

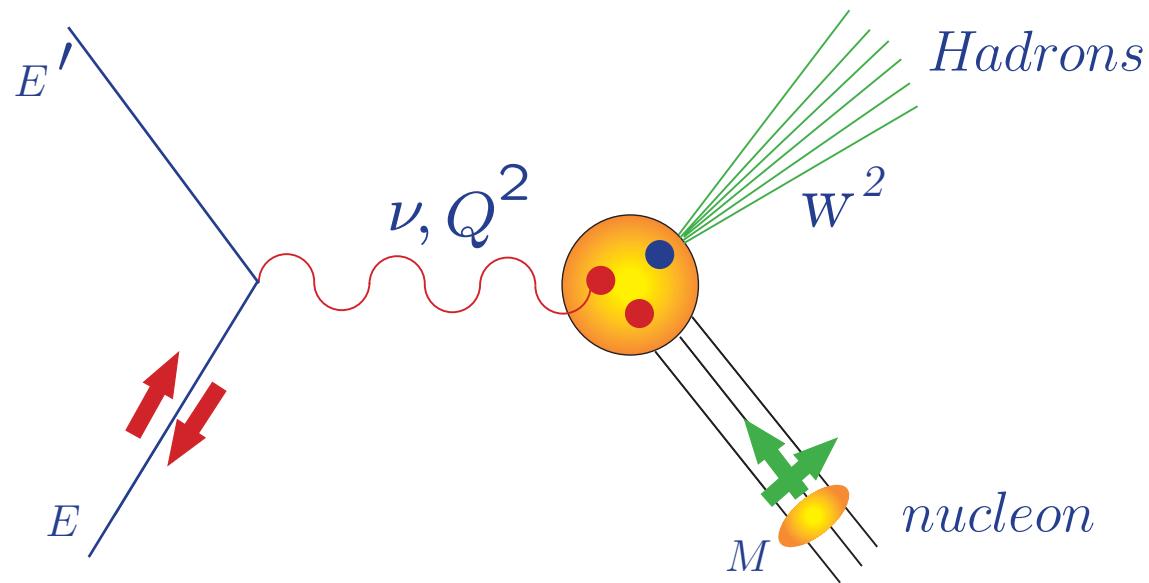
Precision Measurement of the Neutron Asymmetry A_1^n at Large x_{Bj} using CEBAF at 11 GeV

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Z.-E. Meziani (contact person), X. Ji

- Physics motivation.
- CEBAF uniqueness.
- Experimental procedure.
- Projected results.
- Summary.



Polarized Deep Inelastic Electron Scattering



$$x = \frac{Q^2}{2M\nu} \quad \text{Fraction of nucleon momentum carried by the struck quark}$$

Q^2 = 4-momentum transfer of the virtual photon, ν = energy transfer, θ = scattering angle

- All information about the nucleon vertex is contained in F_2 and F_1 the unpolarized (spin averaged) structure functions, and g_1 and g_2 the spin dependent structure functions

Quark-Parton Model

In the Bjorken scaling limit

$$F_1(x) = \frac{1}{2} \sum_i e_i^2 f_i(x) \quad g_1(x) = \frac{1}{2} \sum_i e_i^2 q_i(x)$$

$$f_i(x) = q_{\dot{i}}(x) + q_{\bar{i}}(x)$$

$$q_i(x) = q_{\dot{i}}(x) - q_{\bar{i}}(x)$$

$q_i(x)$ quark momentum distributions of flavor i

() parallel (antiparallel) to the nucleon spin

Observables of interest

$$A_1(x) = \frac{g_1(x)}{F_1(x)} = \frac{q_i(x)}{f_i(x)}$$

$$R^{np}(x) = \frac{F_2^n(x)}{F_2^p(x)}$$

Photon-Nucleon Asymmetry

Parallel Asymmetry

$$\frac{\sigma_{\uparrow\downarrow} - \sigma_{\uparrow\uparrow}}{\sigma_{\uparrow\downarrow} + \sigma_{\uparrow\uparrow}} = A_{//} = D (A_1 + \eta A_2)$$

Perpendicular Asymmetry

$$\frac{\sigma_{\uparrow\leftarrow} - \sigma_{\downarrow\leftarrow}}{\sigma_{\uparrow\leftarrow} + \sigma_{\downarrow\leftarrow}} = A_{\perp} = d (A_2 - \zeta A_1)$$

Kinematics Factors

$$D = (1 - E' \varepsilon / E) / (1 + \varepsilon R), \quad R(x, Q^2) = \sigma_T / \sigma_L$$

$$d = D \sqrt{2\varepsilon / (1 + \varepsilon)}$$

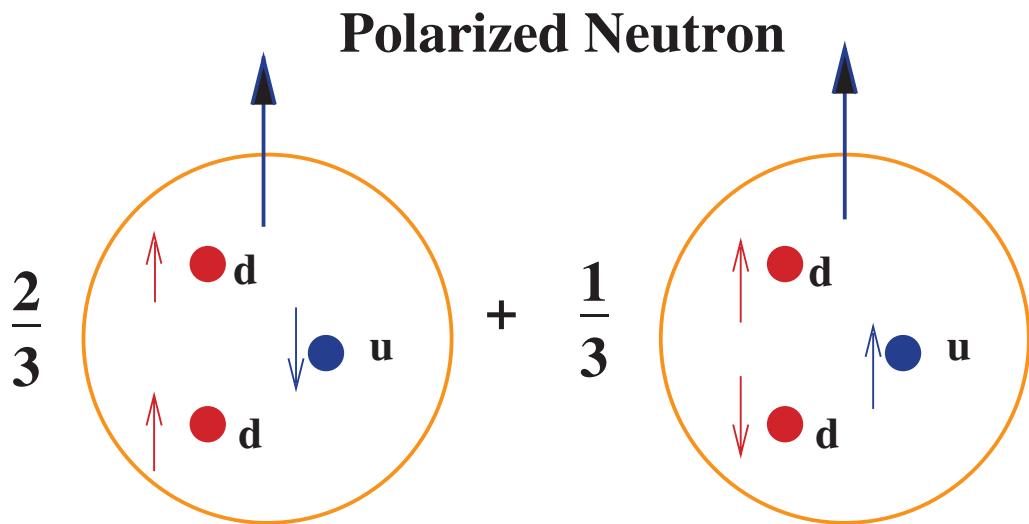
$$\eta = \varepsilon \sqrt{Q^2} / (E - E' \varepsilon)$$

$$\zeta = \eta (1 + \varepsilon) / 2\varepsilon$$



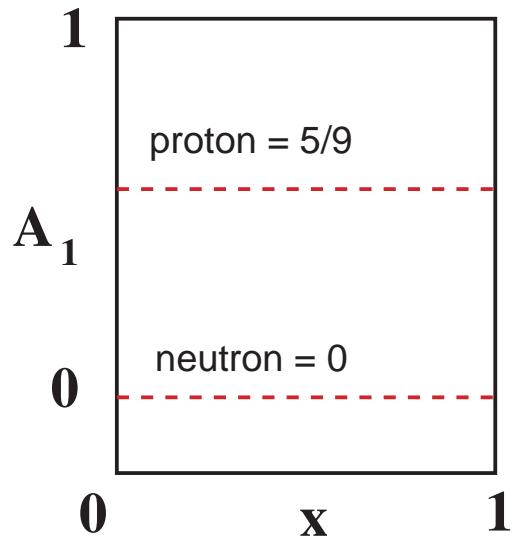
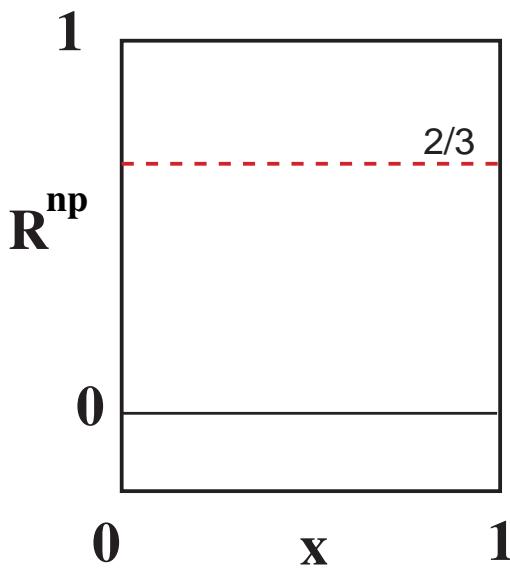
SU(6) Predictions

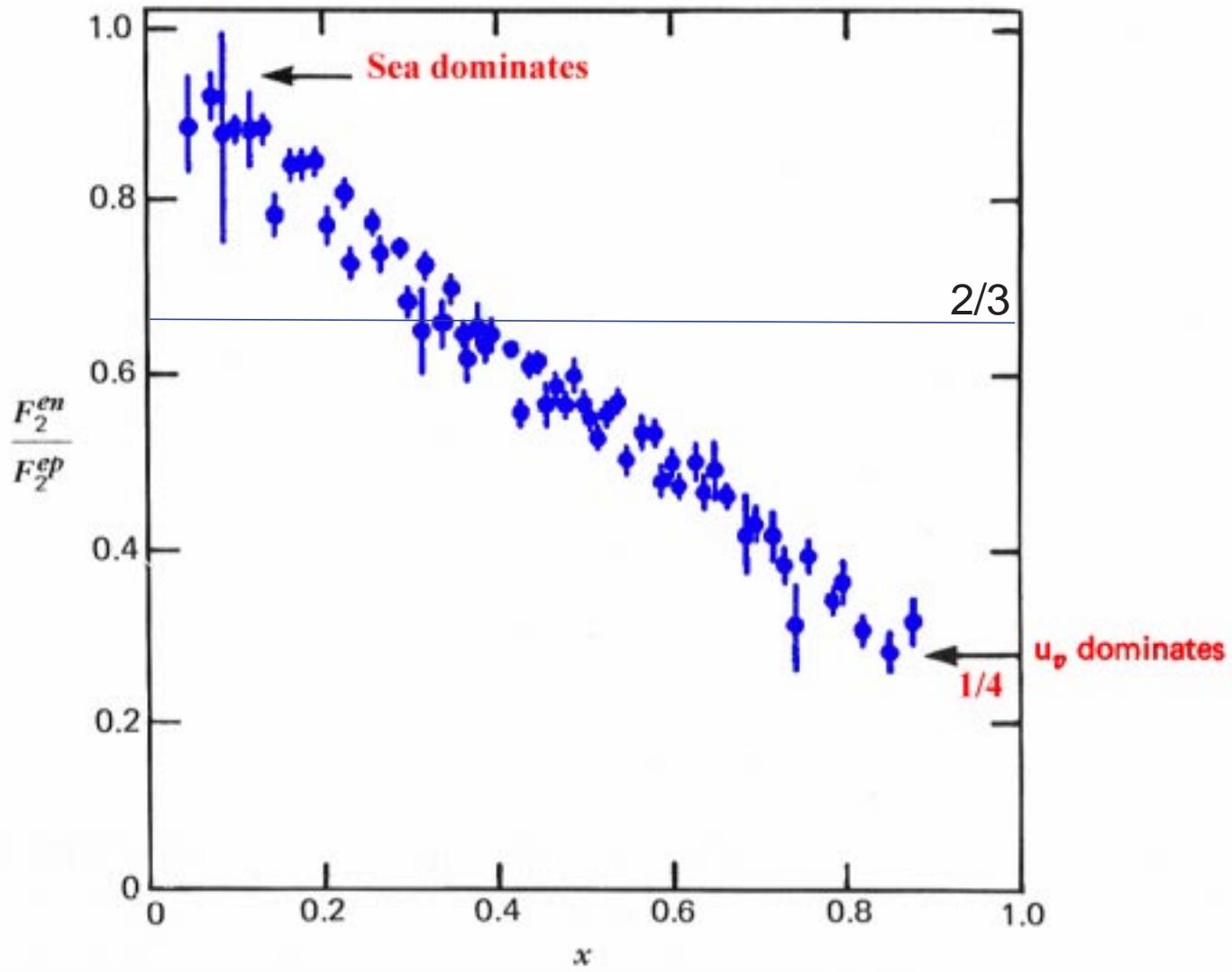
Polarized Neutron Static Wave Function in SU(6)



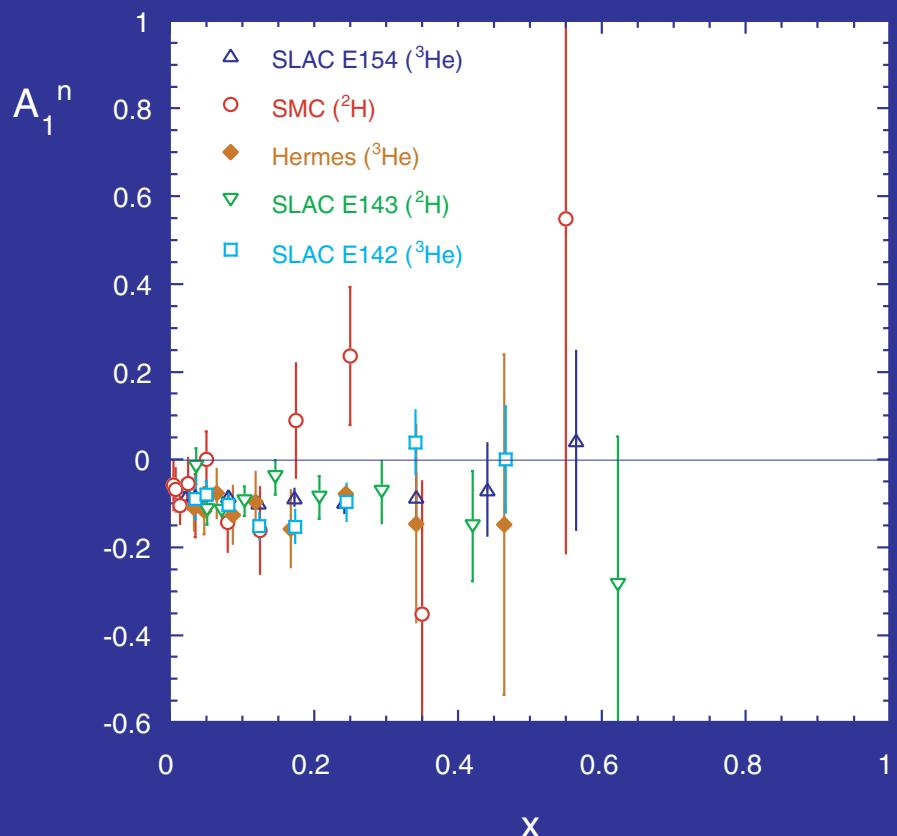
S=0 and **S=1** components of the wave function are equiprobable leading to the following predictions

$$R^{np} = 2/3, \quad A_1^p = 5/9, \quad A_1^n = 0$$

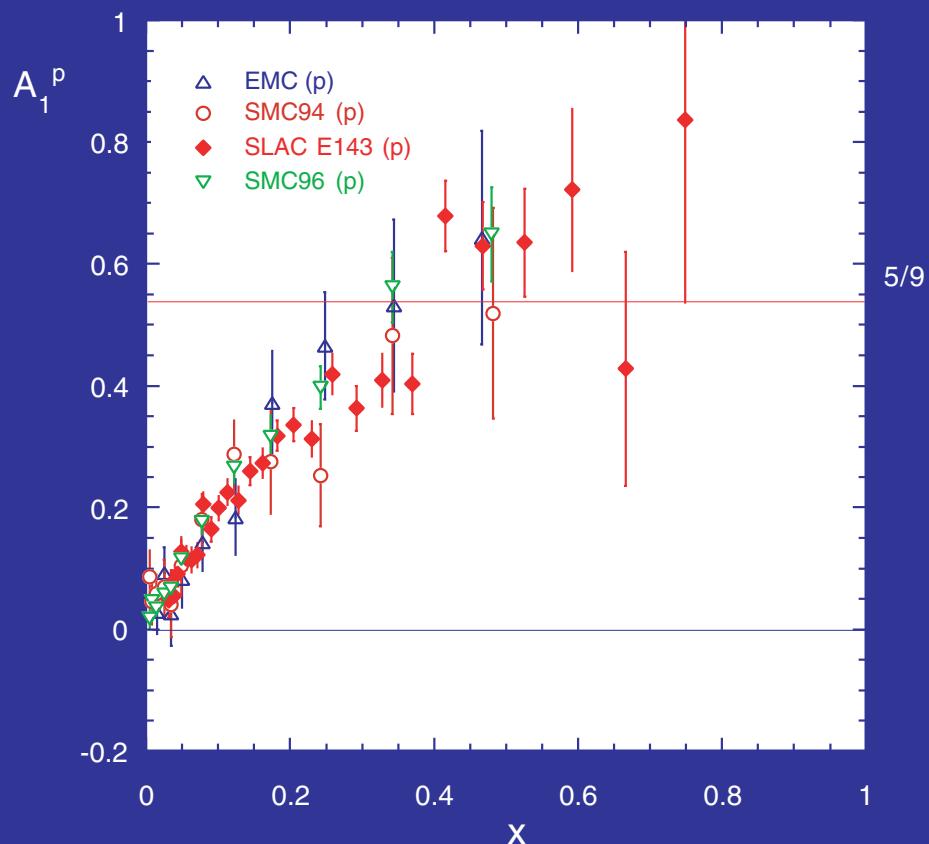




Neutron



Proton



Broken SU(6) Predictions

- Low x region : Dominated by sea quarks .
Quantitative predictions are difficult.
- High x region: Dominated by valence quarks.
Predictions are possible.

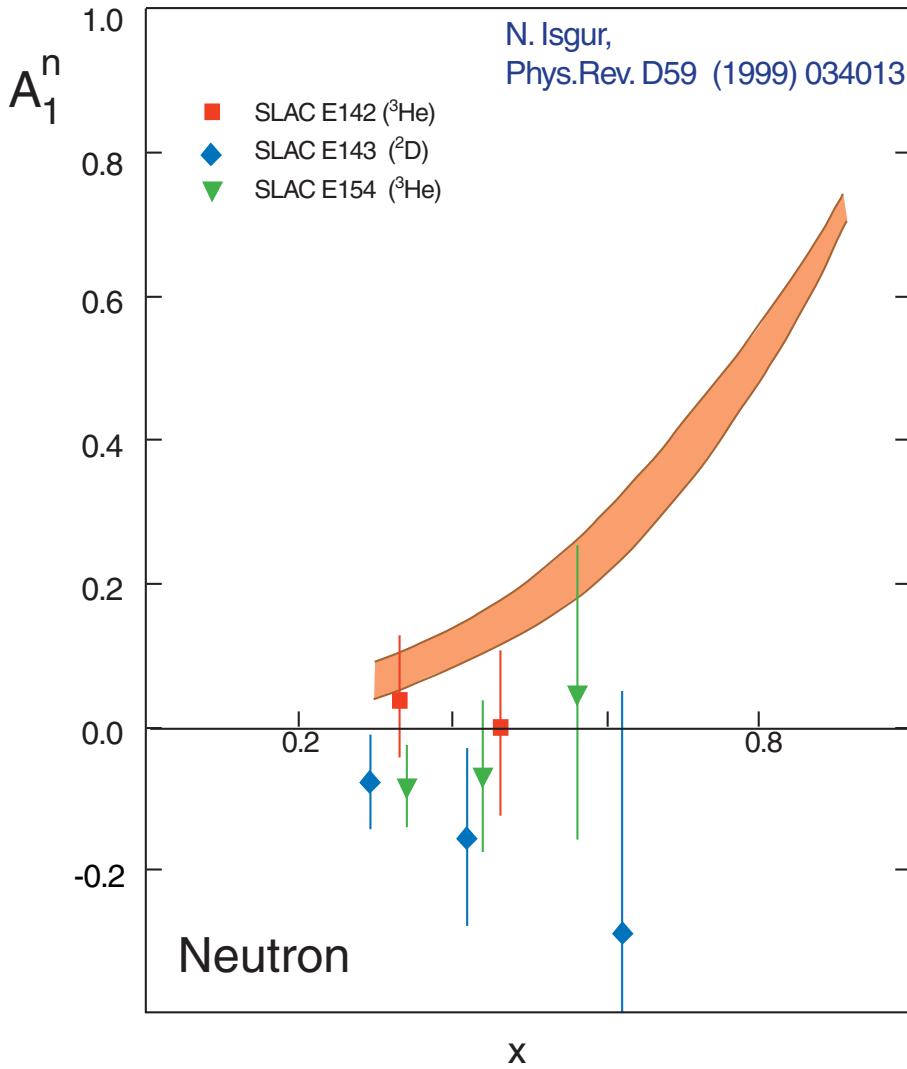
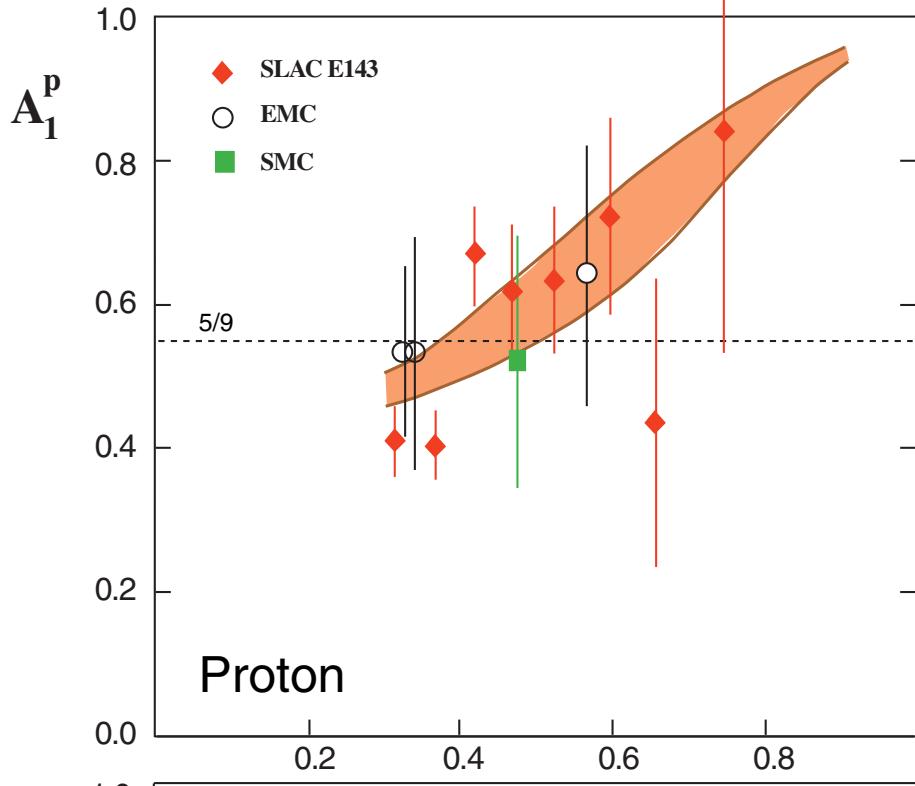
$$\begin{aligned} |n \uparrow\rangle = & \frac{1}{\sqrt{2}} |d \uparrow (du)_{S=0}\rangle + \frac{1}{\sqrt{18}} |d \uparrow (ud)_{S=1}\rangle \\ & - \frac{1}{3} |d \downarrow (ud)_{S=1}\rangle - \frac{1}{3} |u \uparrow (dd)_{S=1}\rangle \\ & - \frac{\sqrt{2}}{3} |u \downarrow (dd)_{S=1}\rangle \end{aligned}$$

SU(6) symmetry breaks:

- $R^{np} \rightarrow 1/4$ as $x \rightarrow 1$.
 - $\vec{S}_i \cdot \vec{S}_j \delta^3(\vec{r}_{ij})$ interaction (N - Δ mass splitting, etc...)
- Both  $|d \uparrow (du)_{S=0}\rangle$ dominates.

What about $A_1^{n,p}$?

Recent paper by N. Isgur

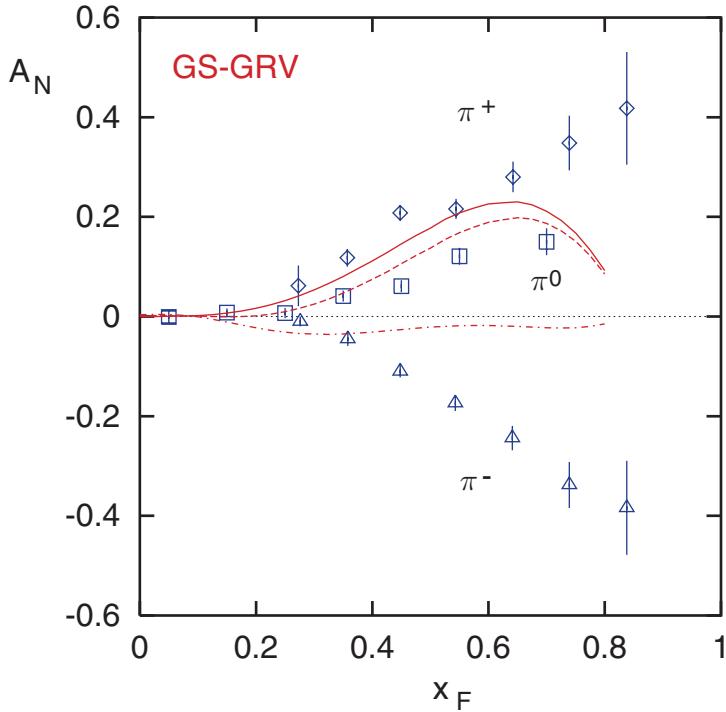


Single-Spin Semi-Inclusive Pion Production Asymmetries: $p\uparrow p \rightarrow \pi X$

Data are from Fermilab E704 experiment:

D. L. Adams *et al.*, *Phys. Lett.* **B264** (1991); *Phys. Rev. Lett.* **77** (1996) 2626

Calculations are by M. Boglione and E. Leader
Phys. Rev. **D61** (2000) 114001

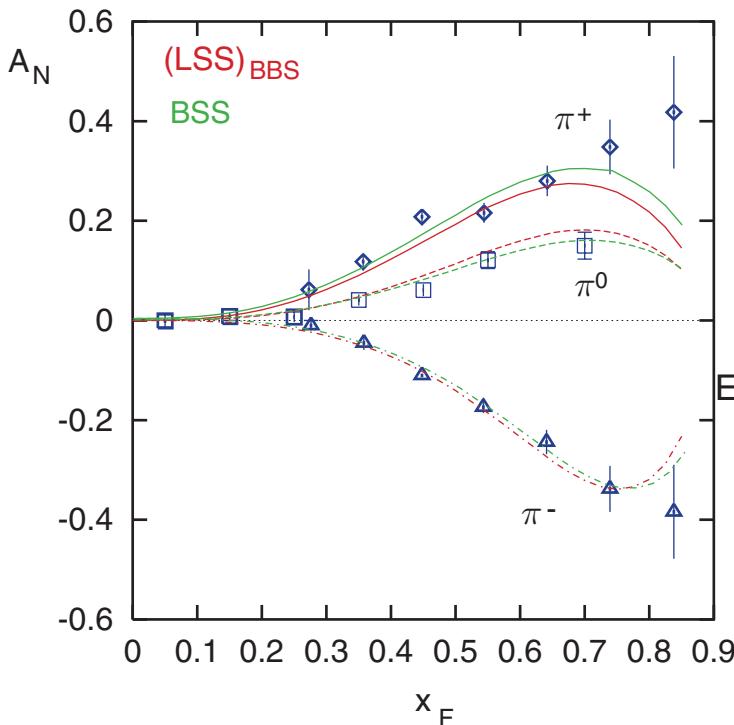


Soffer Bound

$$|\Delta_T q(x)| \leq \frac{1}{2}[q(x) + \Delta q(x)]$$

pQCD

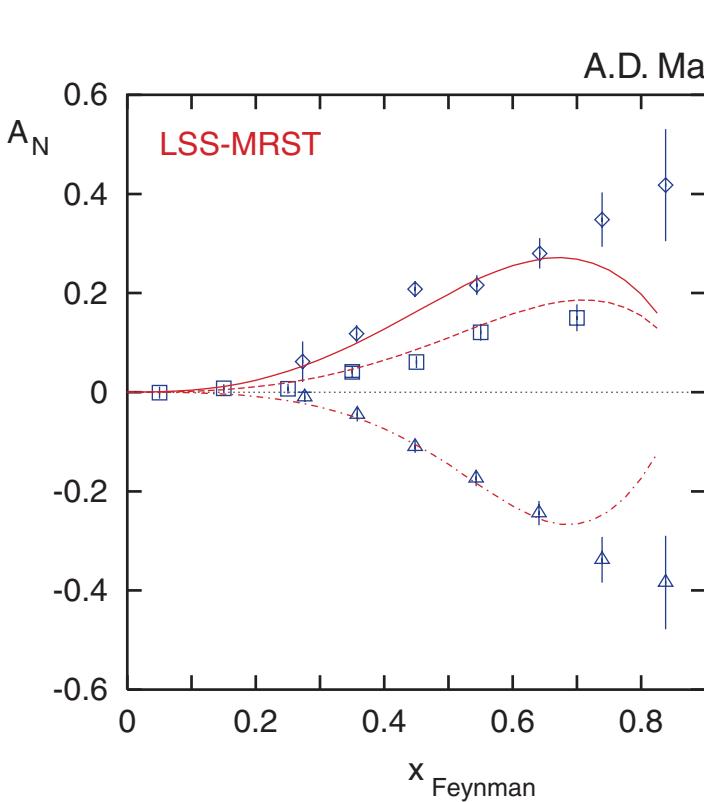
$$\frac{\Delta q(x)}{q(x)} \rightarrow 1$$



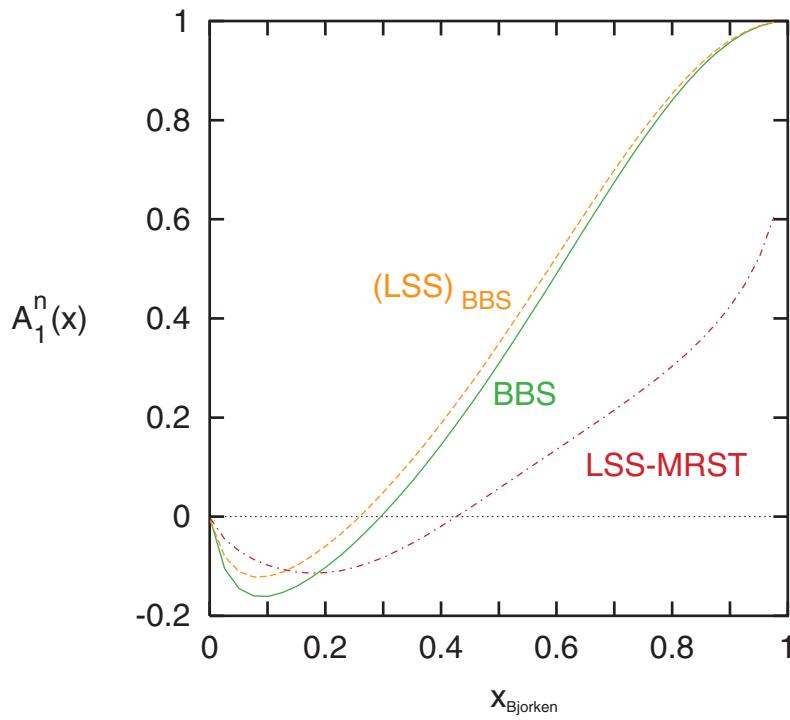
GS-GRV
T. Gehrmann and W. J. Stirling
Phys. Rev. **D53** (1996) 6100,
and

M. Glück, E. Reya and W. Vogelsang
Z. Phys. **C67** (1995) 433.

LSS-BSS
E. Leader, A. V. Sidorov, and D. B. Stamenov
Int. J. Mod. Phys. **A13**, No.32, (1998) 5573
and
S. Brodsky, M. Burkhardt and I. Schmidt,
Nucl. Phys. **B441** (1995) 197.



Predictions for the Neutron Asymmetry A_1^n



Physics Overview as $x \rightarrow 1$

Diquark Spin State	F^n_2/F^p_2	A^p_1	A^n_1
S=1 and S=0 equiprobable: SU(6)	2/3	5/9	0
	$d/u=1/2$	$\frac{u}{u} \rightarrow 2/3$	$\frac{d}{d} \rightarrow -1/3$
S=1 suppressed, S=0 retained F. Close, Phys. Lett. 43B (1973) 422. F. Close, An introduction to Quarks and Partons (1979).	1/4	+1	+1
	$d/u=0$	$\frac{u}{u} \rightarrow 1$	$\frac{d}{d} \rightarrow -1/3$
S = 1, $S_z = 1$ suppressed			
S = 1, $S_z = 0$ and S = 0 retained G. Farrar, D. Jackson, Phys. Rev. Lett. 35(1975)1416 G. Farrar, Phys. Lett. 70B (1977)34	3/7	+1	+1
	$d/u=1/5$	$\frac{u}{u} \rightarrow 1$	$\frac{d}{d} \rightarrow 1$

Instantons!

~0

N. Kochelev, hep-ph/9711226

SUMMARY

- In most approaches A_1^n large and positive as x becomes large ($x > 0.3$)
- At present all data are consistent with $A_1^n(x) \leq 0$
- If A_1^n stays negative the constituent quark picture is in jeopardy! New degrees of freedom might need to be considered, for example, Instantons??

**This has been an important question
for 25 years!**

Experiment is believed to be possible with

- An intense polarized \vec{e} beam
- A dense polarized ${}^3\vec{H}e$ target
- A beam energy $E > 6 GeV$, a MAD spectrometer, etc...

**CEBAF at 11GeV is by far the best facility
to measure A_1^n at high x**

Proposed Measurements

Measure $A_{//}^{^3\text{He}}$ & $A_{\perp}^{^3\text{He}}$

- 3 incident energies: $E_i = 6.6, 8.8$ and 11GeV
- 3 scattering angles: $\theta = 35^\circ, 27^\circ$ and 25°
- 3 **MAD** momentum settings covering the range:

$$0.1 < x < 0.75$$

$$2.0 < Q^2 < 10 \text{ GeV}^2$$

$$W^2 \geq 4 \text{ GeV}^2$$

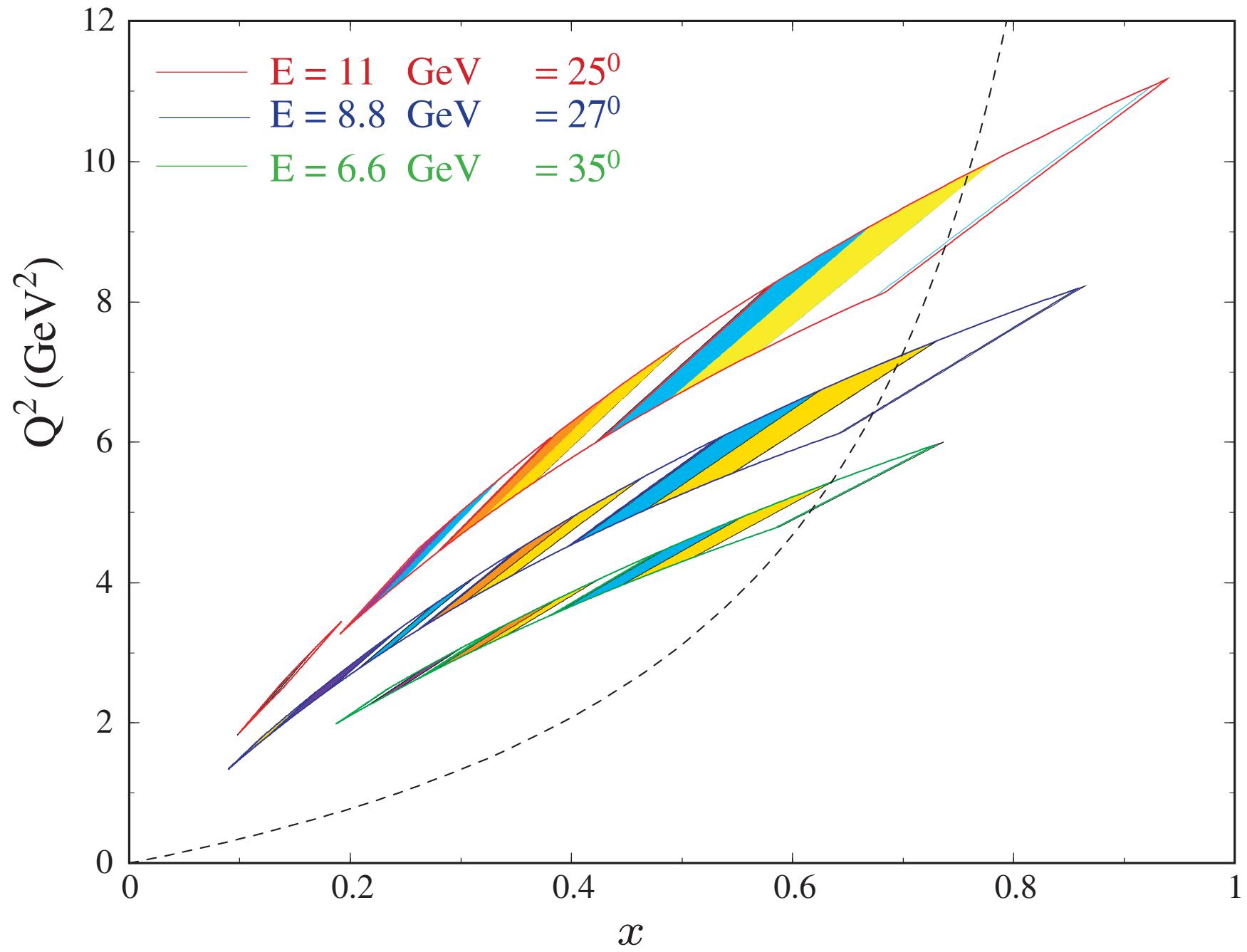
- Perform radiative corrections on $A_{//}^{^3\text{He}}$ & $A_{\perp}^{^3\text{He}}$
- Determine $A_1^{^3\text{He}} = (A_{//}/D - \eta A_{\perp}/d)/(1+\eta\zeta)$
- Correct for nuclear effects to extract $A_1^n(x, Q^2)$

Uniqueness of CEBAF

- Depolarization factor typically about 0.7 compared to 0.3 in most experiments performed at the high energy facilities ($A_1 \approx A_{\parallel}/D$).
- Scattered electrons detected at large angle lead to high x , high Q^2 and low scattered energy ($E' < 6$ GeV). A large acceptance spectrometer like **MAD** matches the kinematics efficiently.
- High beam and target polarizations and high beam current provide for a good polarized luminosity.
- Target reconstruction reduces entrance and exit windows background thus, dilution of the asymmetry.



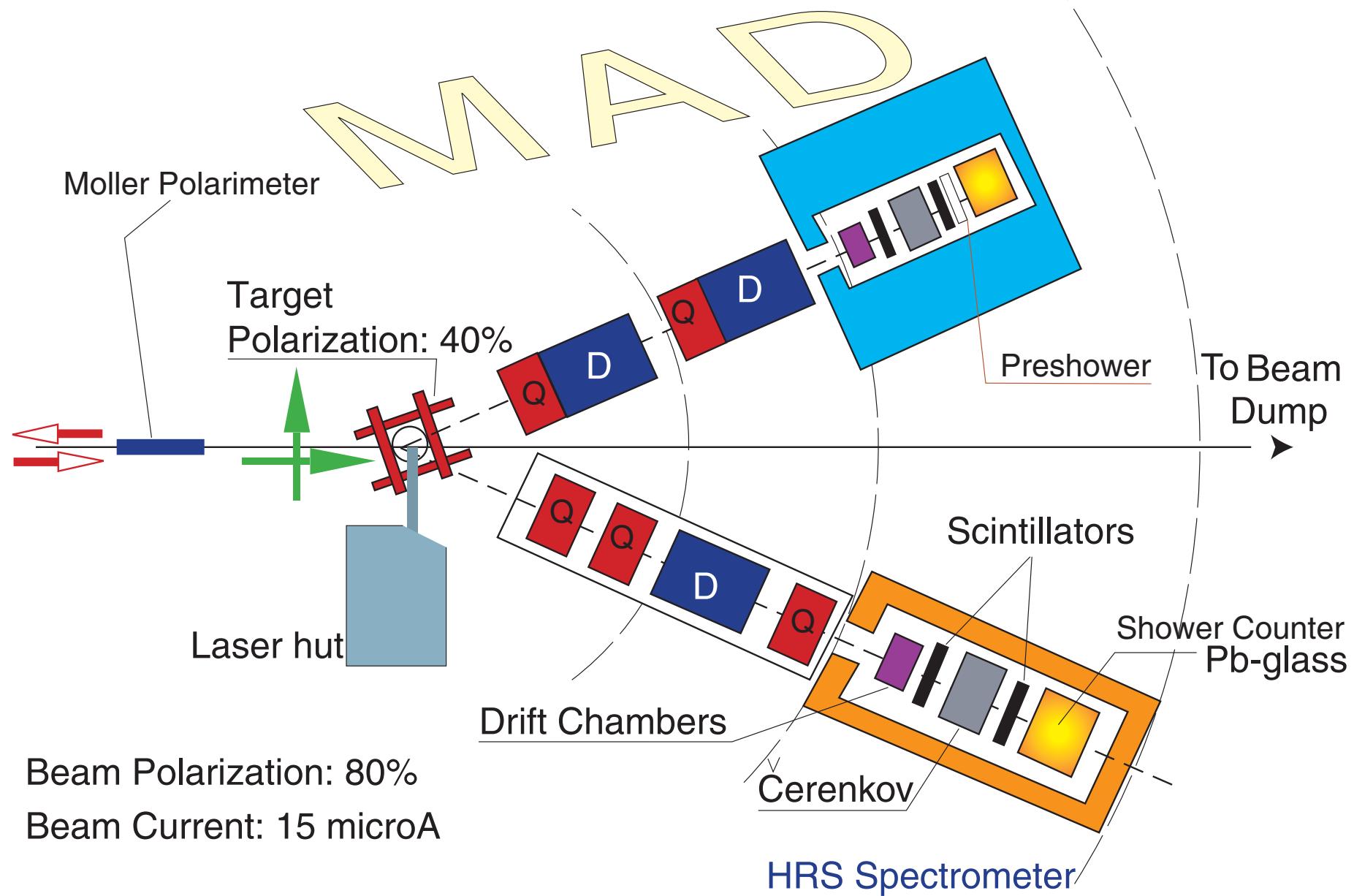
Kinematic Coverage for an A_1^n measurement using MAD



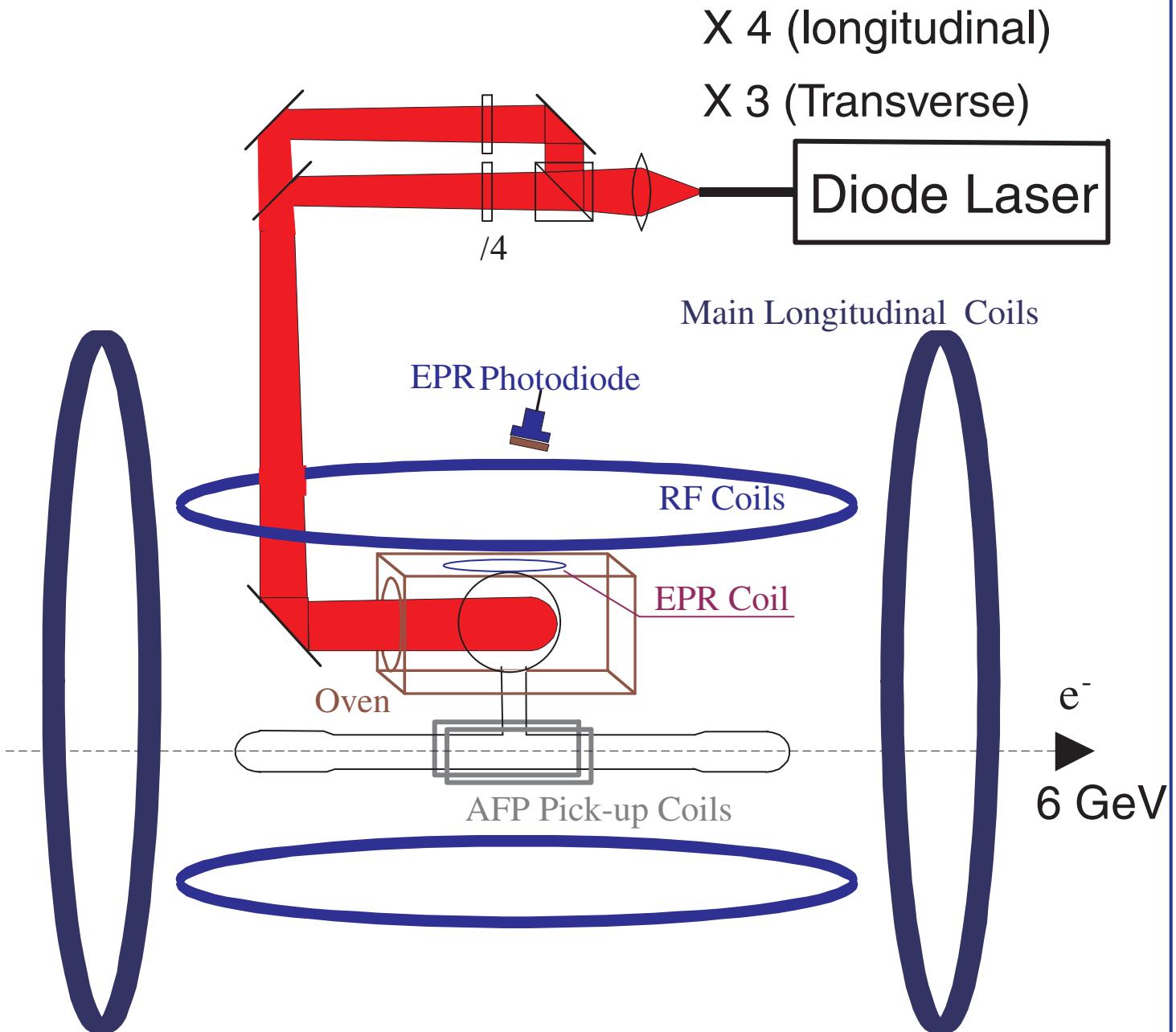
Comparison of some relevant parameters between CERN, HERA, SLAC and CEBAF. Note the difference in the **D factor** and size of the **x bin**.

Expt. Name	E_i <i>GeV</i>	E' <i>GeV</i>	θ <i>deg</i>	x bin	Q^2 <i>GeV</i> ²	D	$P_{e,\mu}$	Rate (Hz)
HERMES	35	17.0	5.2	0.6-0.7	9.1	0.22	0.50	0.05
SLAC E142	23	16.5	7.0	0.4-0.6	5.2	0.27	0.35	7.0
SLAC E143	29	25.5	7.0	0.6-0.7	9.1	0.29	0.84	0.3
SMC	190	161	1.8	0.4-0.7	29.5	0.14	0.80	0.005
CEBAF	11	4.4	25	0.7-0.75	10	0.67	0.80	1.3

Hall A Floor Configuration with MAD

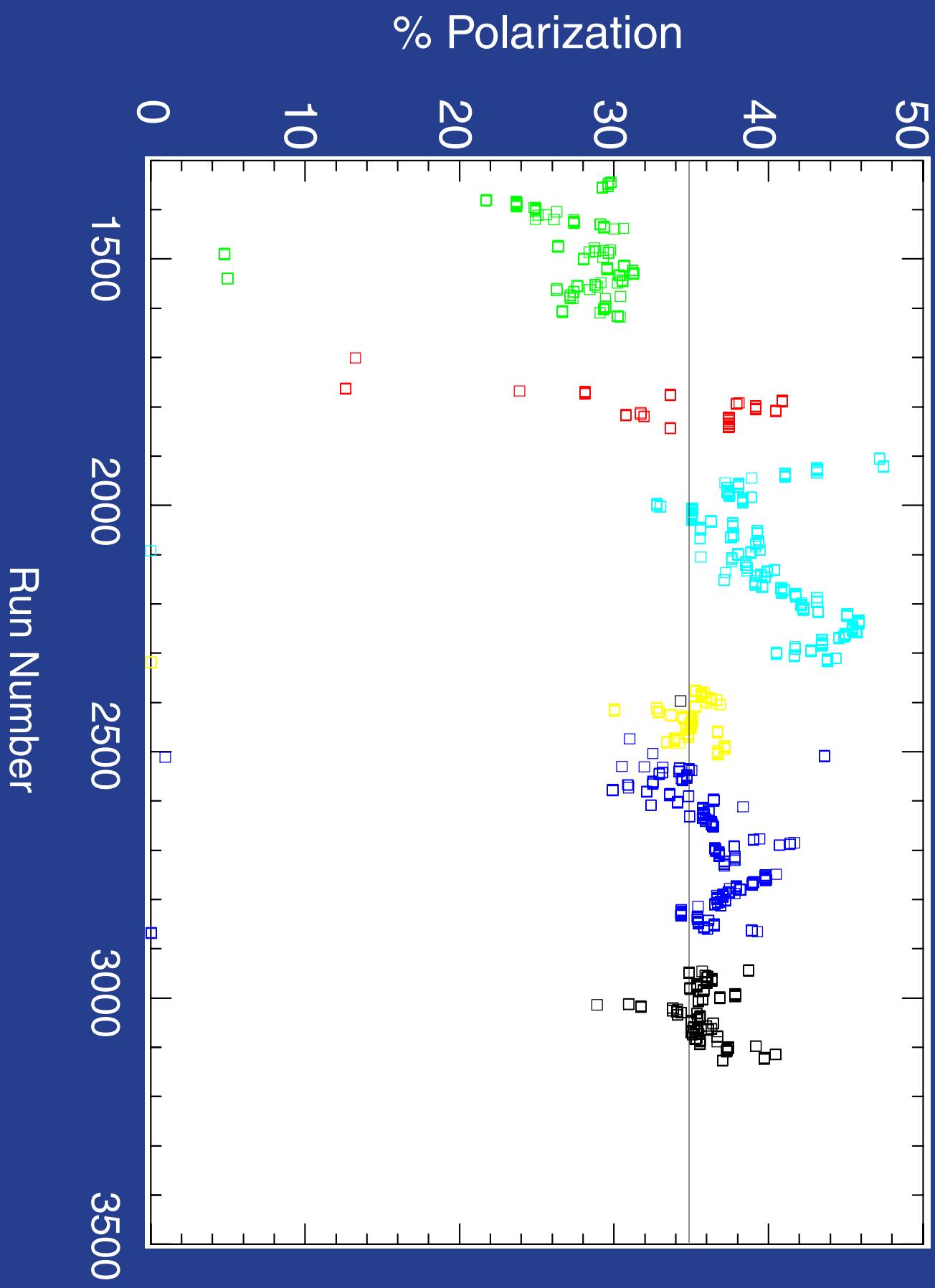


Jlab Hall A polarized ^3He Target



- NMR and EPR techniques for polarization monitoring.
- Elastic scattering for current induced depolarization.
- Target used successfully in E94-010 and E95-001.
- Target length will be 25 cm.

E94-010 ${}^3\text{He}$ Target Polarization



From ^3He to the Neutron

- Extract an effective \tilde{A}_1^n
 - Wave function includes S, S' and D waves.
 - Fermi motion not included.
 - binding effects not included

$$\tilde{A}_1^n = \frac{1}{f_n \rho_n} (A_1 - 2 f_p \rho_p A_1) \quad \text{where}$$

$$f_{p(n)} = \frac{F_2^n}{F_2^{^3\text{He}}} \quad \& \quad \rho_p = -2\Delta' = -2.7 \pm 0.3\% \\ \rho_n = 1 - 2\Delta = 87 \pm 2\%$$

$$\Delta = (\rho_{S'} + 2 \rho_D)/3 \quad \rho_{S'} = 1.55 \pm 2\% \\ \Delta' = (\rho_D - \rho_{S'})/6 \quad \rho_D = 9.1 \pm 0.9\%$$

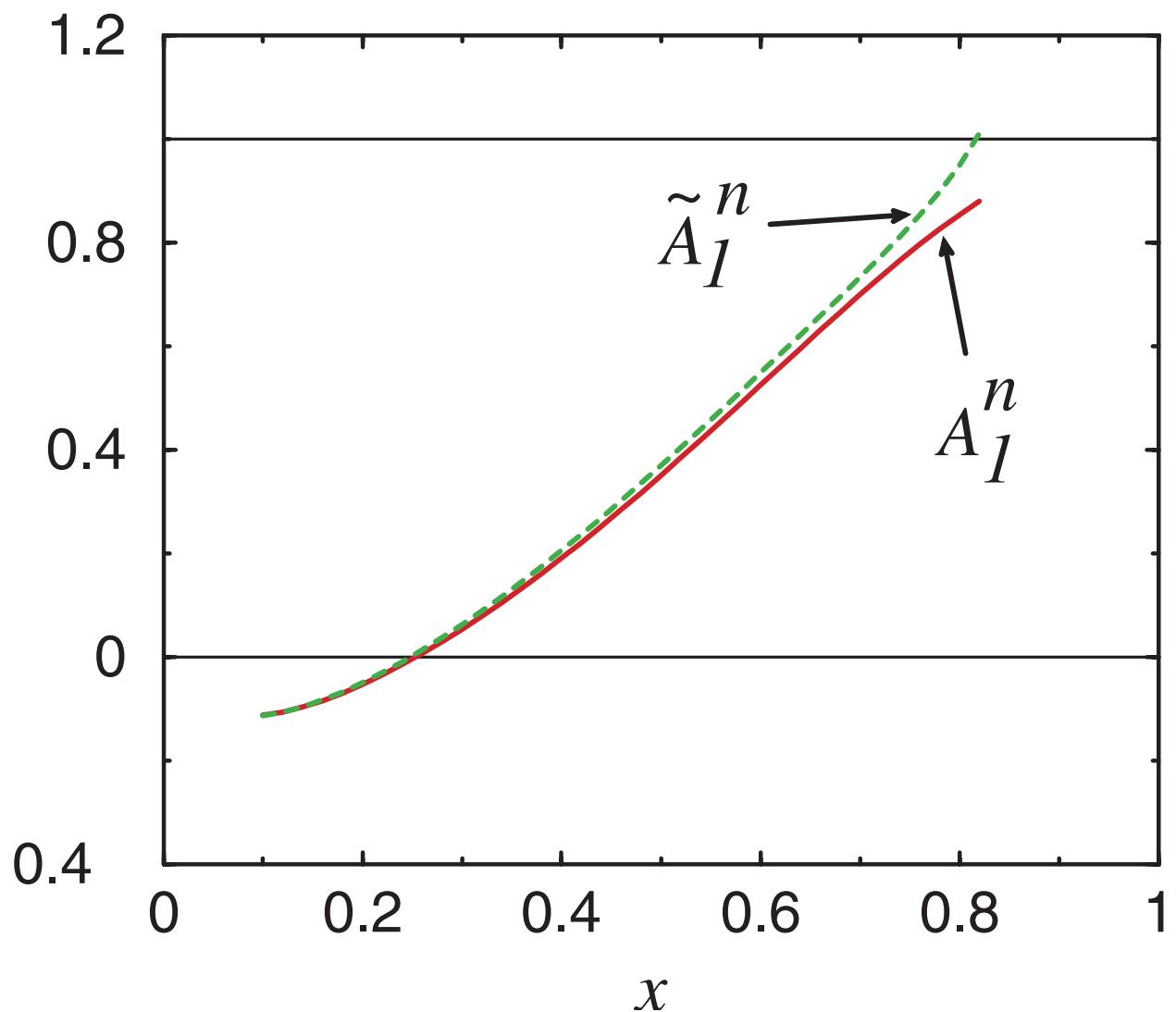
Very good approximation according to

C. Cioffi Degli Atti, S. Scopetta, E. Pace and G. Salme *University of Perugia report DFUPG 75/92.*

R. W. Shulze and P.U. Sauer, Phys. Rev. C48(1993)38.

W. Melnitchouk et al., Private communication

Residual of Nuclear corrections to extract the Neutron from ${}^3\text{He}$



W. Melnitchouk *et al.*, *private communication*

Rates and Times for parallel and perpendicular measurements which optimize the statistical uncertainty on A_{\perp}^n

$E_j = 11 \text{ GeV}$ $\theta = 25^\circ$

E' (GeV)	x	Q^2 (GeV) ²	W (GeV)	D	$A_1^{^3He}$	$\Delta A_1^{^3He}$	$A_2^{^3He}$	$\Delta A_2^{^3He}$	Rate Hz	time Hours	time _⊥ Hours
4.40	.732	9.07	2.05	0.67	0.072	0.0046	0.0330	0.0159	1.26	540	22
3.98	.623	8.20	2.42	0.71	0.050	0.0041	0.0205	0.0155	2.69	252	10
3.60	.534	7.42	2.71	0.75	0.036	0.0036	0.0132	0.0153	4.21	161	6
3.26	.463	6.72	2.95	0.78	0.022	0.0033	0.0075	0.0152	5.56	122	4.9
2.95	.403	6.08	3.15	0.81	0.010	0.0030	0.0031	0.0152	6.66	102	4.1
2.67	.352	5.50	3.32	0.83	0.000	0.0028	-0.0001	0.0153	7.47	91	3.6
2.40	.307	4.95	3.47	0.86	-0.009	0.0027	-0.0024	0.0154	8.06	84	3.3
2.20	.275	4.53	3.59	0.87	-0.015	0.0026	-0.0037	0.0156	8.38	81	3.2
2.00	.244	4.12	3.69	0.89	-0.020	0.0025	-0.0045	0.0159	8.58	79	3.2
1.85	.214	3.78	4.03	0.93	-0.028	0.0022	-0.0049	0.0175	8.56	79	3.2
1.70	.185	3.47	4.10	0.94	-0.028	0.0022	-0.0046	0.0182	8.41	81	3.2
1.50	.162	3.27	4.15	0.95	-0.028	0.0022	-0.0043	0.0187	8.28	82	3.3

Each color represents one momentum setting for MAD

$E' = 4.05 \text{ GeV}$

Each momentum bin in the table corresponds to:

$E' = 3.00 \text{ GeV}$

$\Delta\Theta = +/- 35 \text{ mrd}$

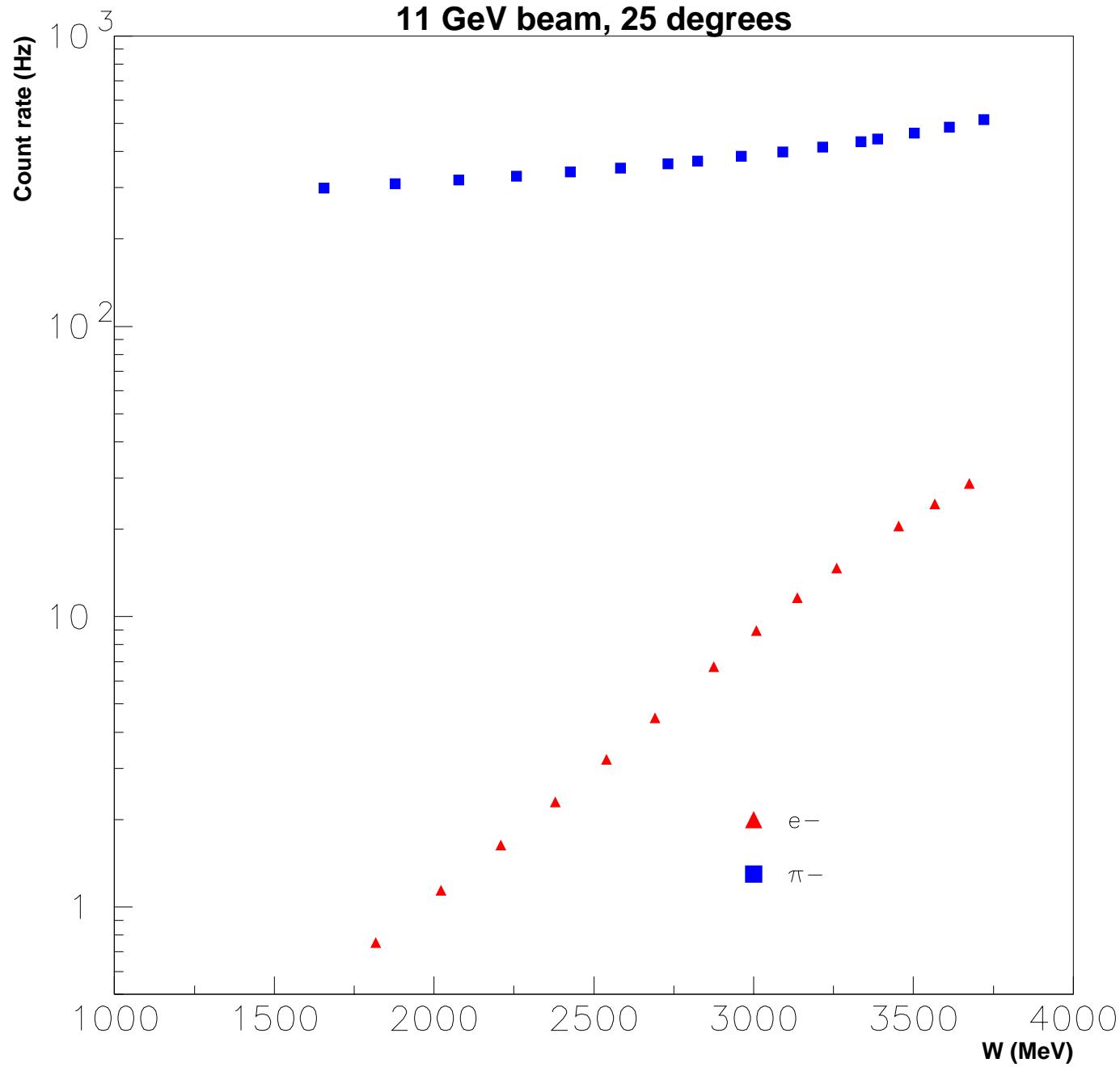
$E' = 2.20 \text{ GeV}$

$\Delta\Phi = +/- 150 \text{ mrd}$

$E' = 1.25 \text{ GeV}$

$\delta p/p = +/- 5\%$

11 GeV beam, 25 degrees



Total uncertainty of the neutron asymmetry A_1^n extracted from that of ${}^3\text{He}$

$E_i = 11 \text{ GeV}$

$\theta = 25^\circ$

E' (GeV)	x	Q^2 (GeV) ²	W (GeV)	D	$A_1^{{}^3\text{He}}$	$\Delta A_1^{{}^3\text{He}}$ (stat.)	$\Delta A_1^{{}^3\text{He}}$ (syst.)	$\Delta A_1^{{}^3\text{He}}$ (total)	A_1^n	ΔA_1^n (total)
4.40	.732	9.07	2.05	0.67	0.072	0.0046	0.0042	0.0062	0.561	0.048
3.98	.623	8.20	2.42	0.71	0.050	0.0041	0.0029	0.0050	0.415	0.040
3.60	.534	7.42	2.71	0.75	0.036	0.0036	0.0021	0.0042	0.294	0.033
3.26	.463	6.72	2.95	0.78	0.022	0.0033	0.0013	0.0035	0.196	0.028
2.95	.403	6.08	3.15	0.81	0.010	0.0030	0.0058	0.0031	0.115	0.024
2.67	.352	5.50	3.32	0.83	0.000	0.0028	0.0021	0.0028	0.053	0.022
2.40	.307	4.95	3.47	0.86	-0.009	0.0027	0.0005	0.0027	0.002	0.020
2.20	.275	4.53	3.59	0.87	-0.015	0.0026	0.0009	0.0027	-0.028	0.019
2.00	.244	4.12	3.69	0.89	-0.020	0.0025	0.0012	0.0027	-0.053	0.018
1.35	.154	2.78	4.03	0.93	-0.028	0.0022	0.0016	0.0028	-0.093	0.016
1.20	.135	2.47	4.10	0.94	-0.028	0.0022	0.0016	0.0027	-0.094	0.016
1.10	.122	2.27	4.15	0.95	-0.028	0.0022	0.0016	0.0027	-0.094	0.015

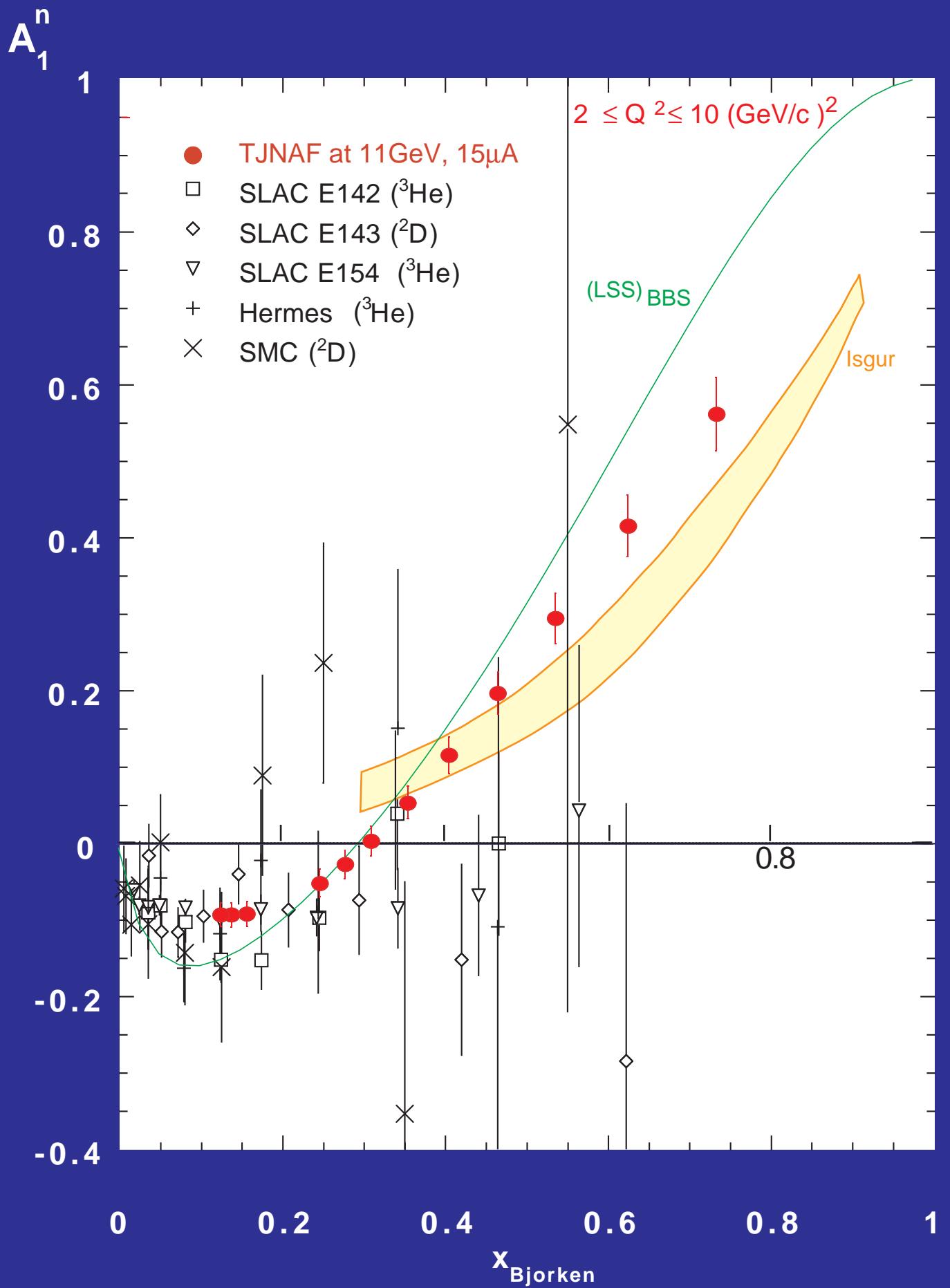
Each color corresponds to a different momentum setting of the MAD spectrometer.

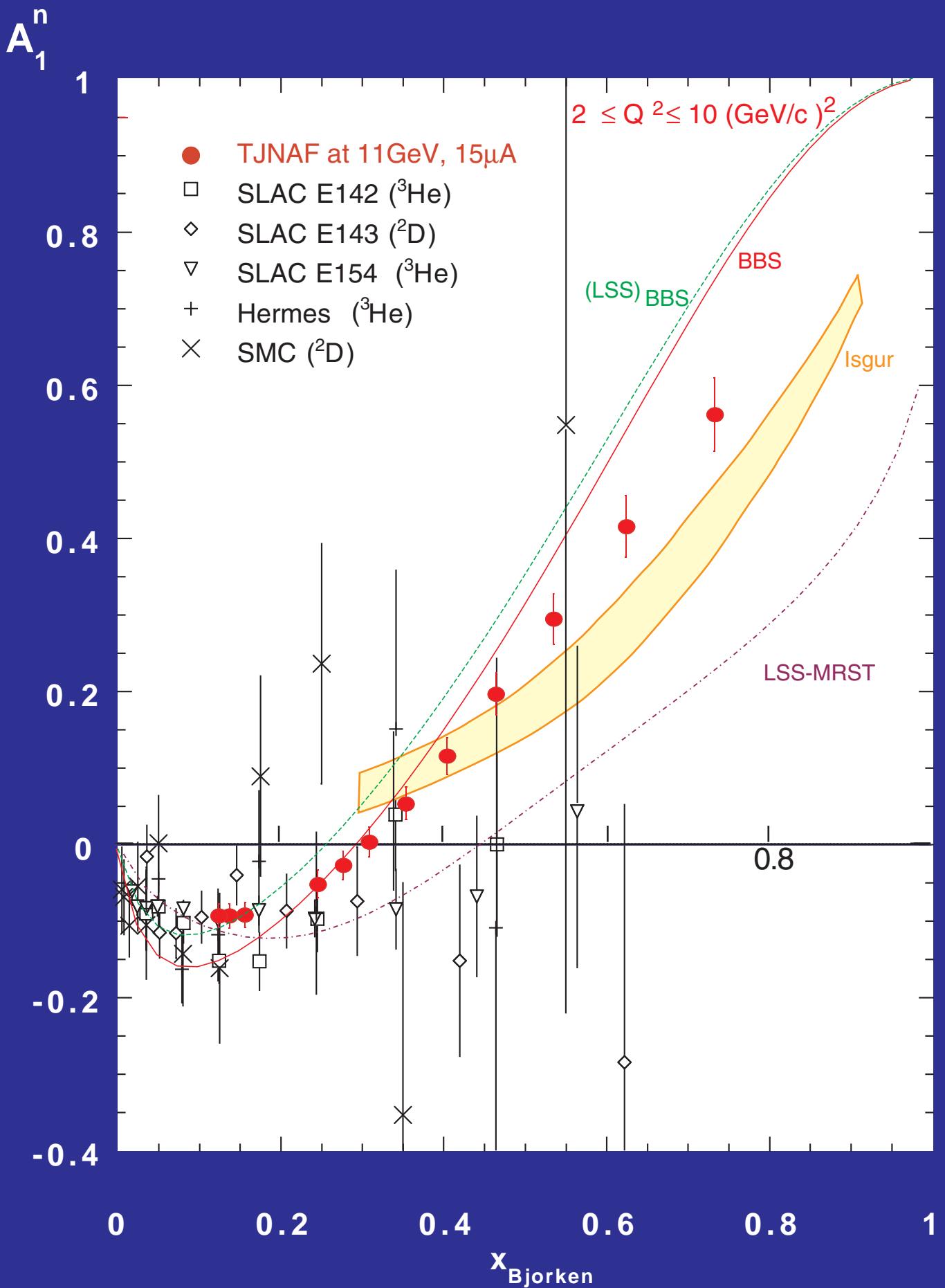
$E' = 4.05 \text{ GeV}$

$E' = 3.00 \text{ GeV}$

$E' = 2.20 \text{ GeV}$

$E' = 1.25 \text{ GeV}$





Conclusion

- Precision measurement of the deep inelastic asymmetry A_1^n in the region $0.10 \leq x < 0.75$ and $2 \leq Q^2 \leq 10 \text{ GeV}^2$
- 865 hours of beam on target for the 11 GeV beam energy measurement.
- A period of 2 months of beam on target should allow us to measure all energies incident beam energies leading to a Q^2 dependence and a W^2 dependence investigation.
- CEBAF at 11 GeV is the best place to perform this measurement. Further observables of great interest can be obtained at the same time. An example d_2^n , a quark-gluon correlation matrix element.



MEASURING g_2^n AT 11 GeV

- g_2 is one of the few clean places to measure higher twist effects which provide *direct* information about quark-gluon interactions.
- The leading twist contribution can be cleanly subtracted away using g_1 data.

$$g_2(x, Q^2) = -\frac{F_1(x, Q^2)}{D'} \frac{\nu}{2E \sin \theta} \left[\sin \theta A_{||} - \frac{E + E' \cos \theta}{E'} A_{\perp} \right]$$

$$d_2^n(Q^2) = 2 \int_0^1 x^2 \left[g_1^n(x, Q^2) + \frac{3}{2} g_2^n(x, Q^2) \right] dx$$

- d_2^n is a twist-3 matrix element which is uniquely sensitive to quark-gluon correlations and can be related to the color electric and magnetic polarizabilities in the nucleon.

$$d_2 = (2\chi_B + \chi_E)/3$$

- This integral is dominated by the high- x region and is well-suited to JLab at 11 GeV.
- Can improve error on d_2^n by a factor of 10 in less than 1000 hours.

