

Fundamental Structure of Hadrons

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DOE Science Review for JLab 12 GeV Upgrade

The Science Problem ?

Quantum Chromodynamics (QCD) in the **confinement** regime:
How does it work?

- What do we know?

QCD works in the perturbative (weak) regime

Many experimental tests led to this conclusion, example:

Nucleon as a laboratory

- ➔ Proton is not pointlike (Nobel Prize: Hofstadter); Elastic electron scattering
- ➔ Quarks and gluons/Partons are the constituents; Deep Inelastic electron Scattering (Nobel prize: Friedman, Kendall and Taylor, 1991).

Theory celebrated recently

Asymptotic freedom (Nobel prize: Gross, Politzer and Wilczek, 2004).

but

Confinement in QCD is still a puzzle and among the 10 top problems in Physics! (Gross, Witten,....)

Strings 2000

Why JLab 12 GeV?

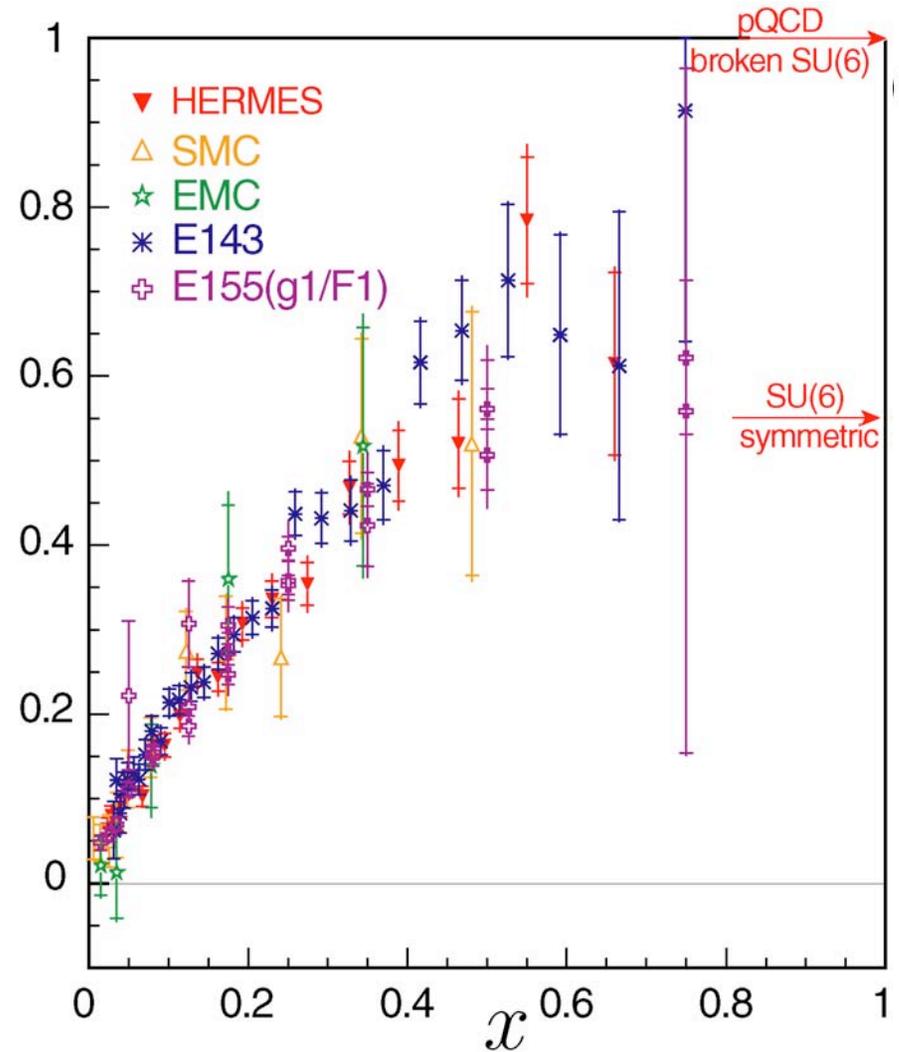
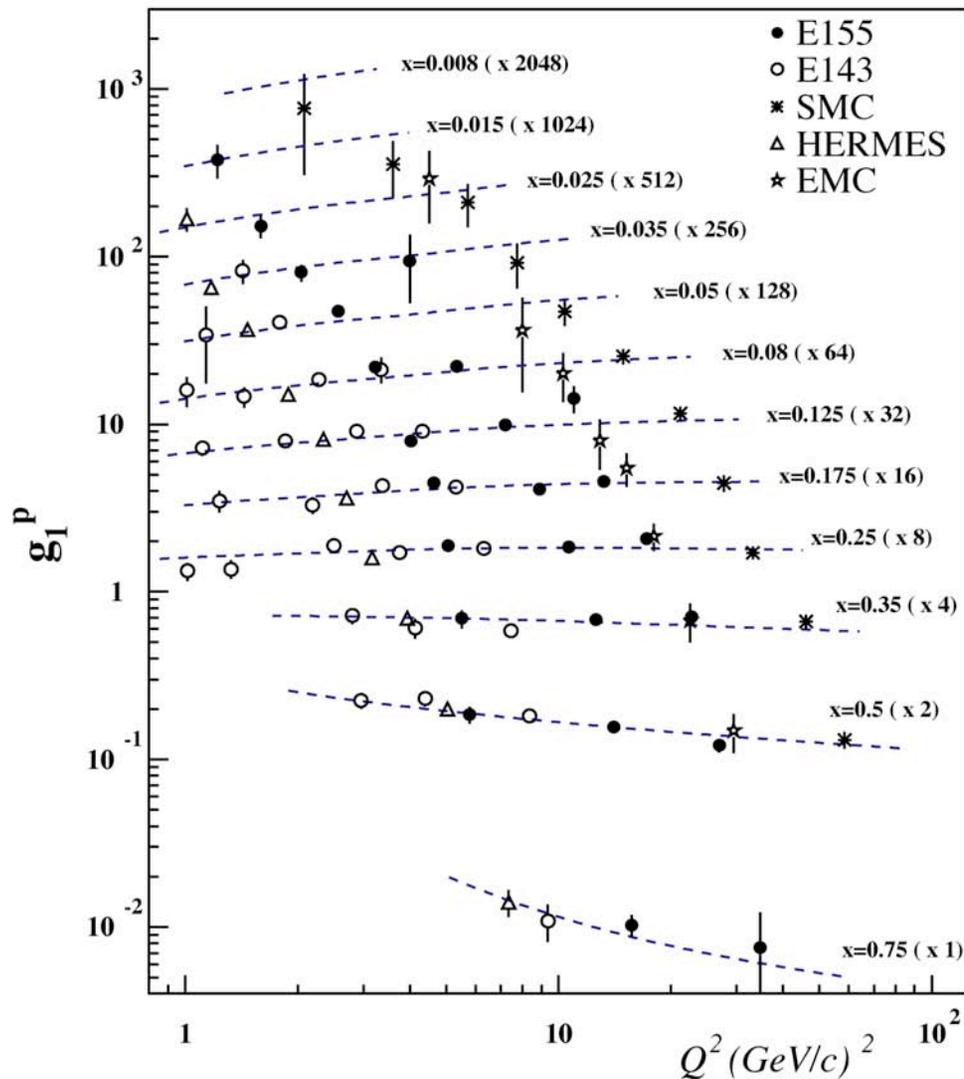
- Transition from pQCD to Strong QCD needs data with high precision for a quantitative understanding of confinement

What quantities do we measure?

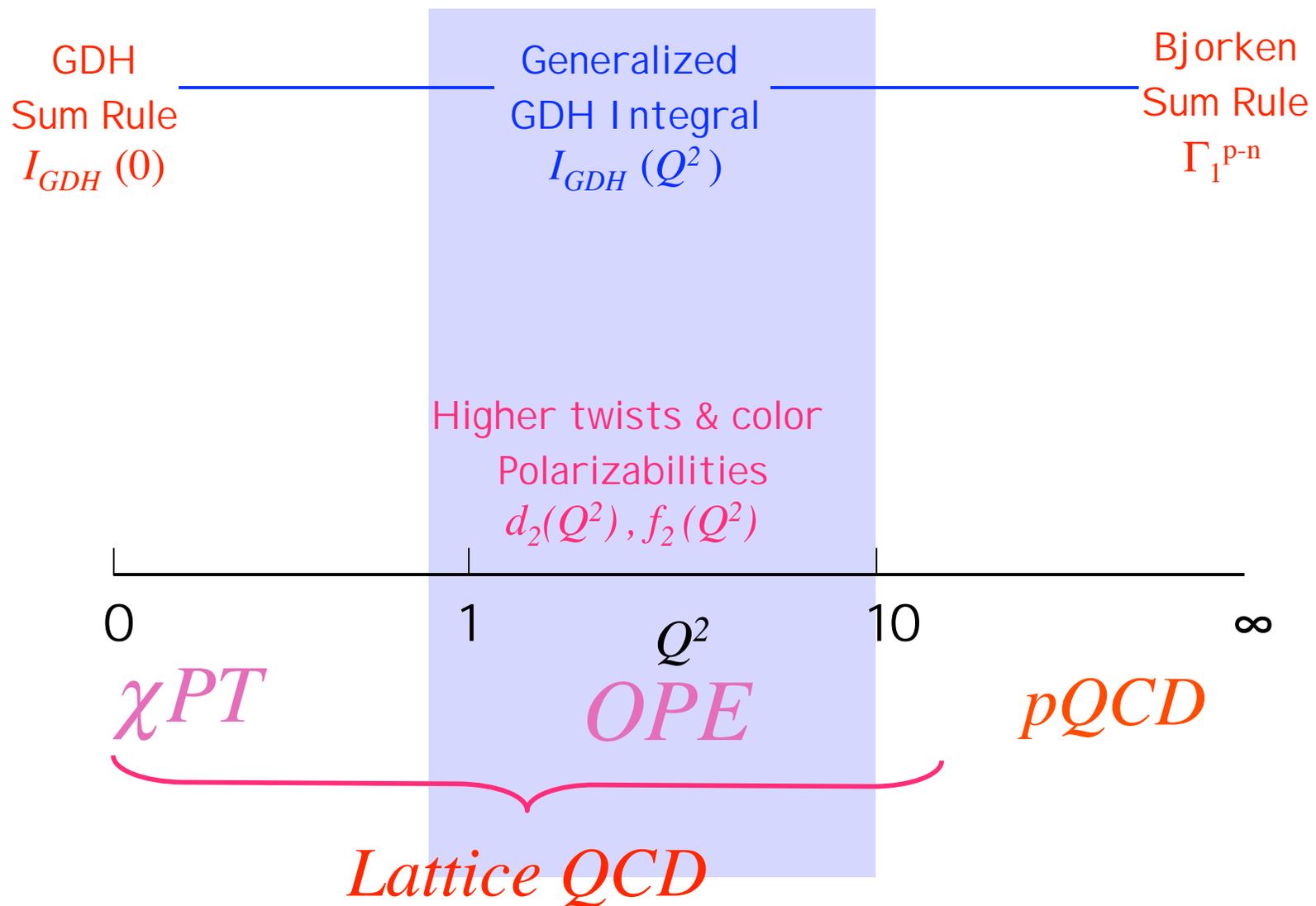
- ➔ Nucleon structure functions: [System responds incoherently]
 - ➔ Determine the helicity-dependent and -independent parton distributions at large x with flavor decomposition
 - ➔ Determine higher moments of structure functions to compare to Lattice QCD
- ➔ Hadron form factors : pion, nucleon [System responds coherently]

Examples of existing data and physics issues

World data on g_1^p



Examples of observables and theory tools



Inclusive DIS

- Unpolarized structure functions $F_1(x, Q^2)$ and $F_2(x, Q^2)$

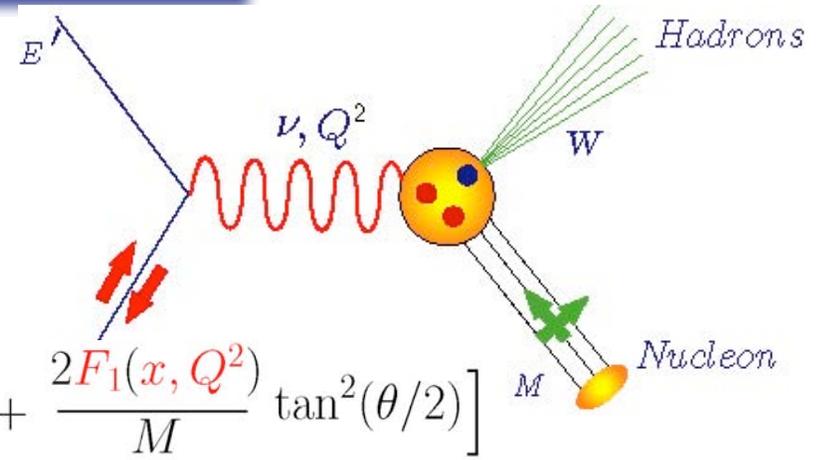
→ Proton & neutron measurements provide d/u distributions ratio

$$U \quad \frac{d^2\sigma}{dE'd\Omega}(\downarrow\uparrow + \uparrow\uparrow) = \frac{8\alpha^2 \cos^2(\theta/2)}{Q^4} \left[\frac{F_2(x, Q^2)}{\nu} + \frac{2F_1(x, Q^2)}{M} \tan^2(\theta/2) \right]$$

- Polarized structure functions

$g_1(x, Q^2)$ and $g_2(x, Q^2)$

→ Proton & neutron measurements combined with d/u provide the spin-flavor distributions $\Delta u/u$ & $\Delta d/d$



Q^2 : Four-momentum transfer
 x : Bjorken variable
 ν : Energy transfer
 M : Nucleon mass
 W : Final state hadrons mass

$$L \quad \frac{d^2\sigma}{dE'd\Omega}(\downarrow\uparrow - \uparrow\uparrow) = \frac{4\alpha^2 E'}{MQ^2 \nu E} \left[(E + E' \cos \theta) g_1(x, Q^2) - \frac{Q^2}{\nu} g_2(x, Q^2) \right]$$

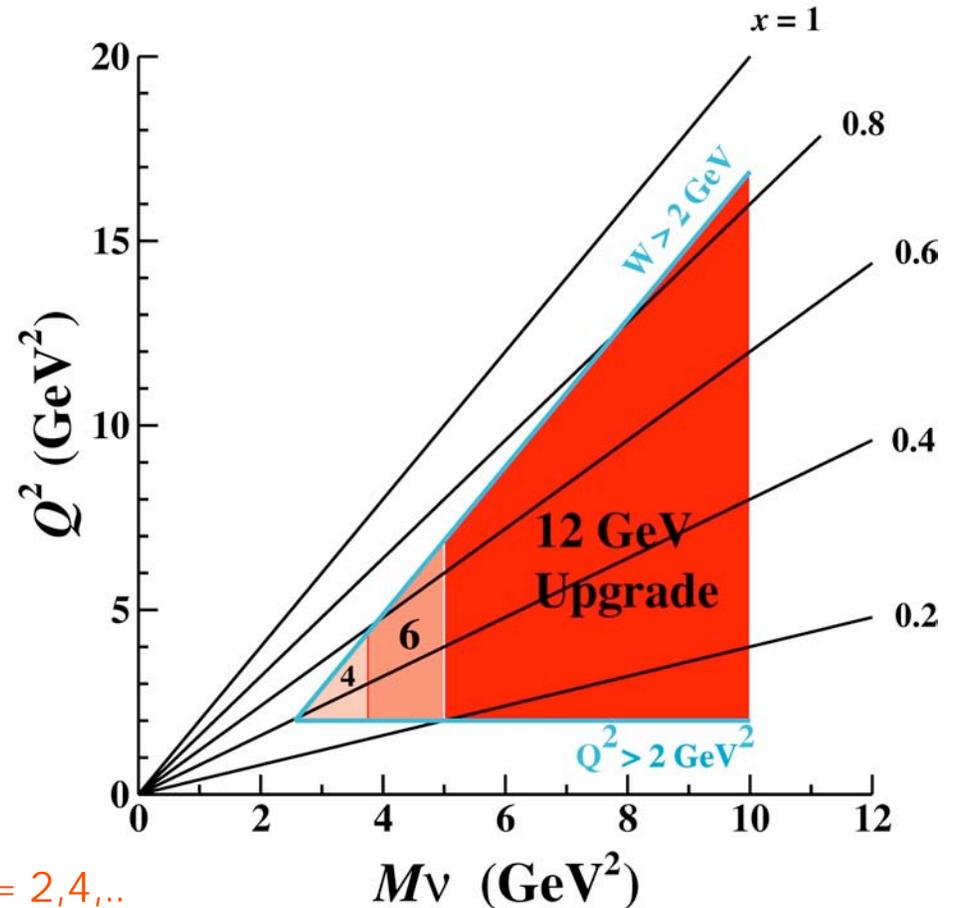
$$T \quad \frac{d^2\sigma}{dE'd\Omega}(\downarrow\Rightarrow - \uparrow\Rightarrow) = \frac{4\alpha^2 \sin \theta E'^2}{MQ^2 \nu^2 E} \left[\nu g_1(x, Q^2) + 2E g_2(x, Q^2) \right]$$

12 GeV upgrade kinematical reach

- Access to very large x ($x > 0.4$)
 - ➔ Clean region
 - ➔ No strange sea effects
 - ➔ No explicit hard gluons to be included
- Quark models can be a powerful tool to investigate the structure of the nucleon
- Comparison with lattice QCD is possible for higher moments of structure functions.

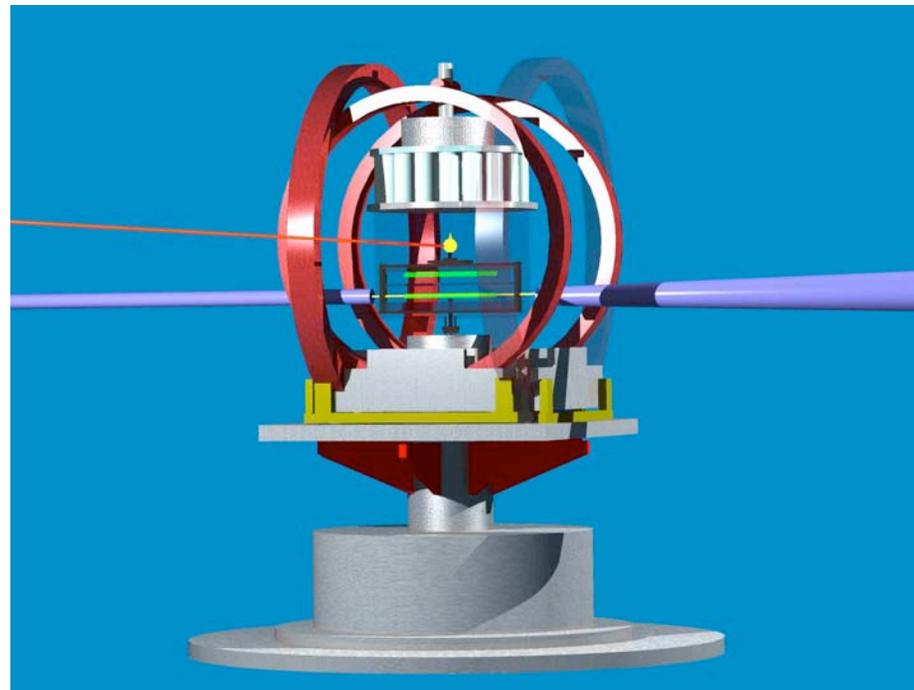
$$M_n(Q^2) = \int_0^1 dx x^{n-2} F_2(x, Q^2) \quad n = 2, 4, \dots$$

$$M_n(Q^2) = \int_0^1 dx x^{n-1} g_1(x, Q^2), \quad n = 1, 3, 5, \dots$$



The tools

- A high duty cycle, high current, polarized 12 GeV electron beam
- A high luminosity Hall.
- A large acceptance Hall.
- Polarized targets



PDFs in the valence quark region

Understand the nucleon structure in the valence quark region

- What is required?

➔ Complete knowledge of parton distribution functions (PDFs).

➔ Unpolarized, helicity-dependent

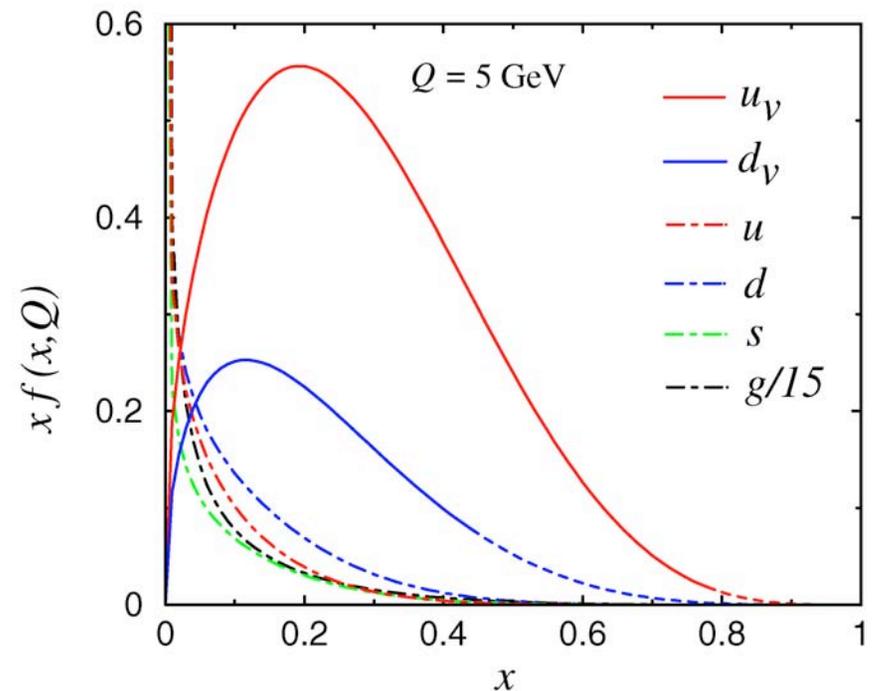
➔ Theoretically

➔ large x exposes valence quarks
- free of sea effects

➔ $x \rightarrow 1$ behavior - sensitive test of
spin-flavor symmetry breaking

➔ important for higher moments of
PDFs - compare with **lattice QCD**

➔ intimately related with resonances,
quark-hadron duality

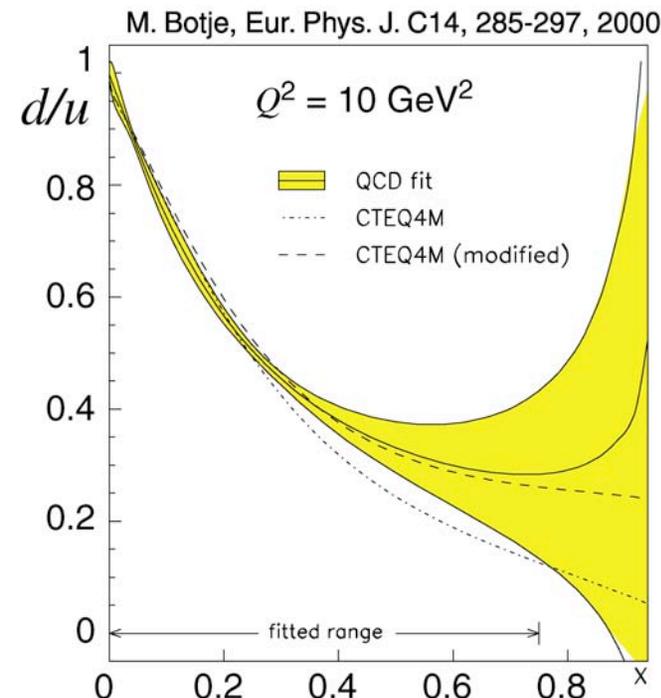
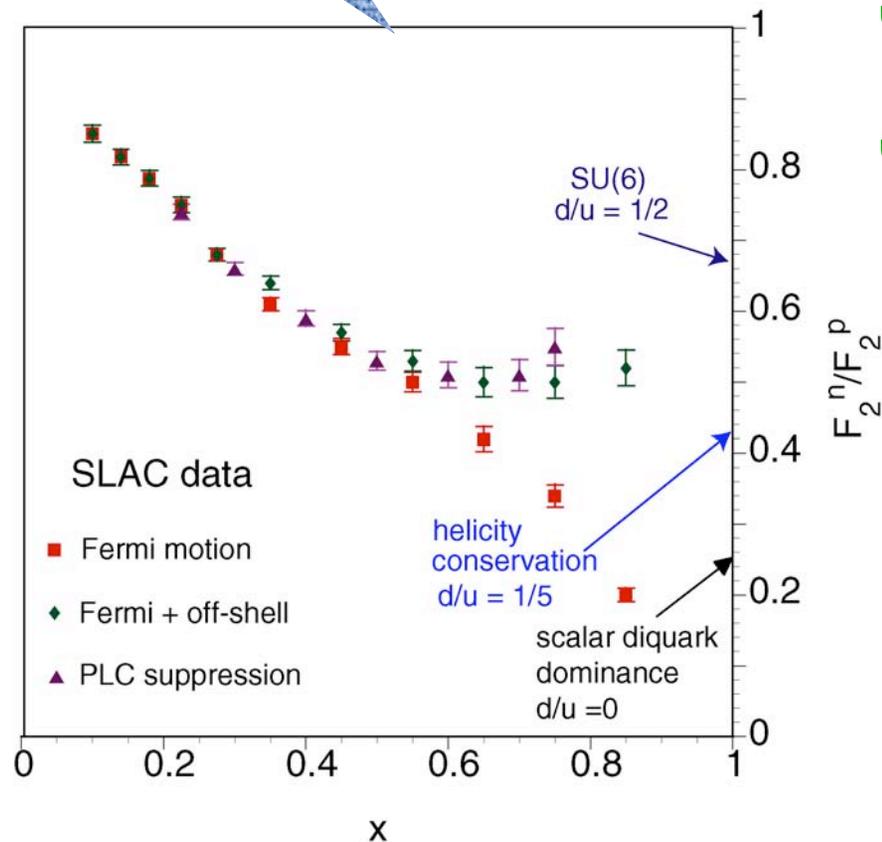


Unpolarized Neutron to Proton ratio

• In the large x region ($x > 0.5$) the ratio F_2^n/F_2^p is not well determined due to the lack of free neutron targets

• Impact:

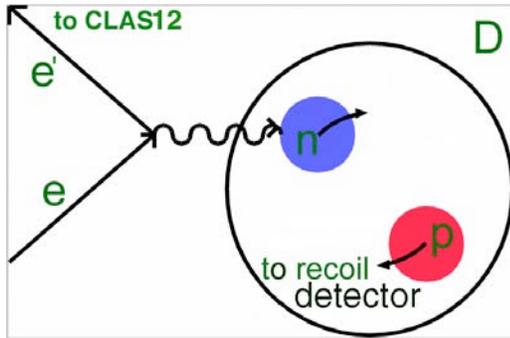
- determine valence d quark momentum distribution
- extract helicity dependent quark distributions through inclusive DIS
- high x and Q^2 background in high energy particle searches.
- construct moments of structure functions



Unpolarized Neutron to Proton ratio

Spectator tagging

- Nearly free neutron target by tagging low-momentum proton from deuteron at backward angles



- Small p (70-100 MeV/c)
 - Minimize on-shell extrapolation (neutron only 7 MeV off-shell)
- Backward angles ($\theta_{pq} > 110^\circ$)
 - Minimize final state interactions

DIS from A=3 nuclei

- Mirror symmetry of A=3 nuclei
 - Extract F_2^n/F_2^p from ratio of ${}^3\text{He}/{}^3\text{H}$ structure functions

$$\frac{F_2^n}{F_2^p} = \frac{2\mathcal{R} - F_2^{3\text{He}}/F_2^{3\text{H}}}{2F_2^{3\text{He}}/F_2^{3\text{H}} - \mathcal{R}}$$

- Super ratio

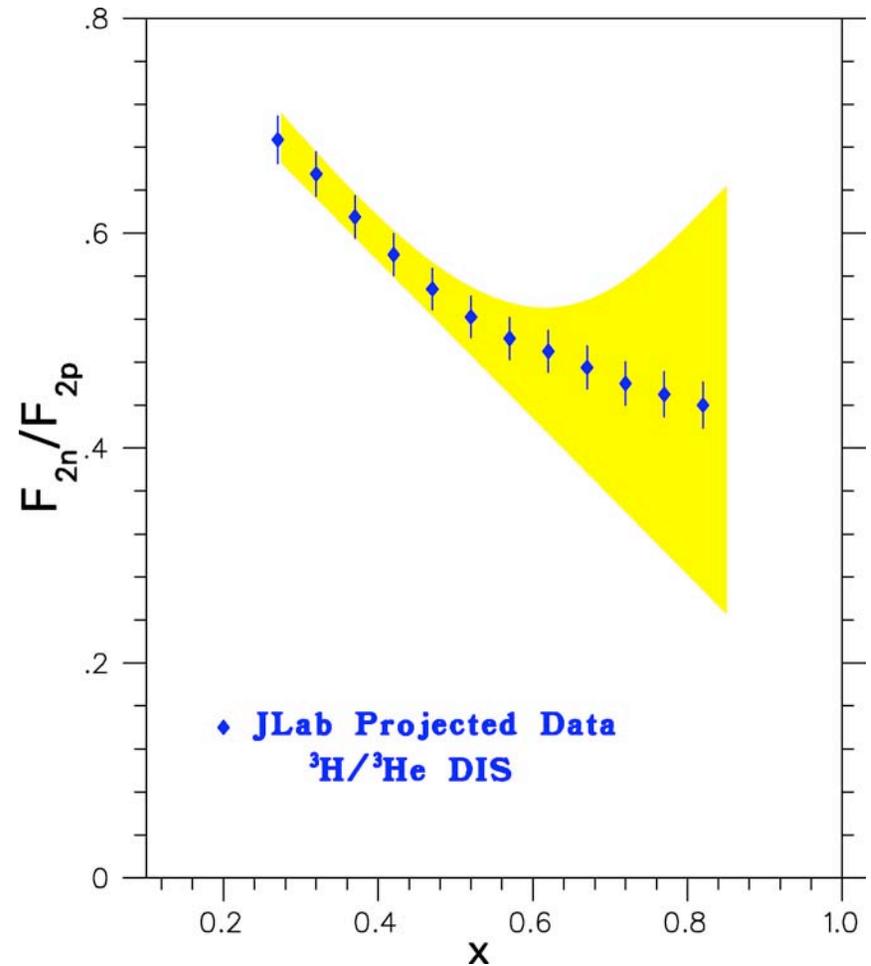
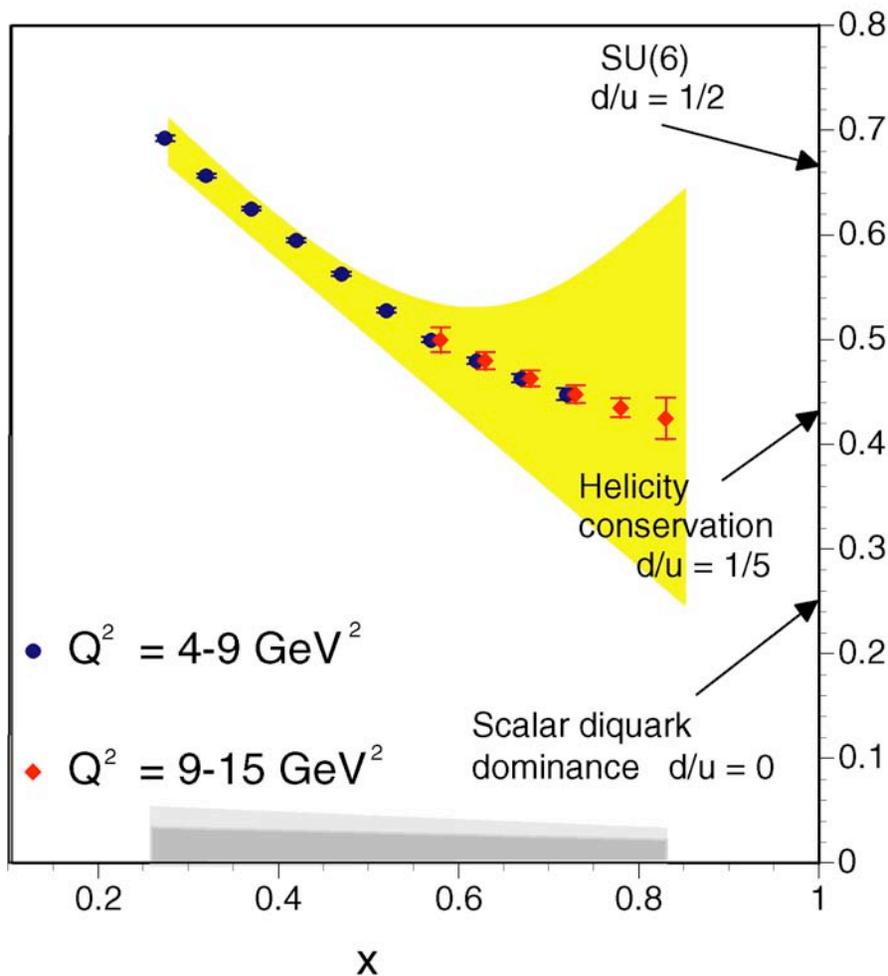
\mathcal{R} = ratio of "EMC ratios" for ${}^3\text{He}$ and ${}^3\text{H}$ calculated to within 1%

- Most systematic and theoretical uncertainties cancel

Unpolarized Neutron to Proton Ratio

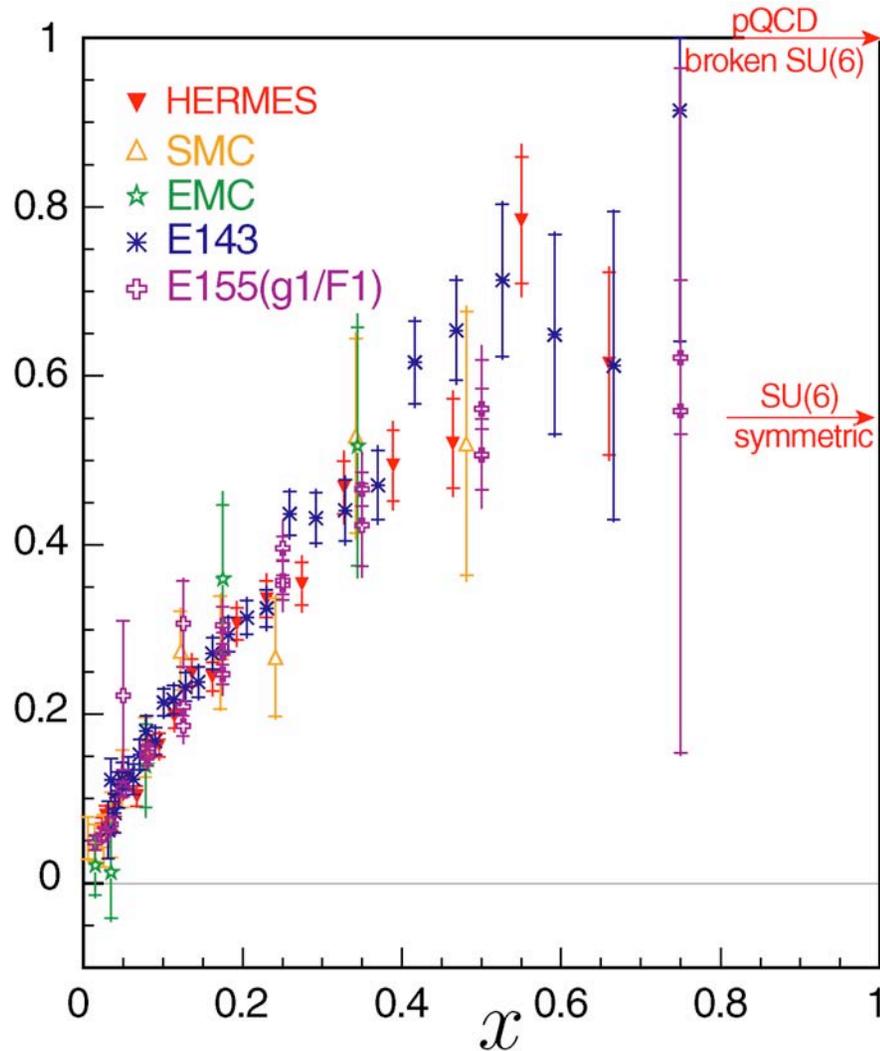
Hall B 11 GeV with CLAS12

Hall C 11 GeV with HMS

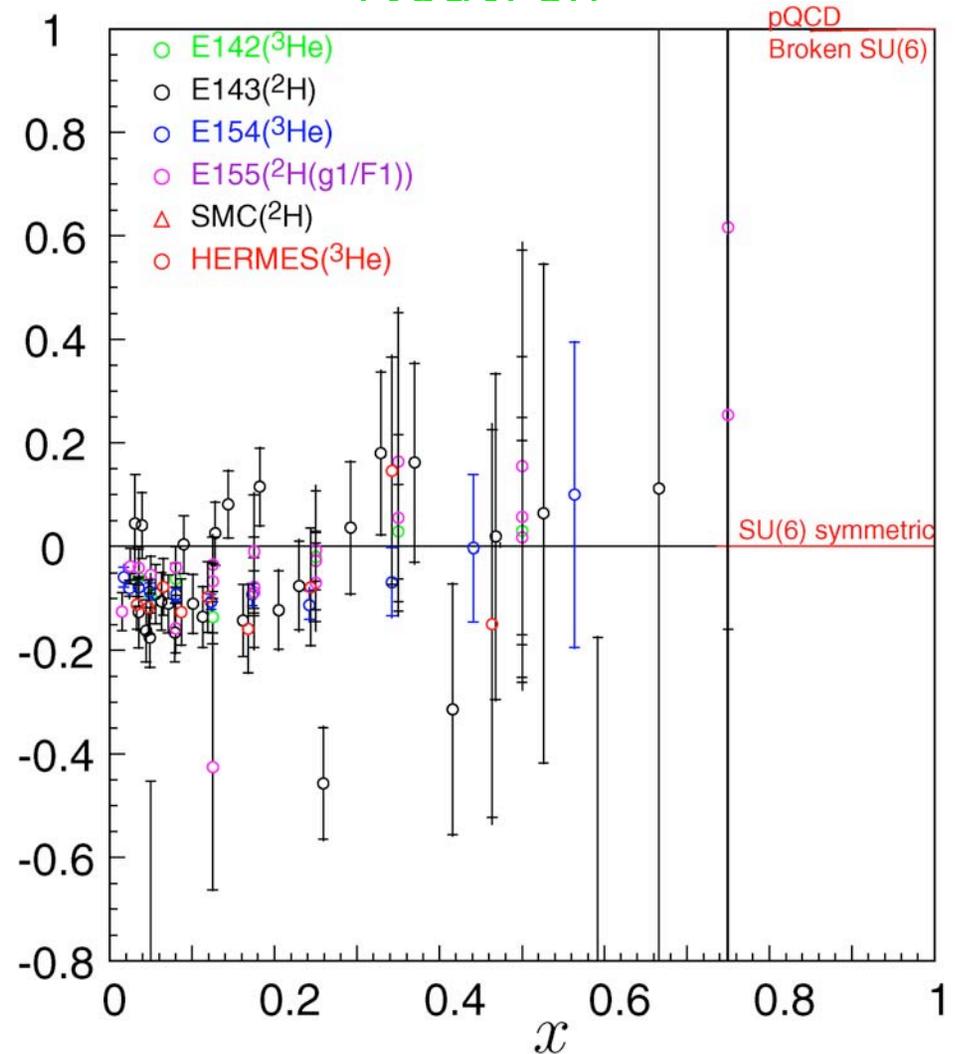


World data for A_1

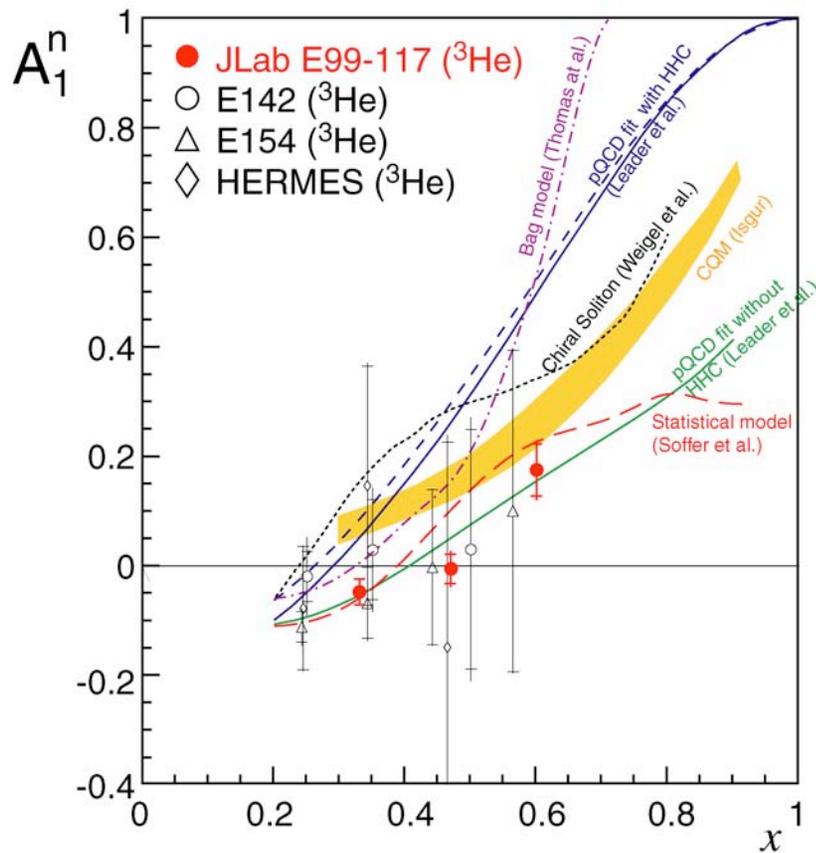
Proton



Neutron



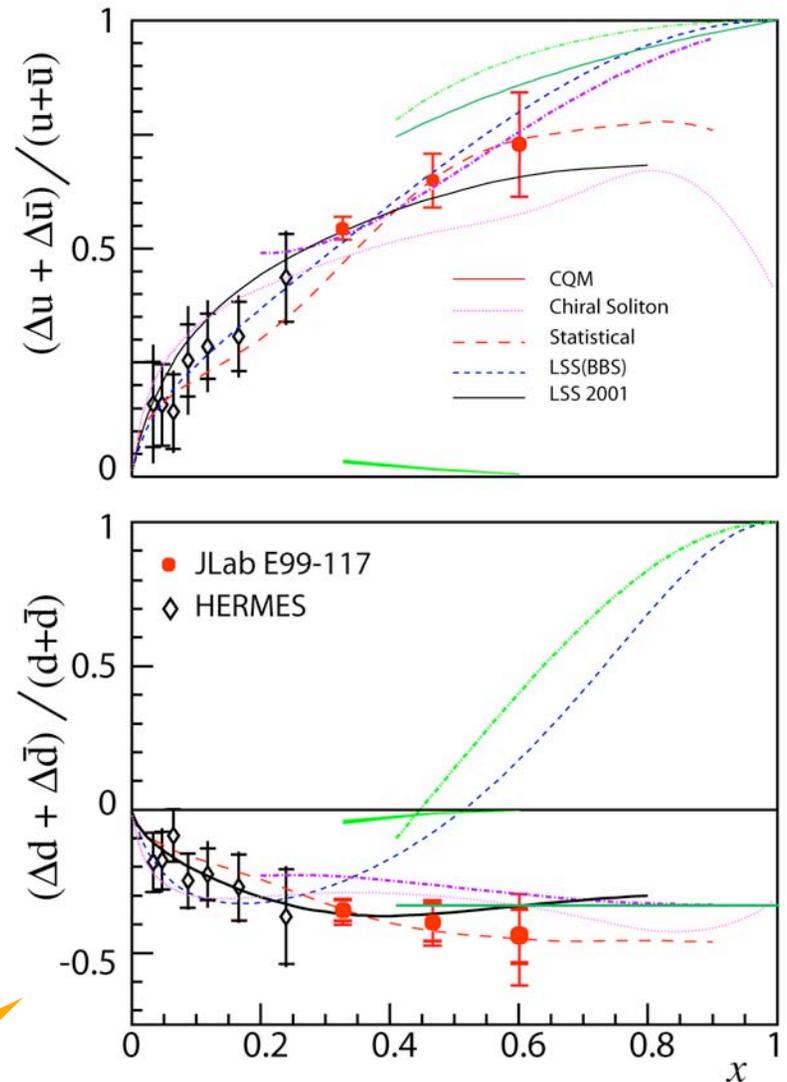
A_1^n and Helicity-Flavor Decomposition



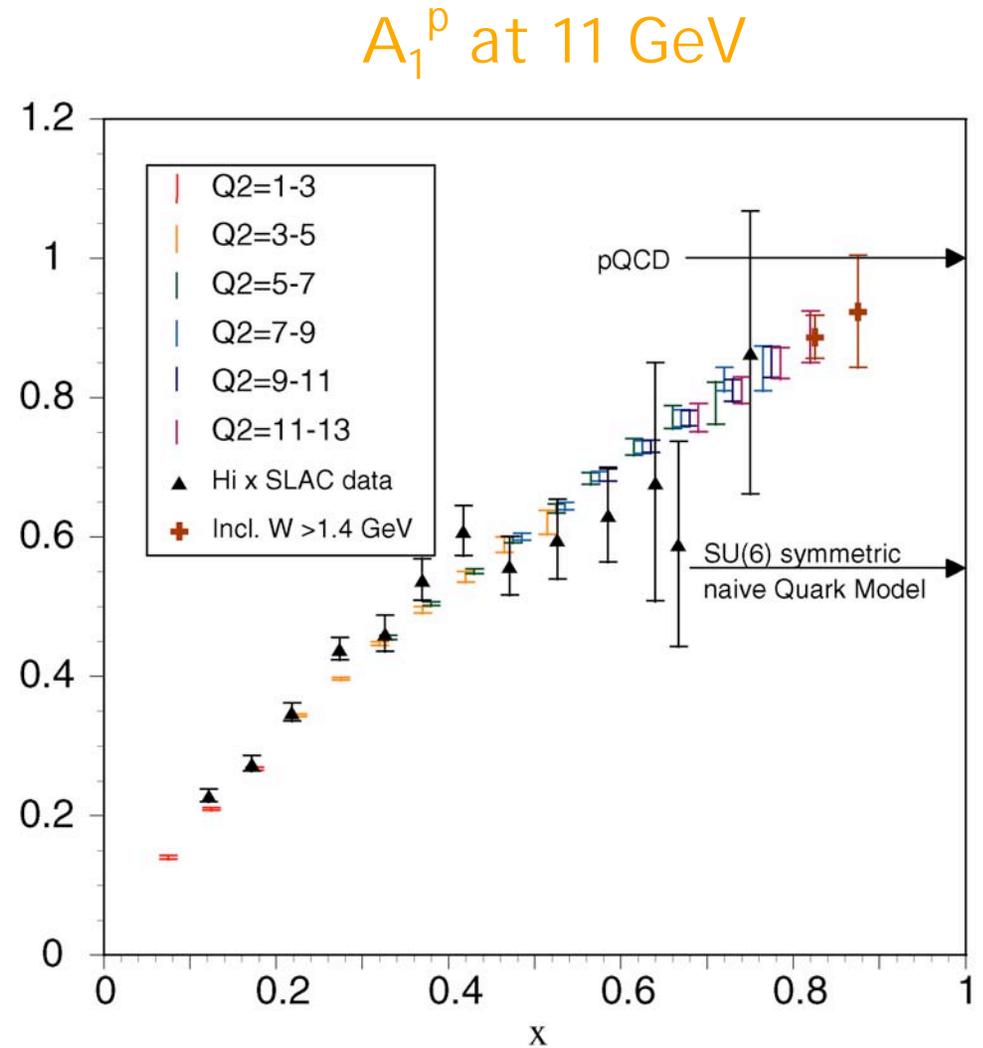
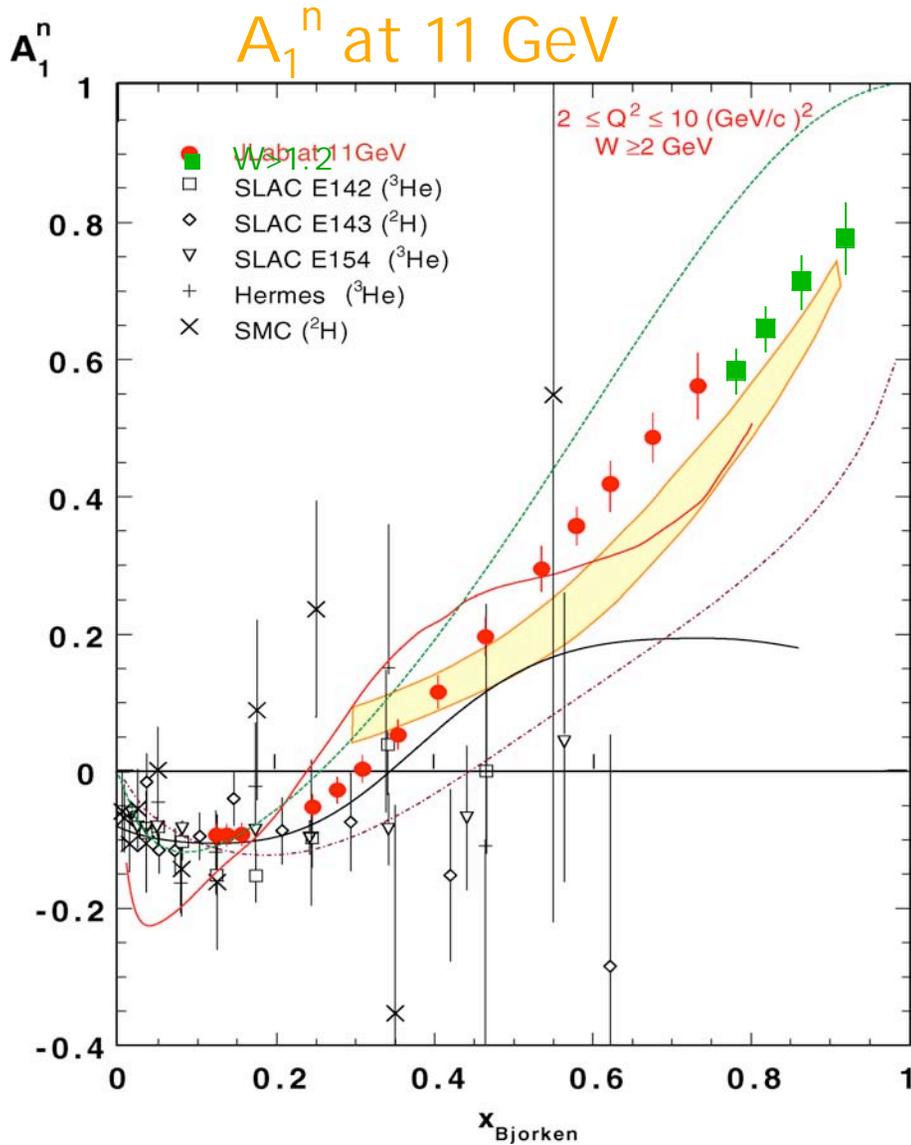
$$\frac{\Delta u + \Delta \bar{u}}{u} = \frac{4}{15} \frac{g_1^p}{F_1^p} (4 + R^{du}) - \frac{1}{15} \frac{g_1^n}{F_1^n} (1 + 4R^{du})$$

$$\frac{\Delta d + \Delta \bar{d}}{d} = \frac{4}{15} \frac{g_1^n}{F_1^n} (4 + \frac{1}{R^{du}}) - \frac{1}{15} \frac{g_1^p}{F_1^p} (1 + 4\frac{1}{R^{du}})$$

$$R^{du} = \frac{d + \bar{d}}{u + \bar{u}}$$



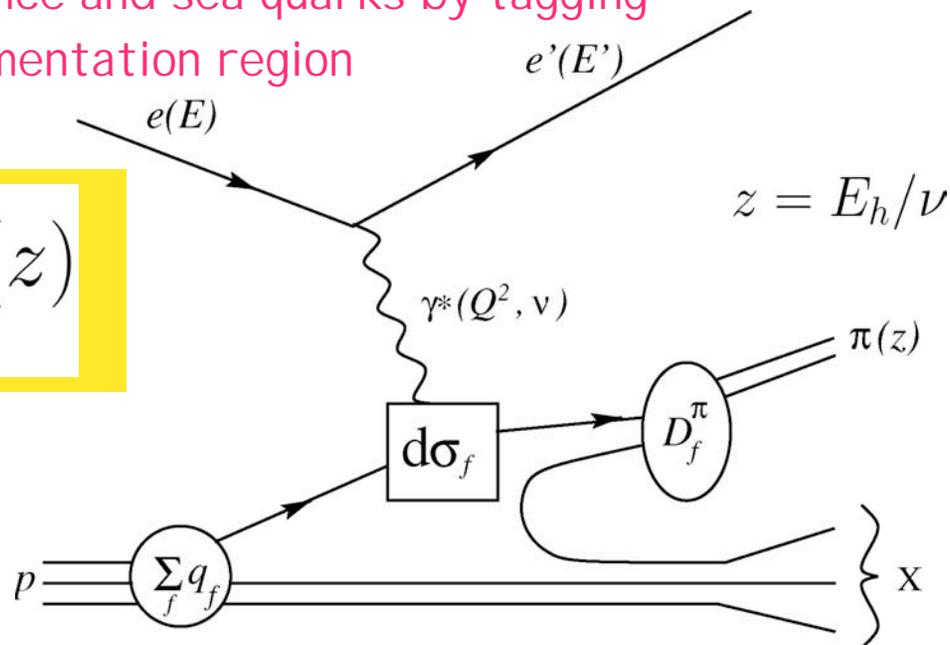
Inclusive measurements of asymmetries



Semi-inclusive DIS

- Spin-flavor decomposition of valence and sea quarks by tagging hadron (e.g. π , K) in current fragmentation region

$$d\sigma = \sum_f e_f^2 q_f(x) D_f^h(z)$$



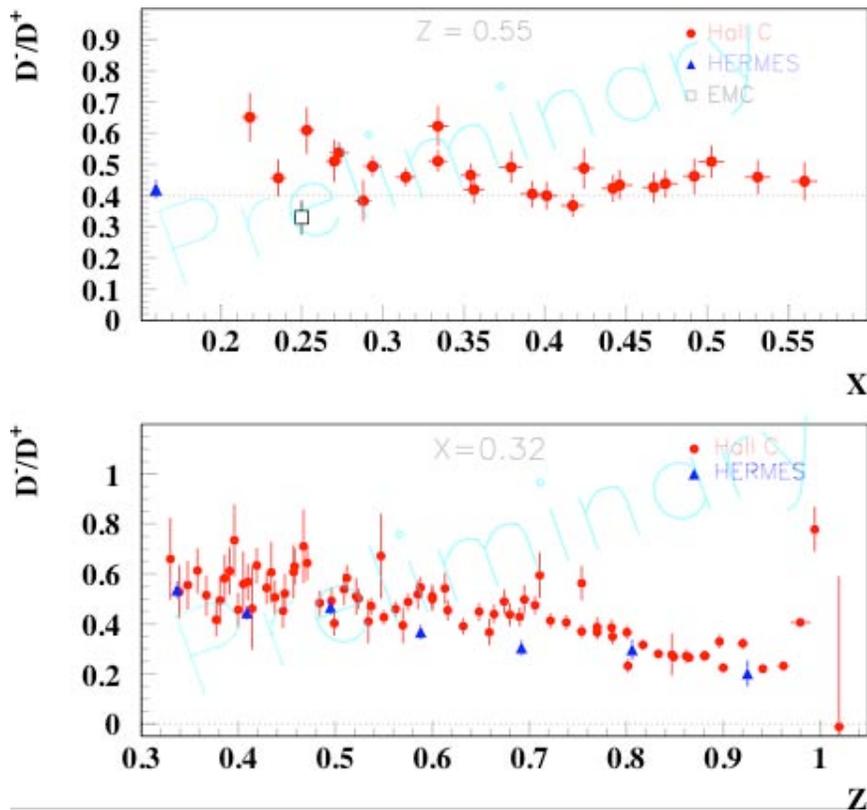
$D(\mathbf{z})$ quark--> hadron fragmentation function

- ➔ unpolarized or polarized beam and target
- ➔ mass of unobserved X system, $W_X > 2 \text{ GeV}$

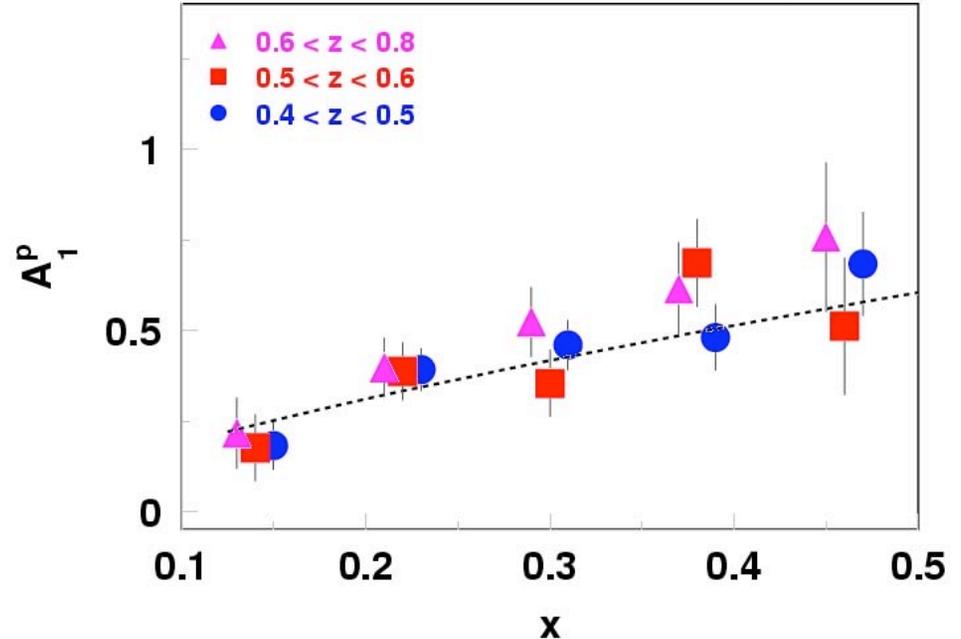
Semi-inclusive DIS (Factorization!)

Factorization of current and target fragmentation

- Berger criterion $\Delta\eta > 2$ to avoid contamination from target fragmentation ($z > 0.4$)

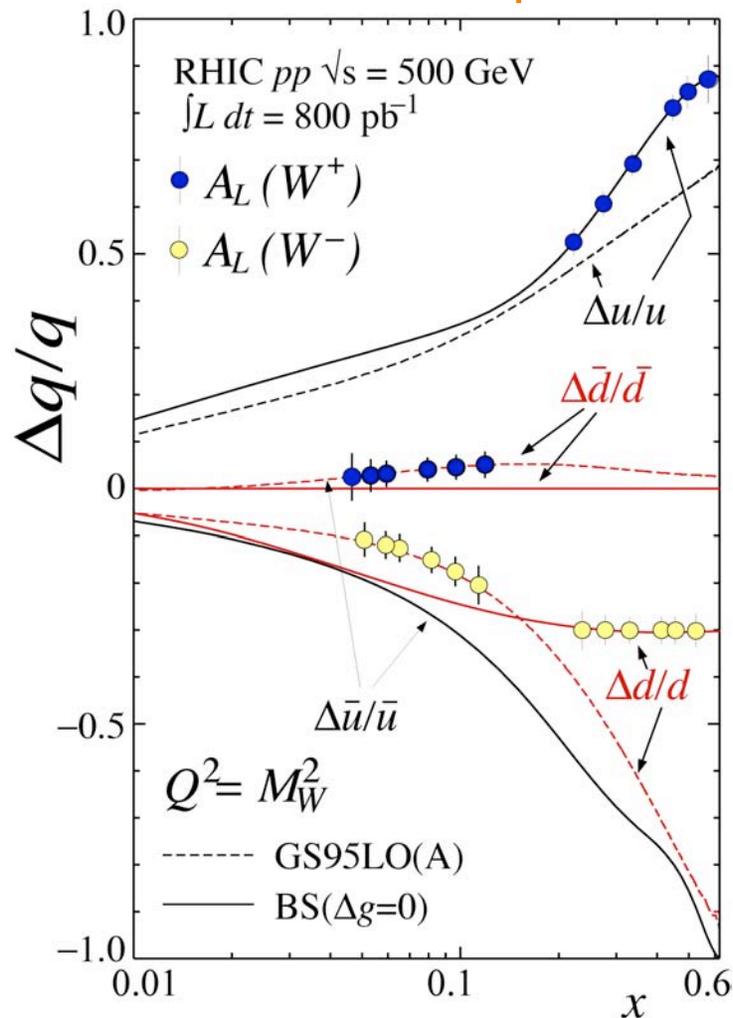


$ep \rightarrow e' \pi^+ X$ ($E_e = 5.7$ GeV, $M_X > 1.1$)

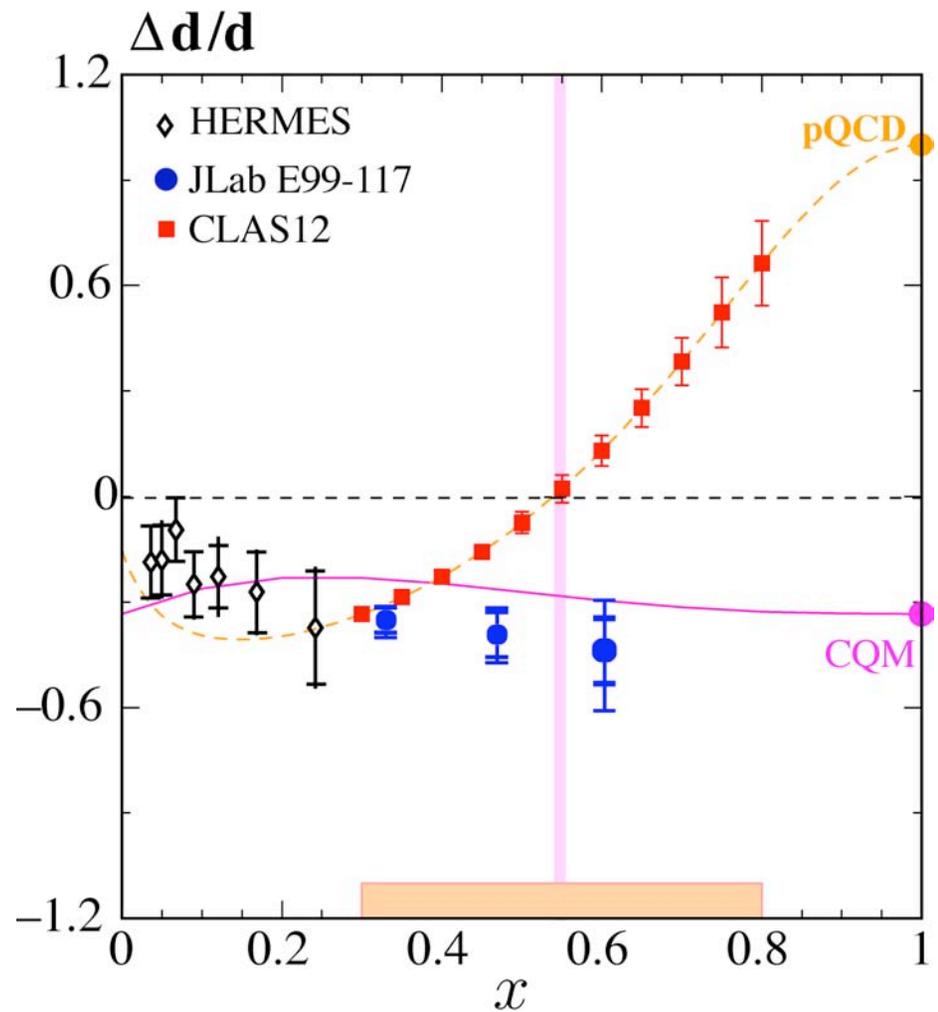


Flavor decomposition (2)

At RHIC C with W production



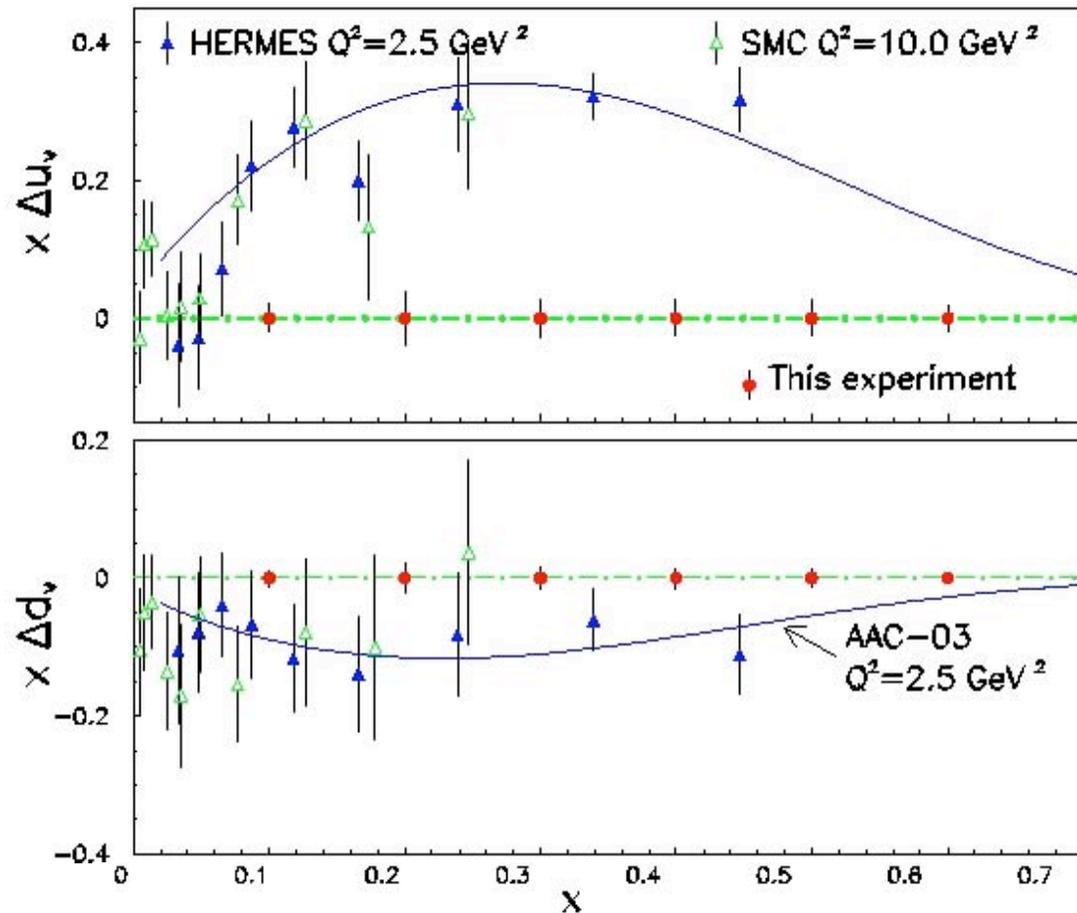
At JLab 12 GeV with SIDIS



Flavor decomposition (2)

$E_e = 11 \text{ GeV}$ NH_3 and ^3He

- Asymmetry measurements with different hadrons (π^+ , π^-) and targets (p,n) allow flavor separation



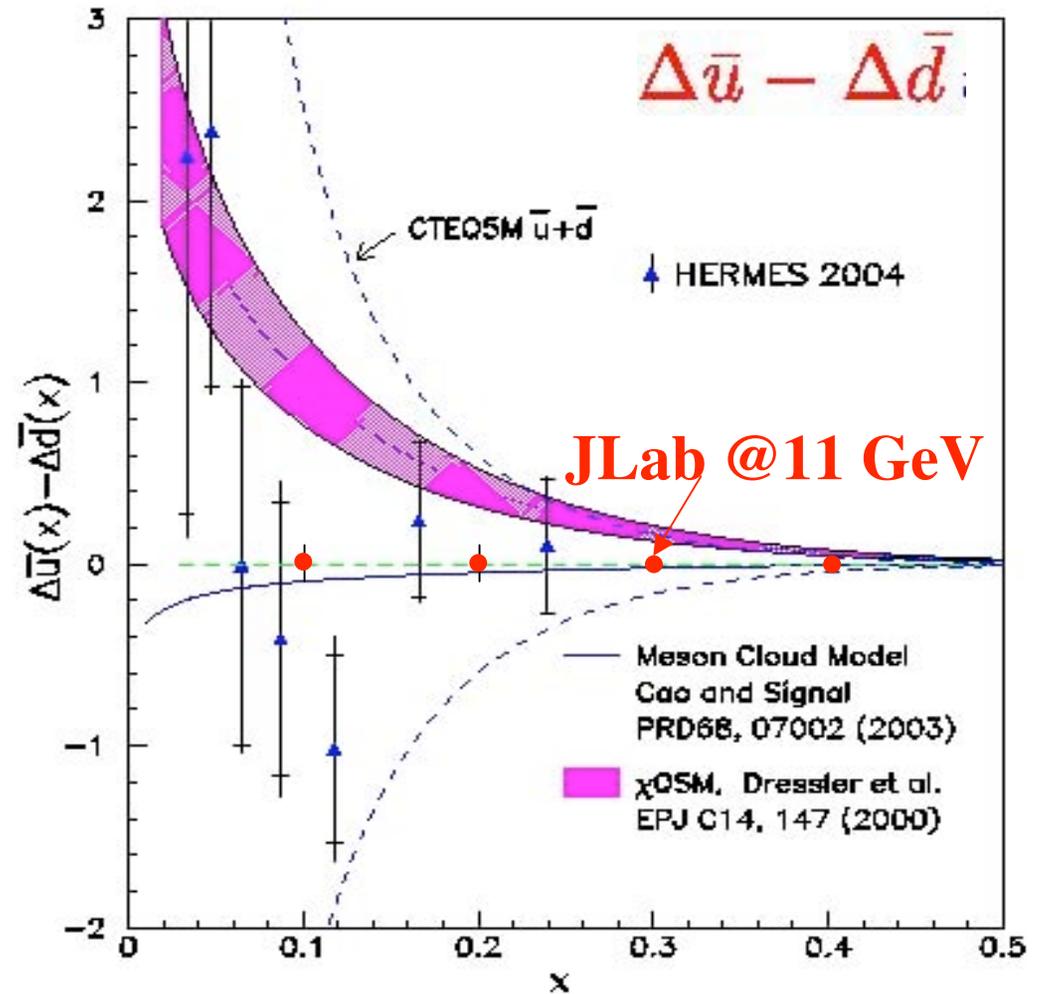
Flavor decomposition: polarized sea

- Predictions:
 - ➔ Instantons (χ QSM):

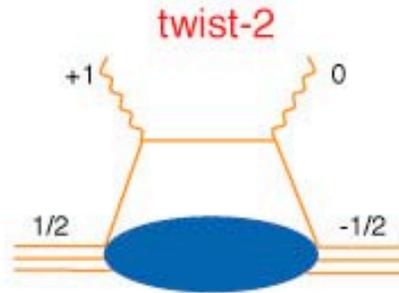
$$\Delta\bar{u} \approx -\Delta\bar{d}$$

- First data from HERMES

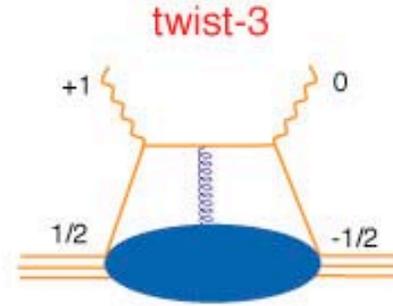
$$\Delta\bar{u} - \Delta\bar{d} \approx 0$$



Quark-gluon correlations and g_2



Carry one unit of orbital angular momentum



Couple to a gluon

$$g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$$

- a twist-2 term (Wandzura & Wilczek, 1977):

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 g_1(y, Q^2) \frac{dy}{y}$$

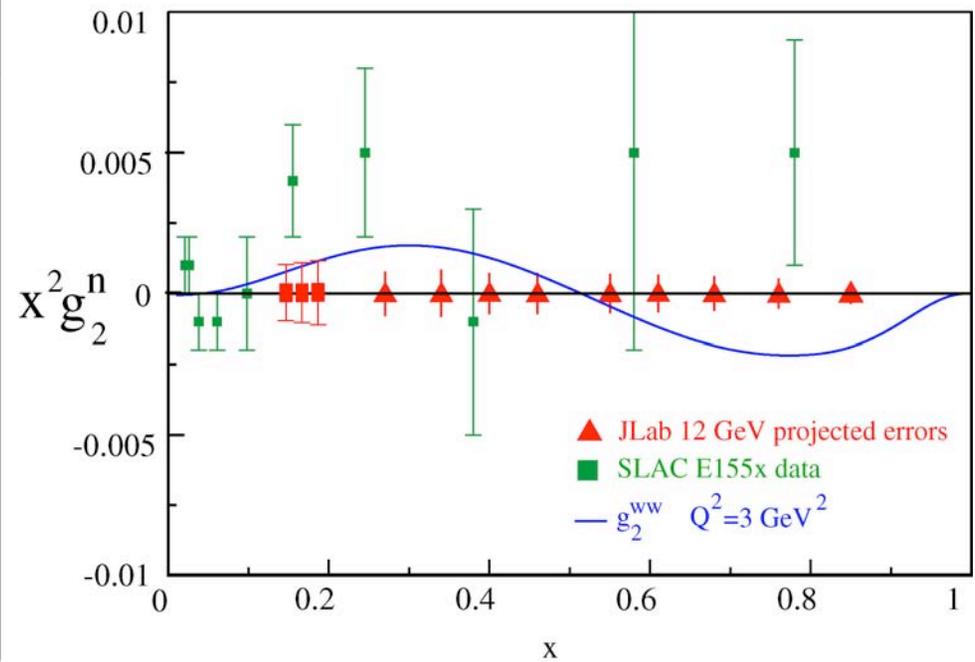
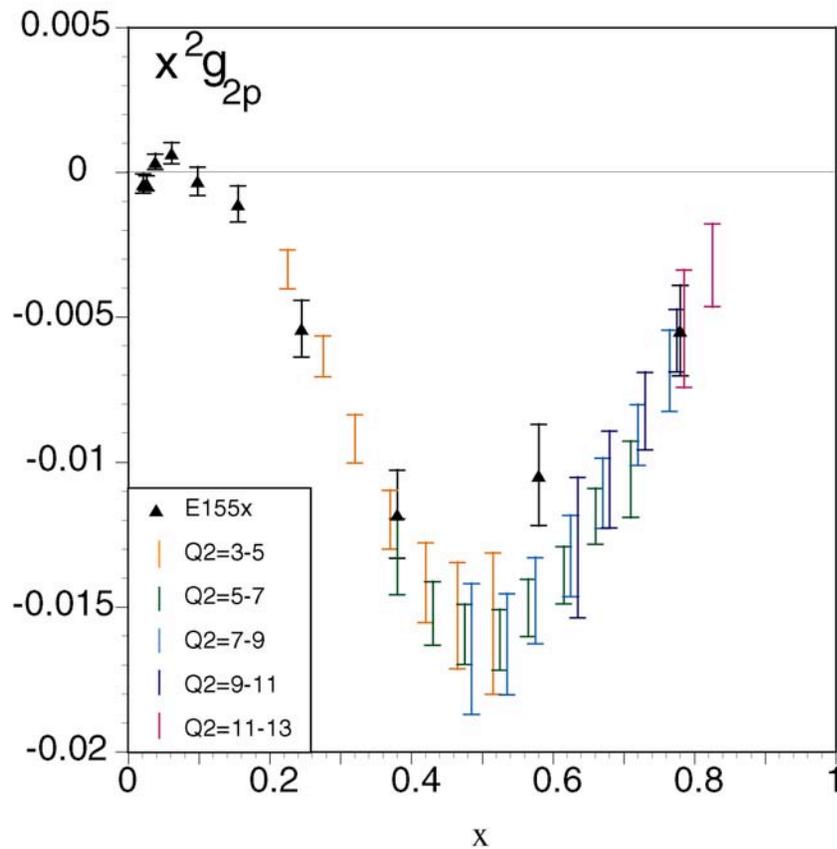
- a twist-3 term with a suppressed twist-2 piece (Cortes, Pire & Ralston, 92):

$$\bar{g}_2(x, Q^2) = -\int_x^1 \frac{\partial}{\partial y} \left(\frac{m_q}{M} h_T(y, Q^2) + \xi(y, Q^2) \right) \frac{dy}{y}$$

transversity

quark-gluon correlation

g_2 at JLab with 11 GeV



Color “Polarizabilities”

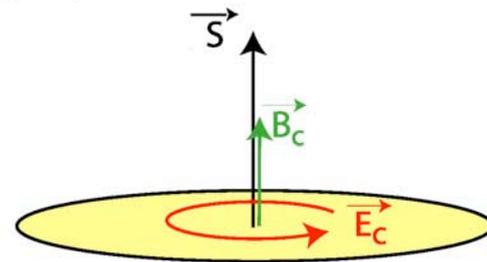
How does the gluon field respond when a nucleon is polarized ?

Define color magnetic and electric polarizabilities (in nucleon rest frame):

$$\chi_{B,E} 2M^2 \vec{S} = \langle PS | \vec{O}_{B,E} | PS \rangle$$

where $\vec{O}_B = \psi^\dagger g \vec{B} \psi$

$$\vec{O}_E = \psi^\dagger \vec{\alpha} \times g \vec{E} \psi$$



$$d_2 = (\chi_E + 2\chi_B)/8$$

$$f_2 = (\chi_E - \chi_B)/2$$

d_2 and f_2 represent the response of the color \vec{B} & \vec{E} fields to the nucleon polarization

Moments of Structure Functions

$$\begin{aligned} \rightarrow \Gamma_1(Q^2) &\equiv \int_0^1 dx g_1(x, Q^2) \\ &= \Gamma_1^{\text{twist}-2}(Q^2) + \frac{M_N^2}{9Q^2} [a_2(Q^2) + 4d_2(Q^2) + 4f_2(Q^2)] + \mathcal{O}\left(\frac{M_N^4}{Q^4}\right) \end{aligned}$$

$$\rightarrow a_2(Q^2) \equiv 2 \int_0^1 dx x^2 g_1^{\text{twist}-2}(x, Q^2) \rightarrow \text{target mass correction term}$$

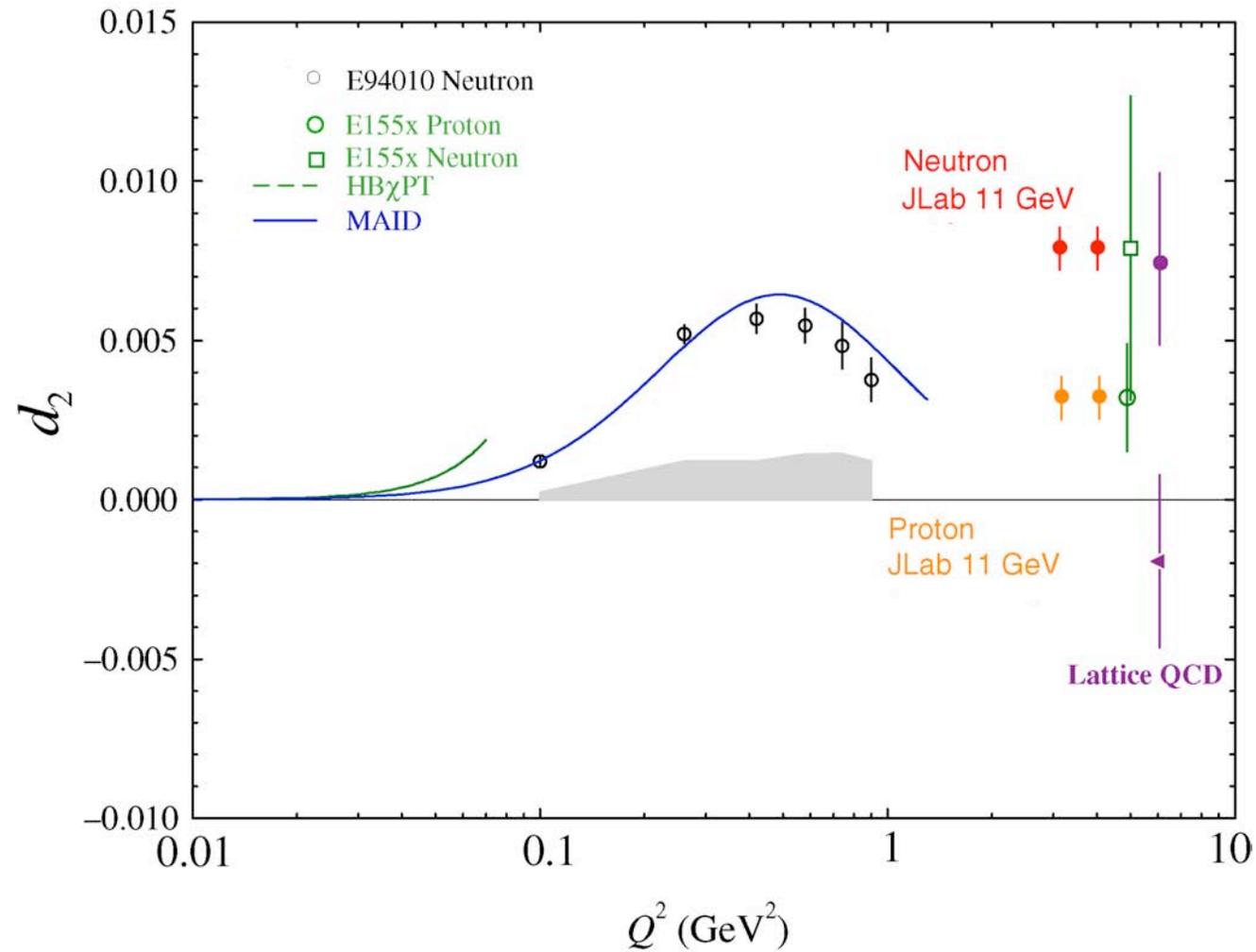
$$\rightarrow d_2(Q^2) \rightarrow \text{dynamical twist-3 matrix element}$$

$$d_2(Q^2) \equiv \int_0^1 dx x^2 \{3g_2(x, Q^2) + 2g_1(x, Q^2)\}$$

$$\rightarrow f_2(Q^2) \rightarrow \text{dynamical twist-4 matrix element}$$

- Both d_2 and f_2 are required to determine the color polarizabilities
- To extract f_2 , d_2 needs to be determined first.

d_2 with 11 GeV at JLab

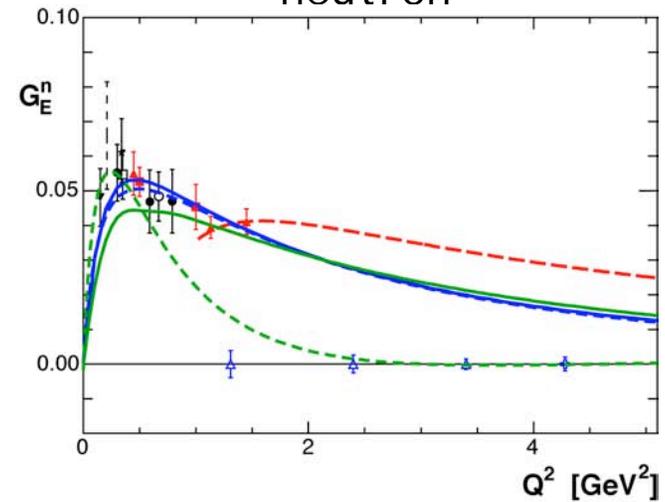
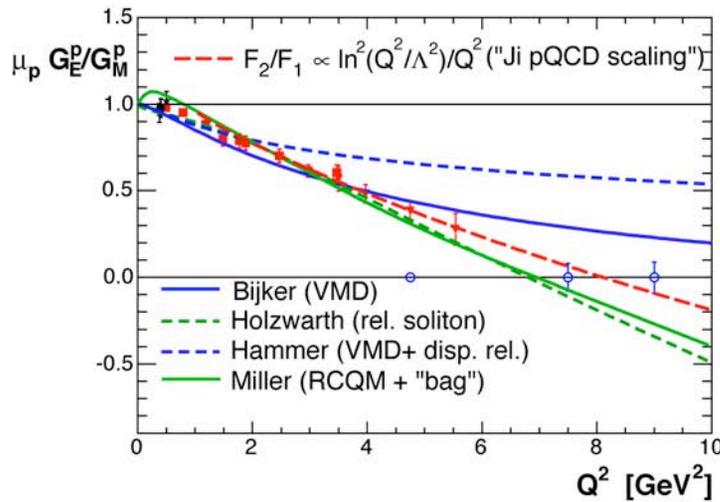


Nucleon Form Factors

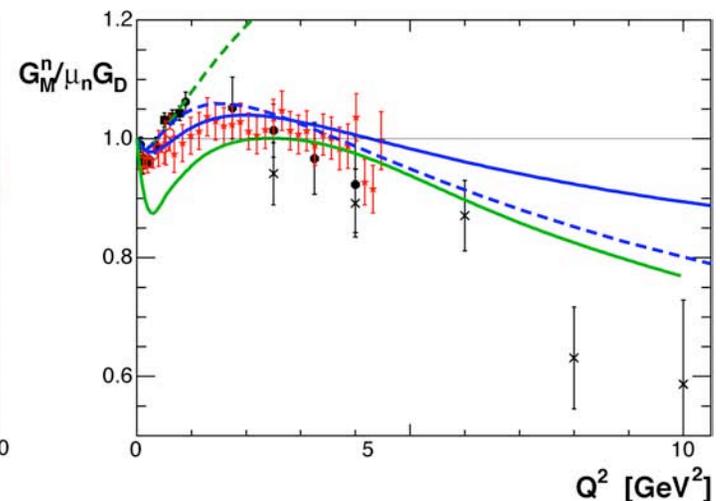
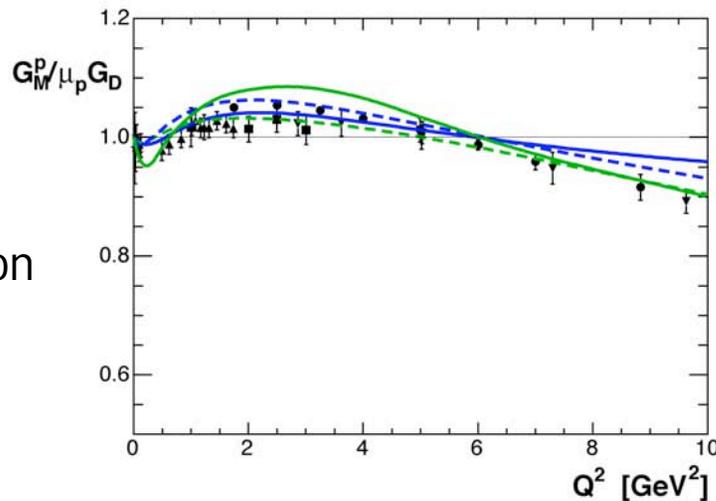
proton

neutron

charge

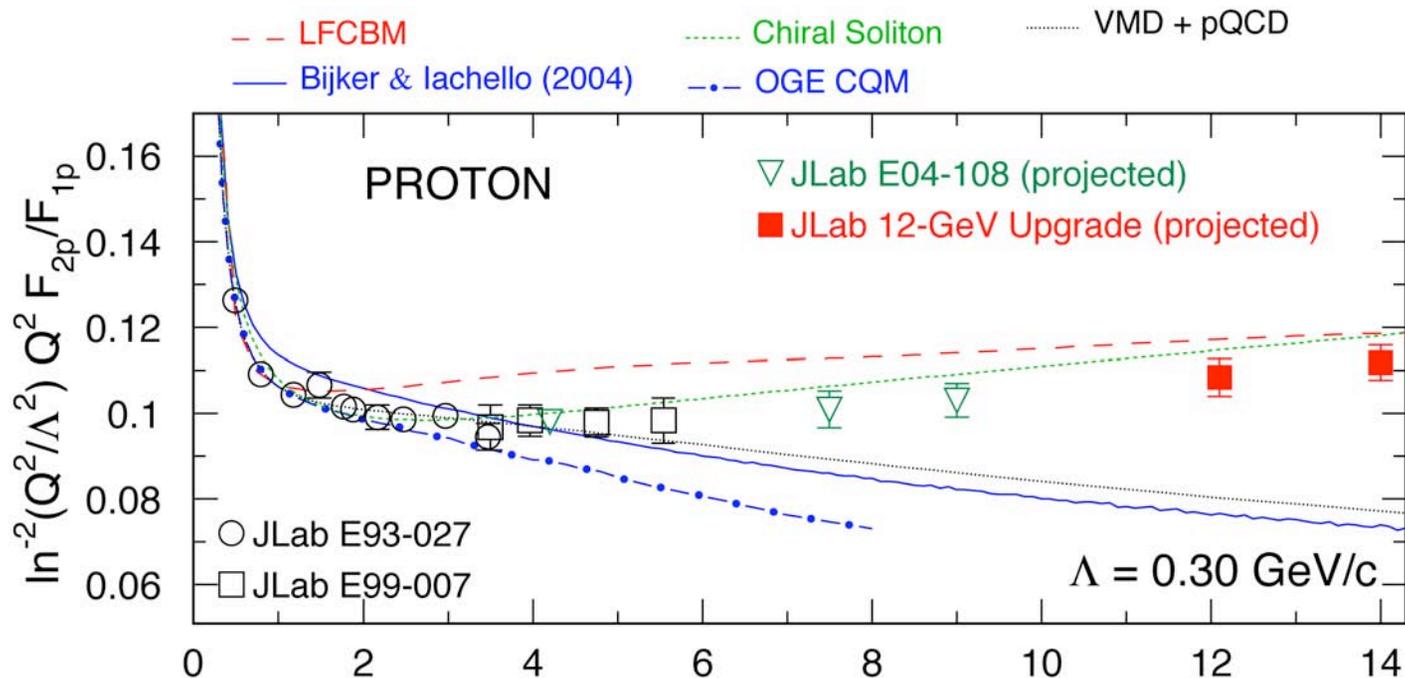


magnetization



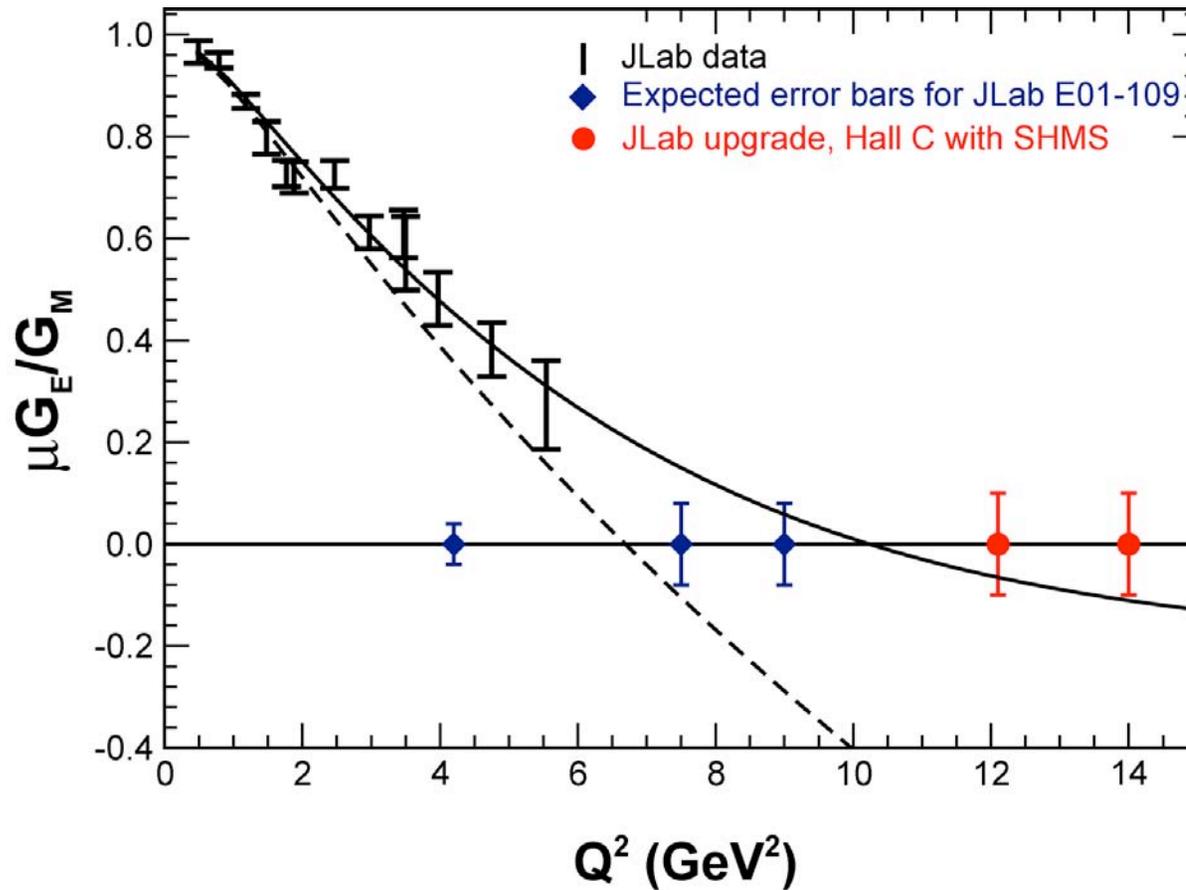
Proton Charge Form Factor @ 12GeV

Here shown as ratio of Pauli & Dirac Form Factors F_2 and F_1



Transverse quark momentum allows for a spin-flip amplitude, thus **orbital momentum** plays a role and $\ln^{-2}(Q^2/\Lambda^2) Q^2 F_2/F_1 \rightarrow \text{constant}$ (Ji)

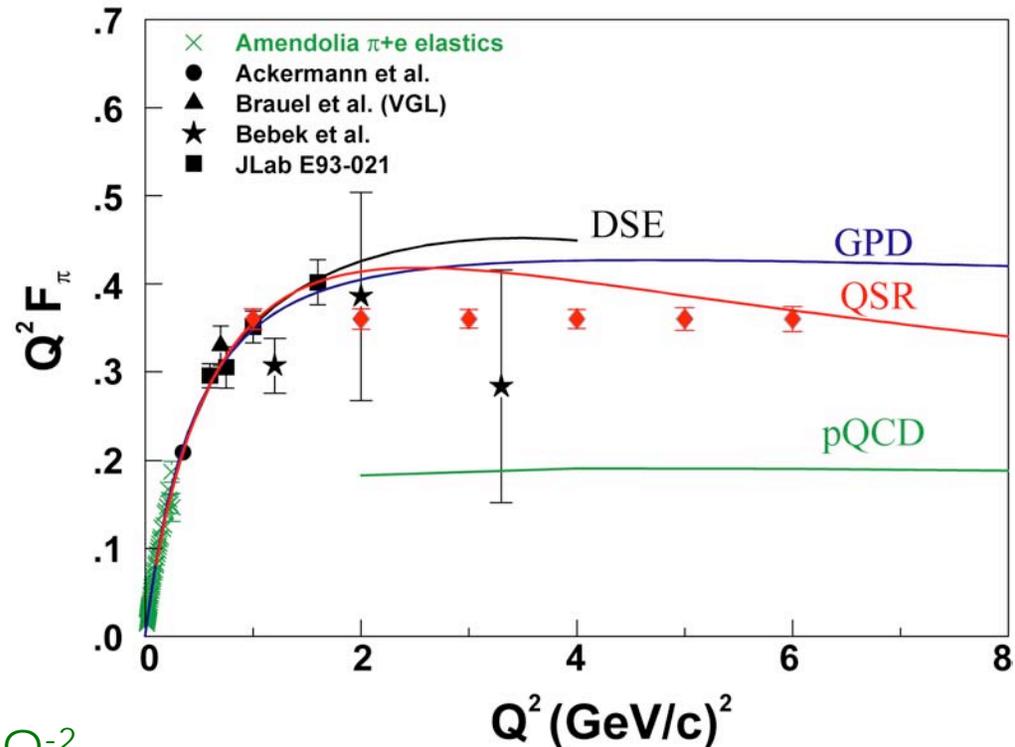
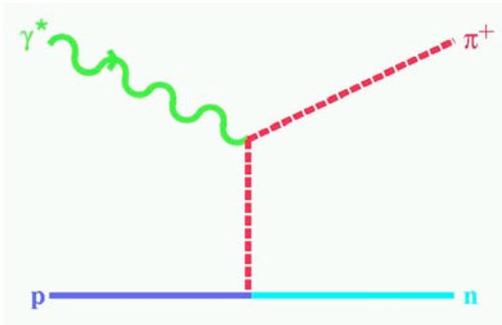
G_E^p with the 12 GeV upgrade



Charged Pion Electromagnetic Form Factor

Where does the dynamics of the q - q interaction make a transition from the strong QCD (confinement) to the pQCD regime?

- It will occur earliest in the simplest systems
 - ↳ the pion form factor $F_\pi(Q^2)$ provides a good starting system to determine the relevant distance scale experimentally



- In asymptotic region, $F_\pi \rightarrow 8\pi\alpha_s f_\pi Q^{-2}$
 HMS+SHMS (11 GeV) projection

Conclusion

- JLab at 12 GeV is a **unique** facility to determine the nucleon **large x quark distributions**.
- Semi-inclusive DIS will allow an unprecedented **flavor decomposition** for **valence** quarks at large x
- First quantitative insights into the effect of the **color E** and **B** fields in the nucleon structure by the measurement of d_2 and f_2 .
- **Proton** charge/magnetic (**coherent**) response will be explored at very short distances.
- Charged **Pion** (**coherent**) response will be investigated to link our understanding to the pQCD regime.

*This program will have a clear and comprehensive impact
on our understanding of
QCD within the first 5 years*