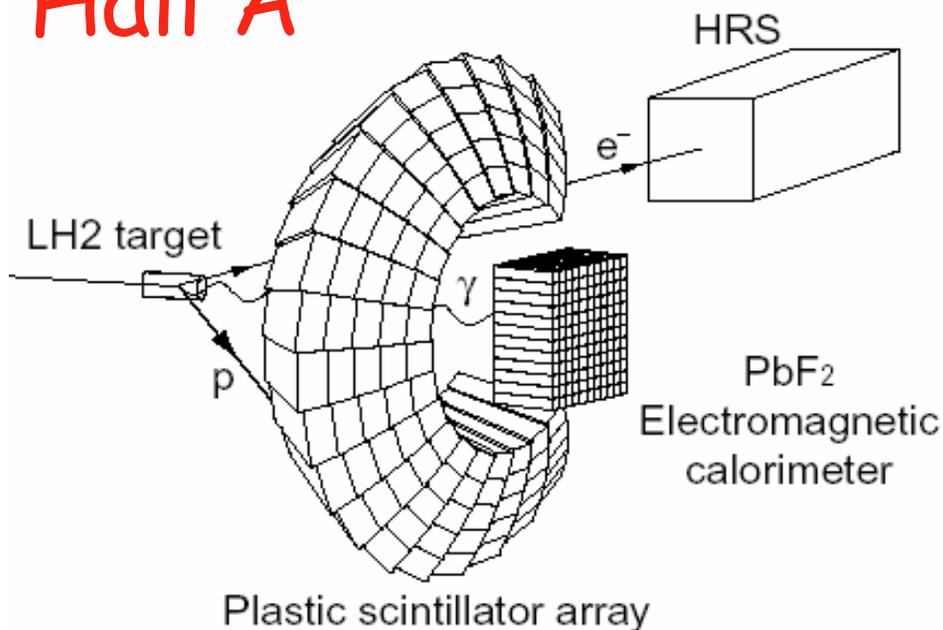
Twist-2 + twist-3: Kivel,
Polyakov, Vanderhaeghen
(2000)

Model with GPD parametrization and
quark k_T corrections describes data.

First Dedicated DVCS Experiments at JLab

- => Full reconstruction of all final state particles e , p , γ
- => High luminosity

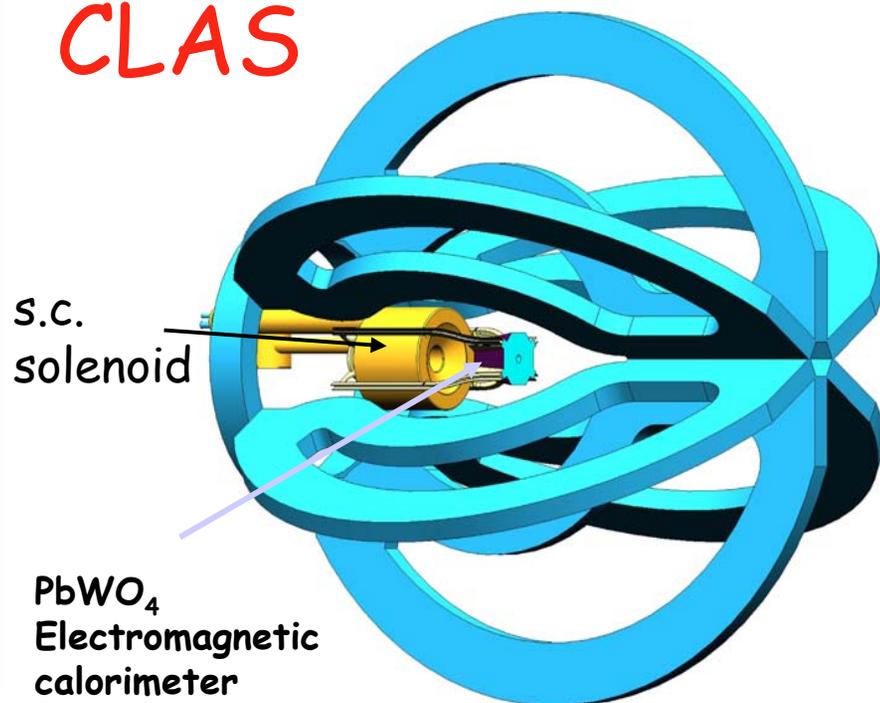
Hall A



Azimuthal and Q^2 dependence of $\text{Im}(\text{DVCS})$ at fixed ξ .
Test Bjorken scaling.

Data taking completed

CLAS



ξ , t , Q^2 - dependence of $\text{Im}(\text{DVCS})$ in wide kinematics. Constrain GPD models.

Currently taking data

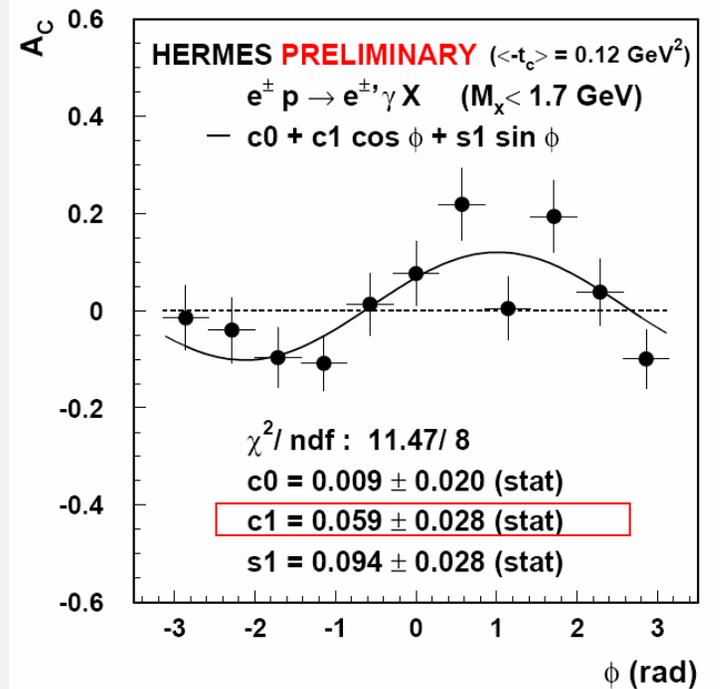
DVCS/BH Beam-Charge Asymmetry

HERMES

The e^+e^- beam asymmetry measures real part of convolution integral for GPDs.

$$H(\xi, t) = \int \frac{H^q(x, \xi, t) dx}{x - \xi}$$

$$\Delta\sigma_C \sim \cos\phi \{ F_1 H + \xi(F_1 + F_2) \tilde{H} + kF_2 E \} d\phi$$

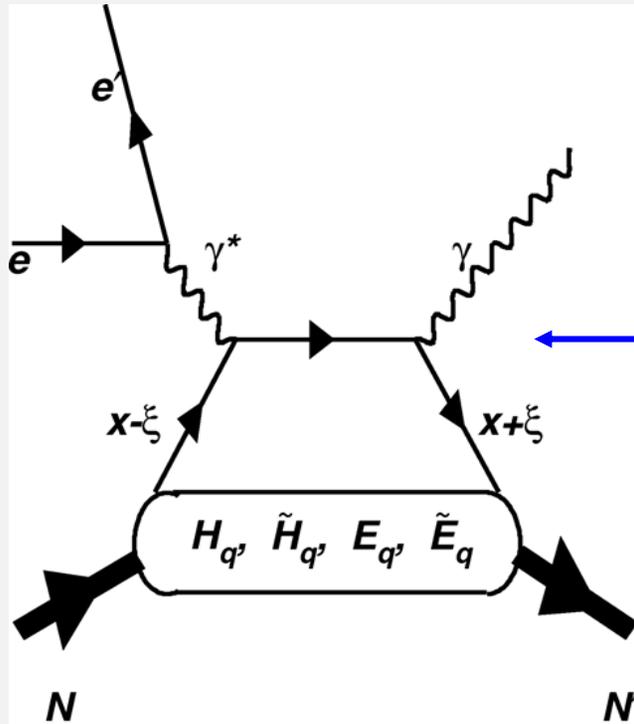


➤ Improved statistics and control of systematic expected in future run

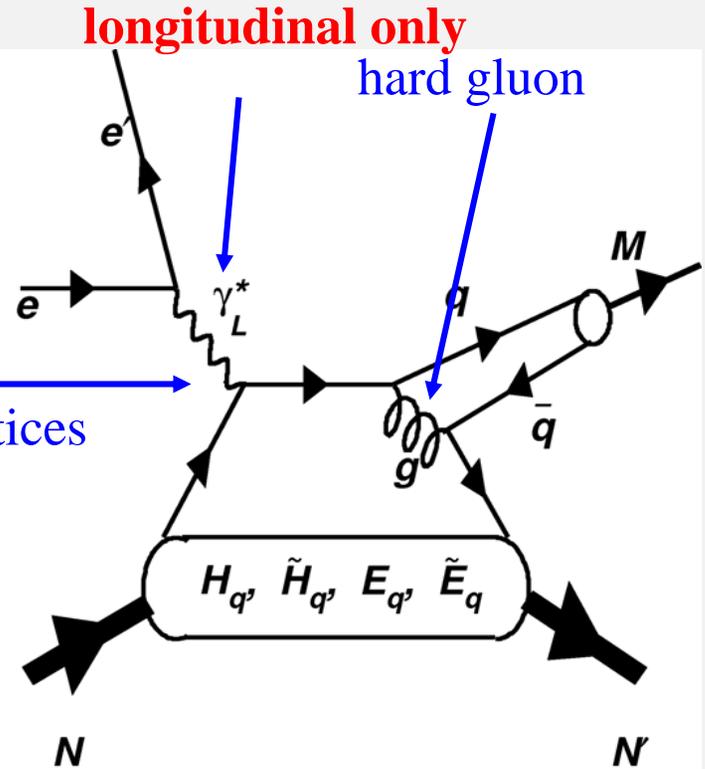
➤ Measurements proposed for COMPASS experiment at CERN in $\mu^+ - \mu^-$.

GPDs - Flavor separation

DVCS



DVMP



hard vertices

longitudinal only

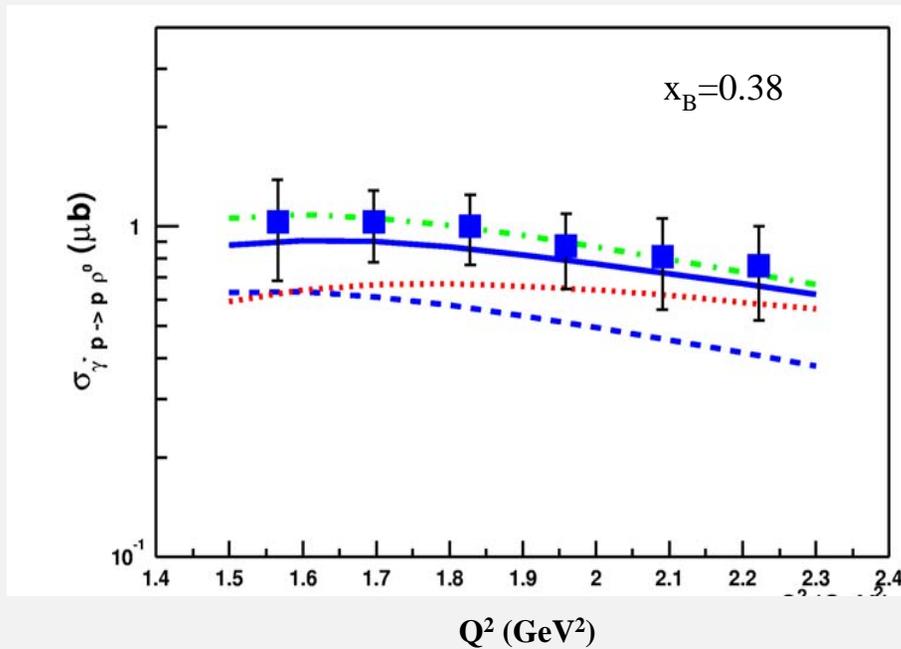
hard gluon

DVCS cannot separate u/d quark contributions.

$M = \rho/\omega$ select H, E , for u/d flavors
 $M = \pi, \eta, K$ select \tilde{H}, \tilde{E}

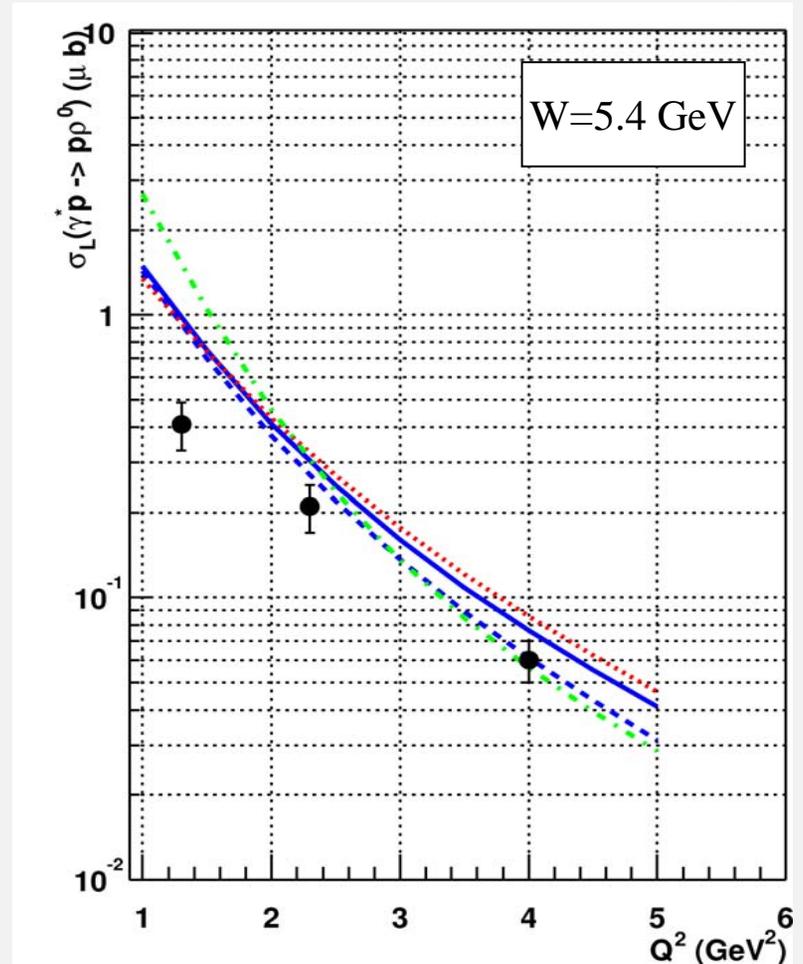
Exclusive $ep \rightarrow epp_L^0$ production

CLAS (4.3 GeV)



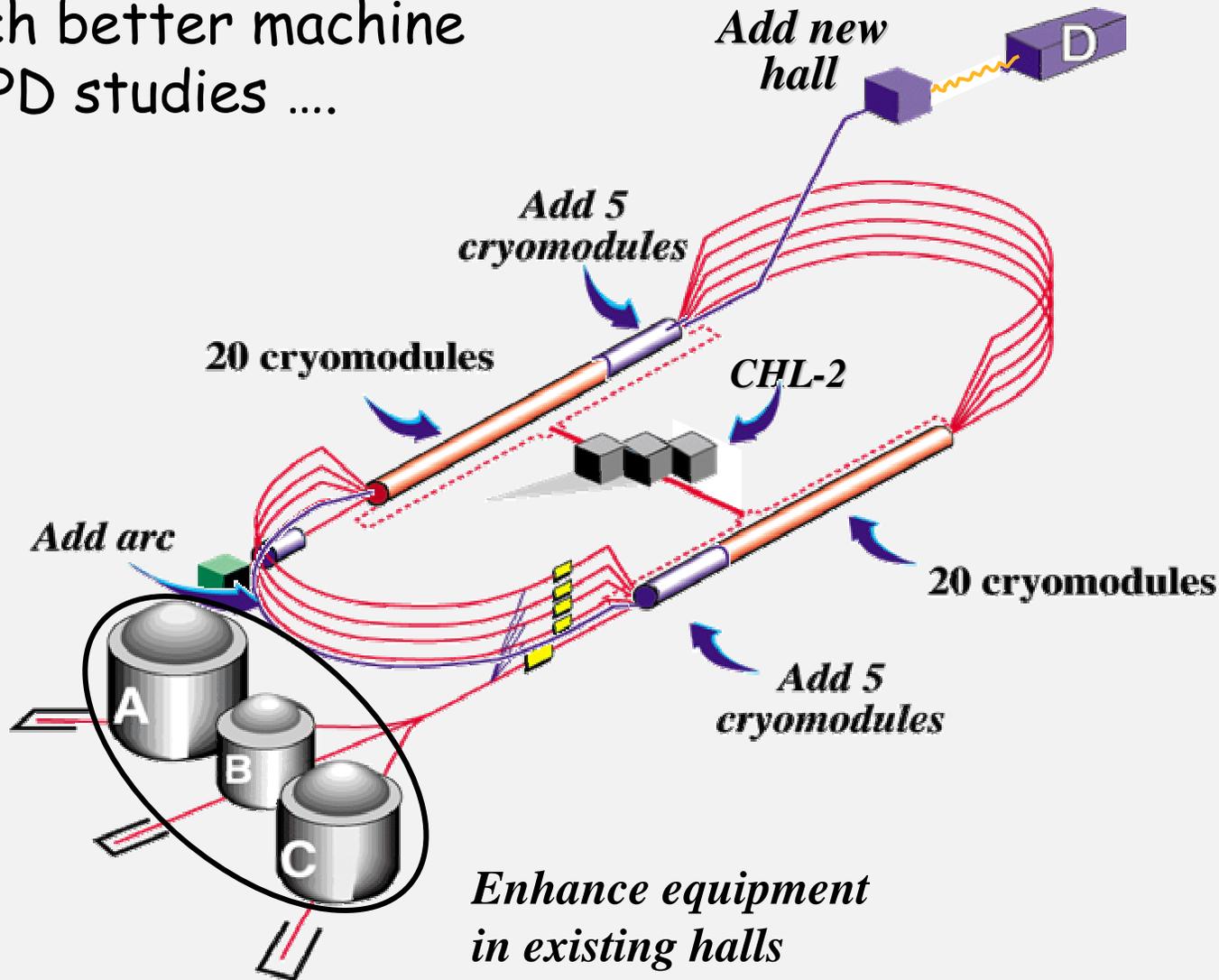
GPD formalism approximately describes CLAS and HERMES data $Q^2 > 2 \text{ GeV}^2$

HERMES (27 GeV)

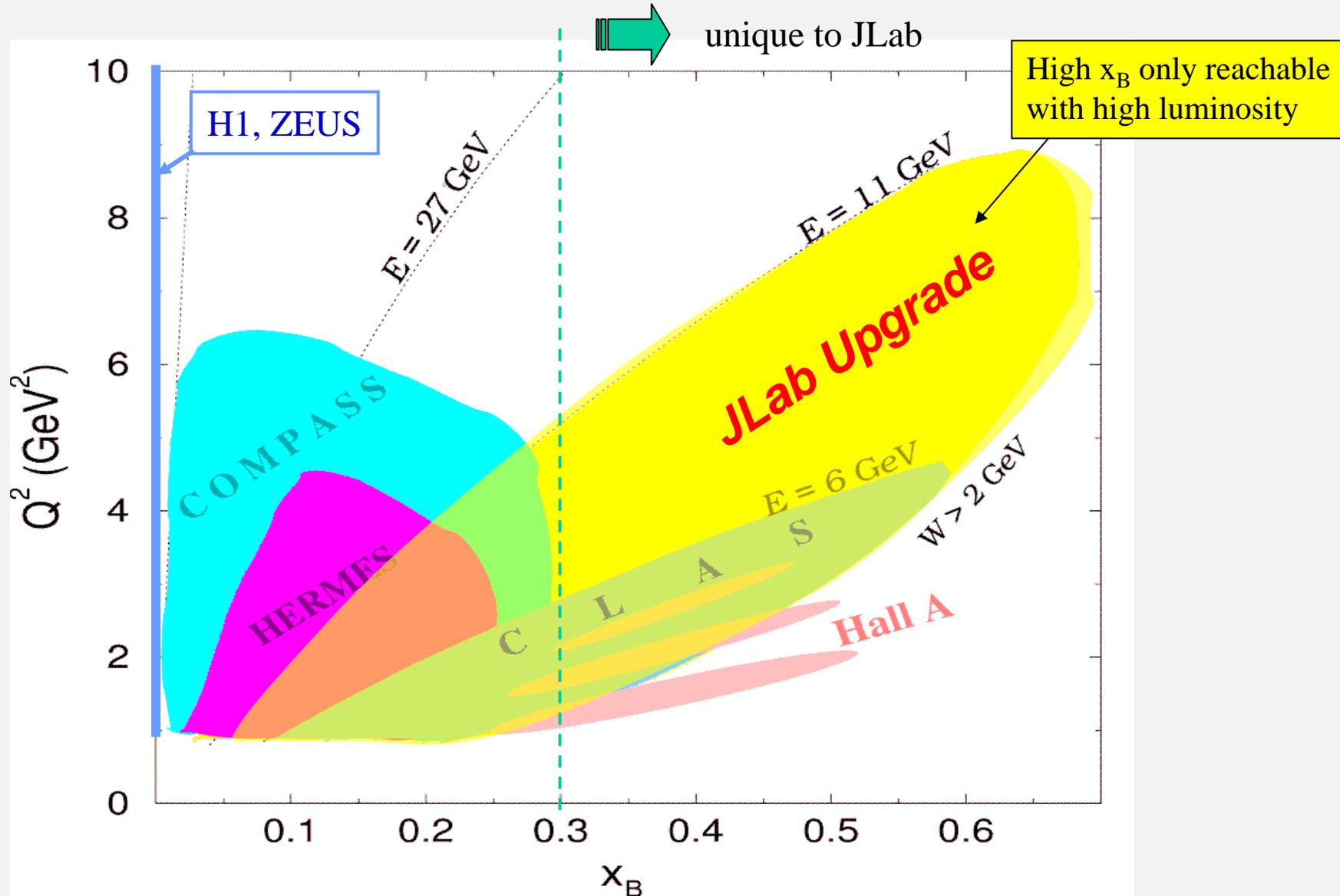


JLab Upgrade to 12 GeV Energy

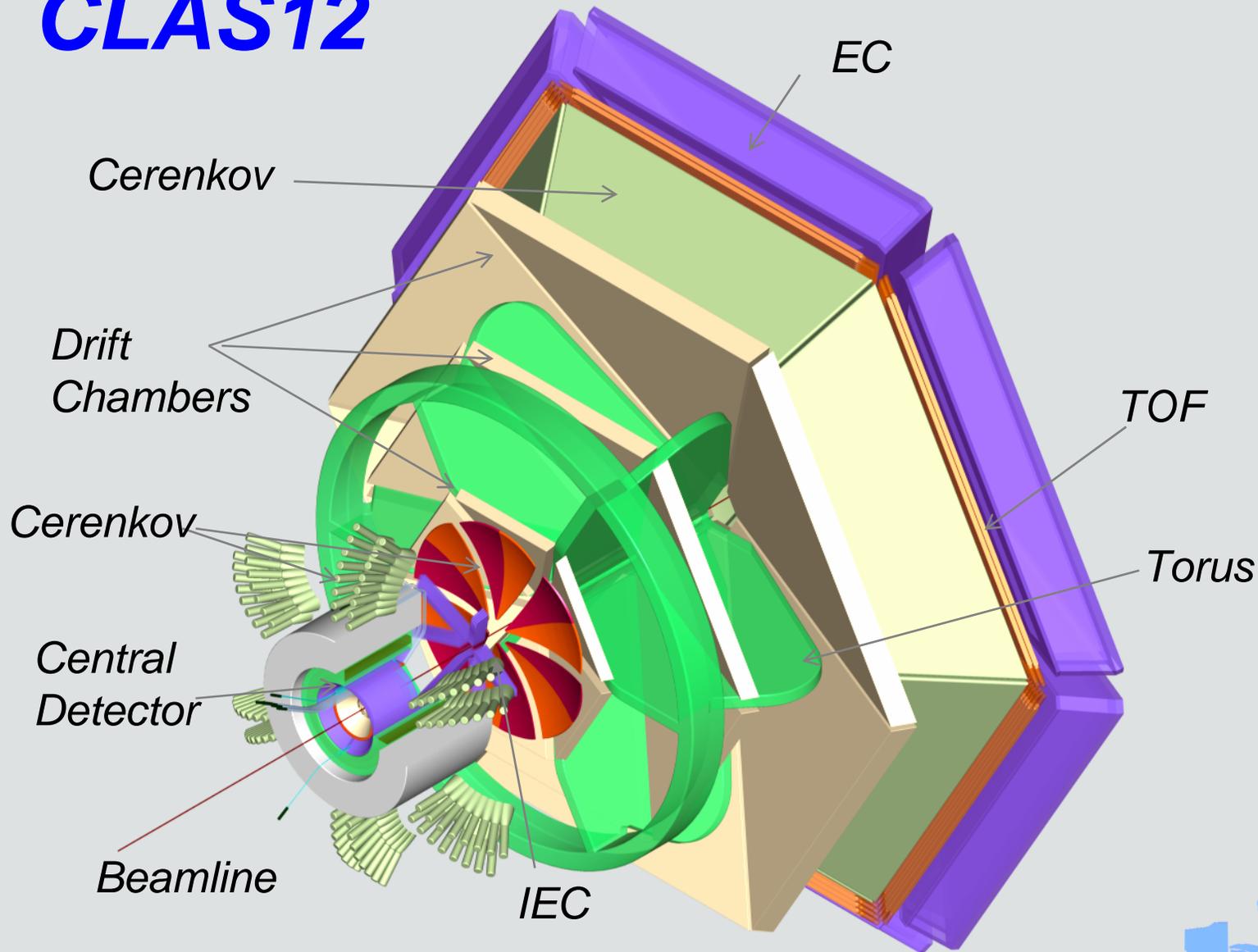
A much better machine
for GPD studies ...



Deeply Virtual Exclusive Processes - Kinematics Coverage of the 12 GeV Upgrade



CLAS12

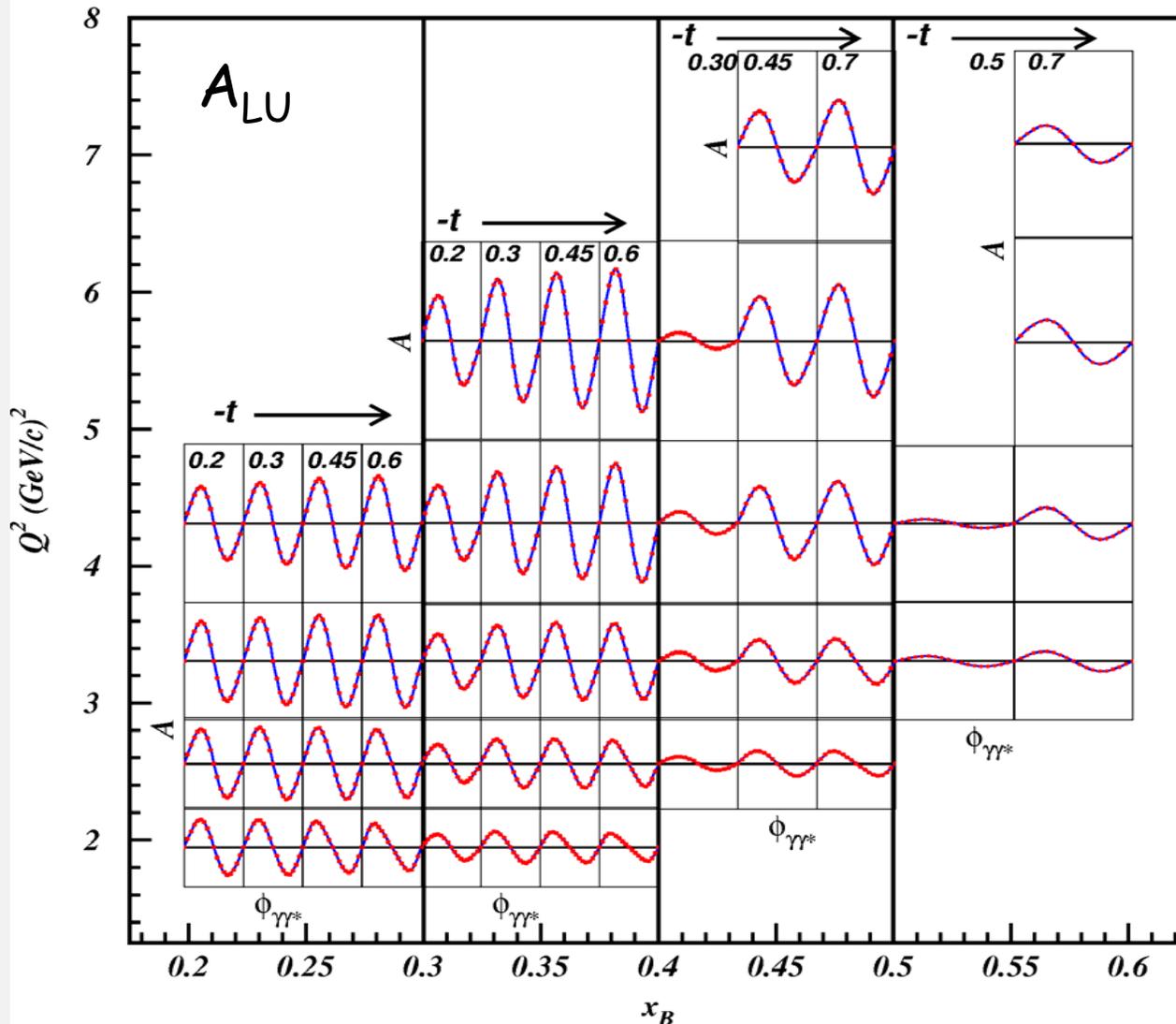


Luminosity $> 10^{35} \text{cm}^{-2} \text{s}^{-1}$



DVCS/BH- Beam Asymmetry

$$E_e = 11 \text{ GeV}$$



With large acceptance, measure large Q^2 , x_B , t ranges simultaneously.

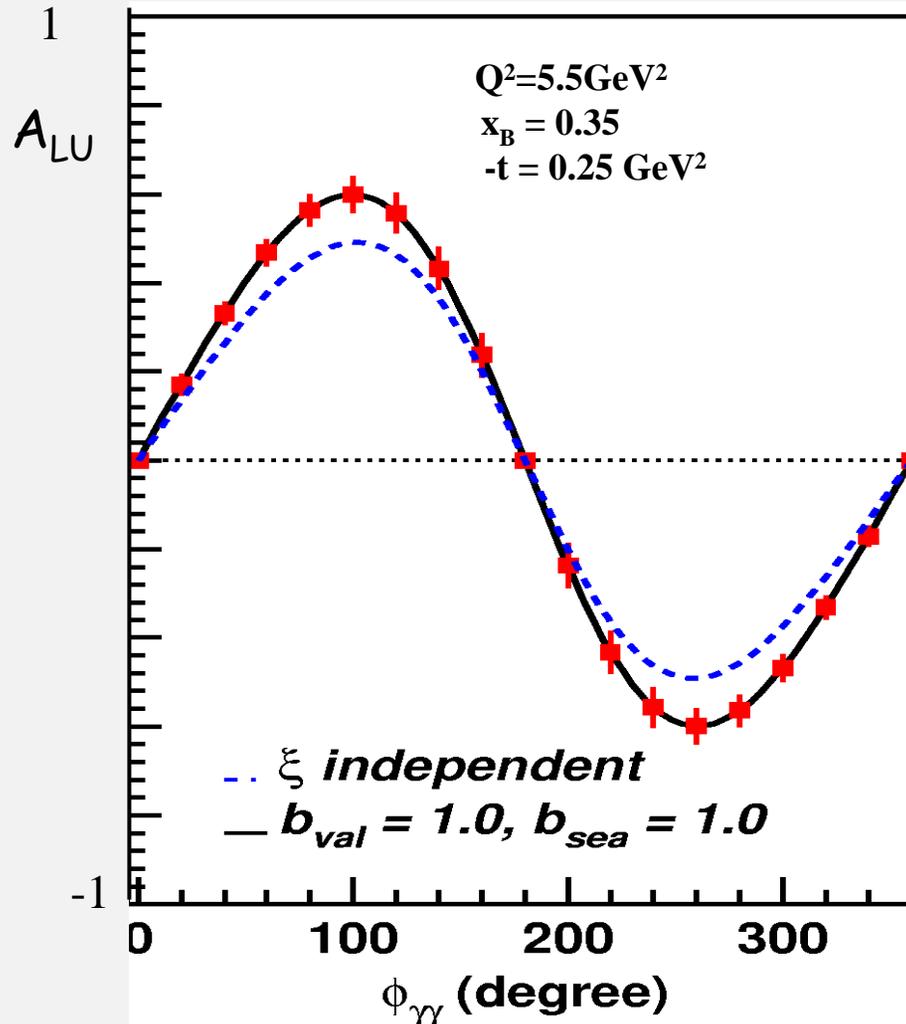
$$A(Q^2, x_B, t)$$

$$\Delta\sigma(Q^2, x_B, t)$$

$$\sigma(Q^2, x_B, t)$$

CLAS12 - DVCS/BH- Beam Asymmetry

$$E_e = 11 \text{ GeV}$$



CLAS12 - DVCS/BH Beam Asymmetry

Projected data:

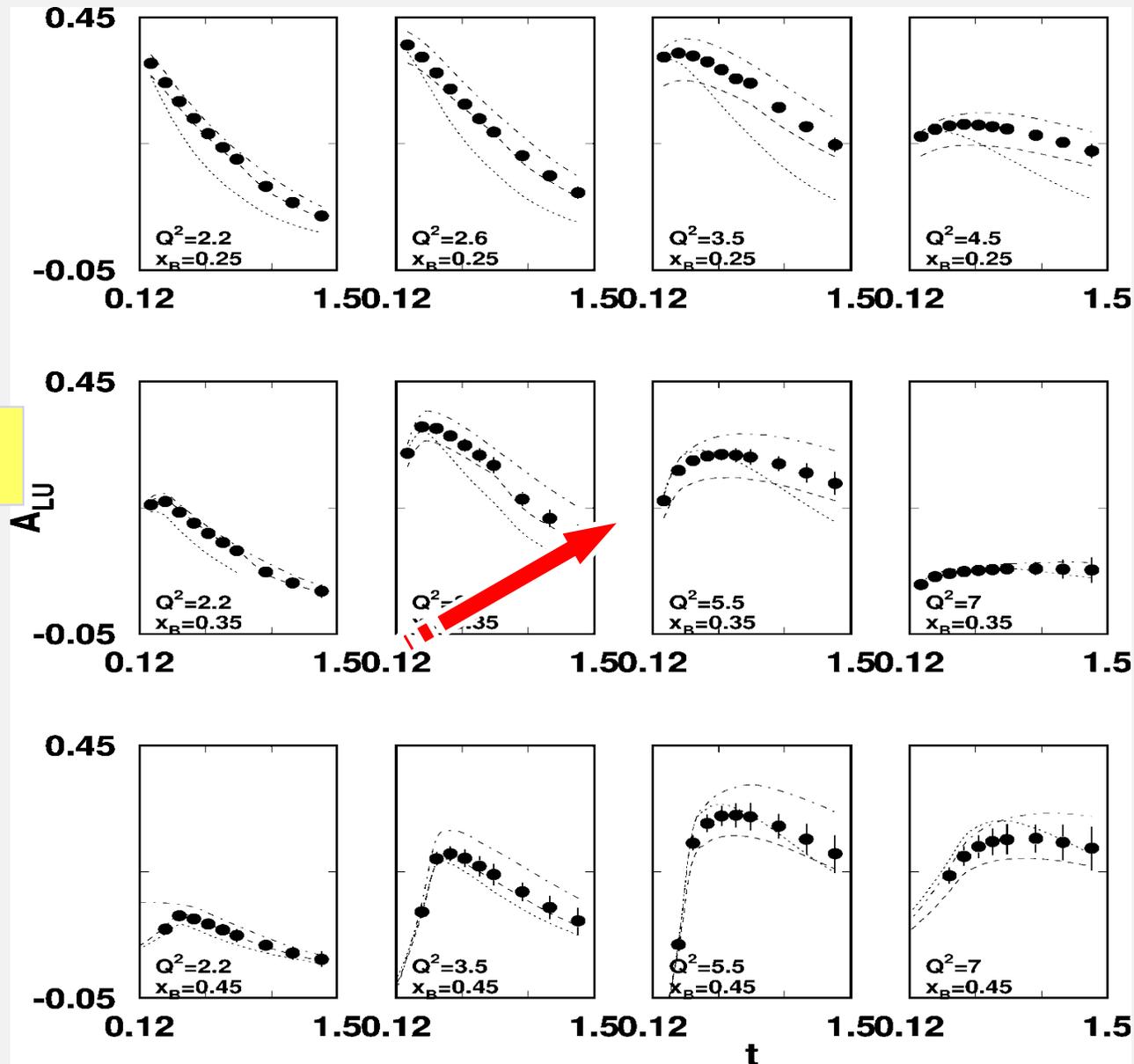
$$\vec{e} p \rightarrow e p \gamma$$

$E = 11 \text{ GeV}$

$$\Delta\sigma_{LU} \sim \sin\phi \text{Im}\{F_1 H + \dots\} d\phi$$

Integrated
luminosity $\sim 720 \text{ fb}^{-1}$

$$\begin{aligned} L &= 1 \times 10^{35} \\ T &= 2000 \text{ hrs} \\ \Delta Q^2 &= 1 \text{ GeV}^2 \\ \Delta x &= 0.05 \end{aligned}$$



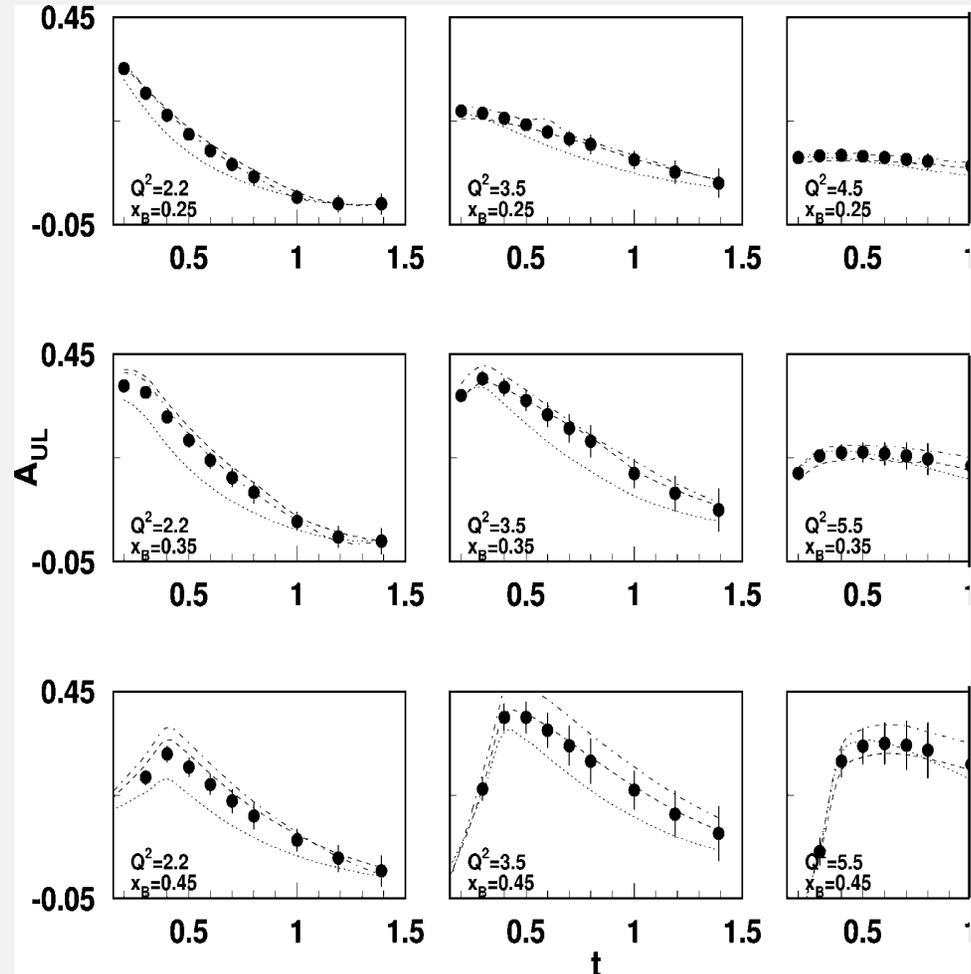
CLAS12 - DVCS/BH Target Asymmetry

$$e \vec{p} \rightarrow e p \gamma$$

$$\Delta\sigma \sim \sin\phi \operatorname{Im}\{F_1 \tilde{H} + \xi(F_1 + F_2) H \dots\} d\phi$$

$$\begin{aligned} L &= 2 \times 10^{35} \\ T &= 1000 \text{ hrs} \\ \Delta Q^2 &= 1 \text{ GeV}^2 \\ \Delta x &= 0.05 \end{aligned}$$

Selected kinematics



Exclusive ρ production on transverse target

$$A_{UT} \sim \text{Im}(AB^*)$$

ρ^0

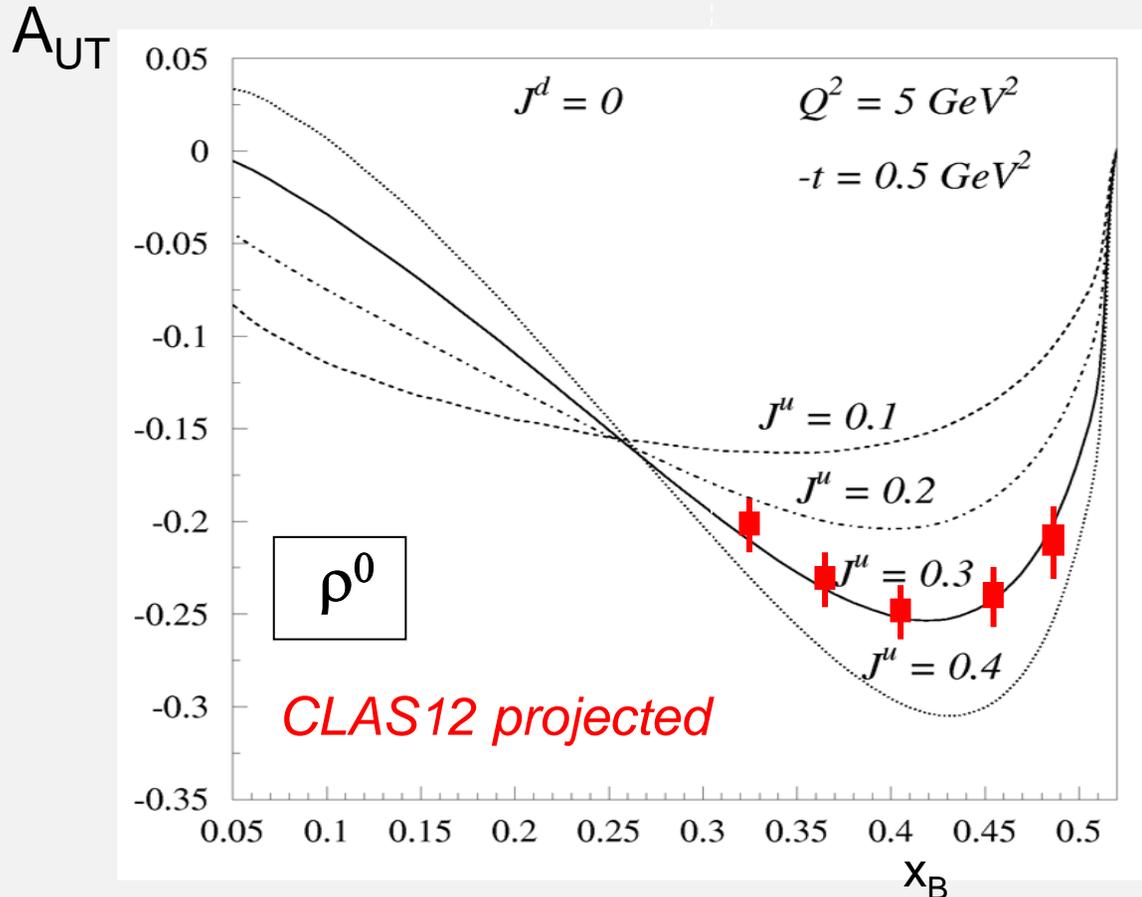
$$A \sim 2H^u + H^d$$

$$B \sim 2E^u + E^d$$

ρ^+

$$A \sim H^u - H^d$$

$$B \sim E^u - E^d$$



Asymmetry depends linearly on the GPD \mathbf{E} in Ji's sum rule.

ρ^0 and ρ^+ measurements allow separation of $\mathbf{E}^u, \mathbf{E}^d$

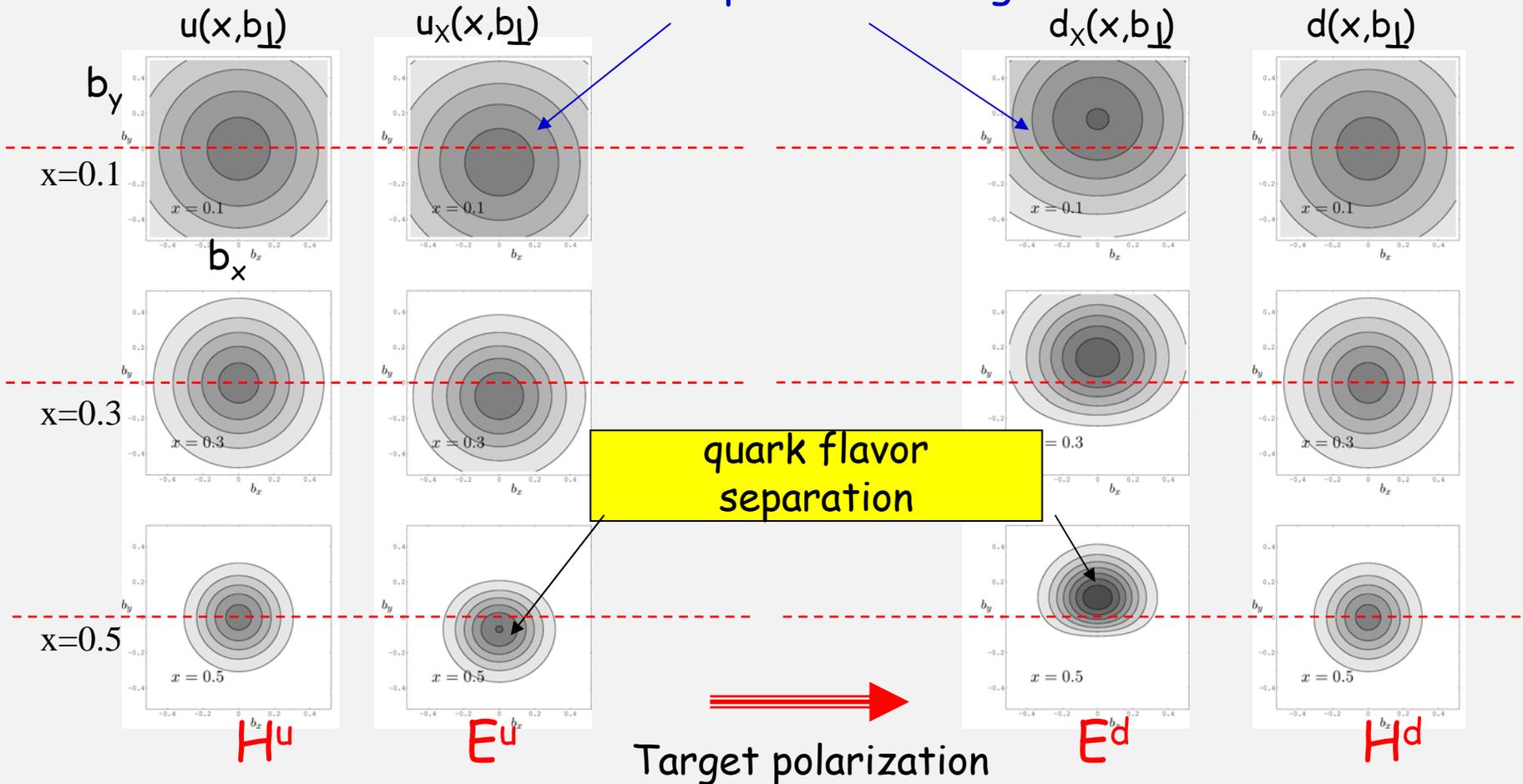
K. Goeke, M.V. Polyakov,
 M. Vanderhaeghen, 2001

Images of the Proton's Quark Content

M. Burkardt (2002)

b_{\perp} - Impact parameter

transverse polarized target



Summary

- The discovery of Generalized Parton Distributions has opened up a new and exciting area of hadron physics that needs exploration in dedicated experiments.
- Moderate to high energy, very high luminosity, and large acceptance spectrometers are needed to measure GPDs in deeply virtual exclusive processes.
- The JLab 12 GeV Upgrade will provide the tools to do this well and explore the nucleon at a deeper level.