

Transversity

--status & opportunities with Hall C upgrade--

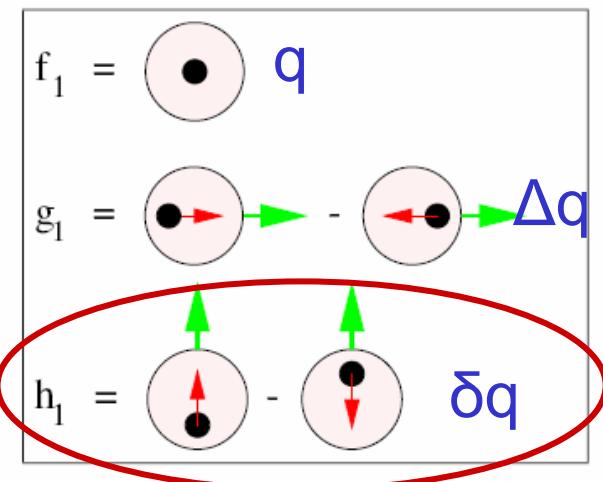
Lingyan Zhu

University of Illinois at Urbana-Champaign

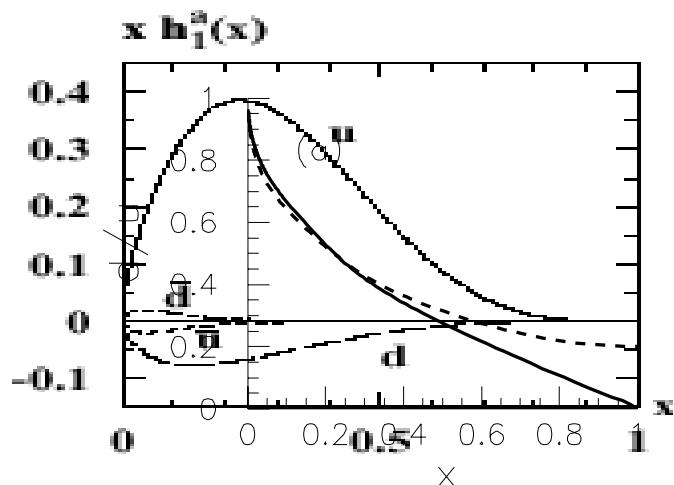
Hall C Summer Workshop, Aug. 25, 2006

Transversity

- $\delta q(x) = \Delta q(x)$ for non-relativistic quarks
- δq and gluons do not mix
→ Q^2 -evolution for δq and Δq are different
- Chiral-odd → not accessible in inclusive DIS



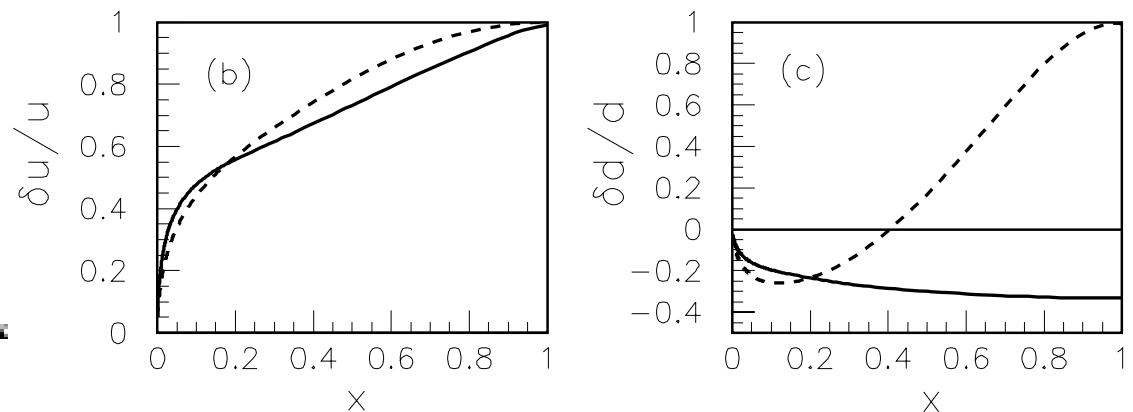
Chiral-quark soliton model



P. Schweitzer *et al*,

Phys.Rev. D64 (2001) 034013

Quark – diquark model (solid) & pQCD-based model (dashed)

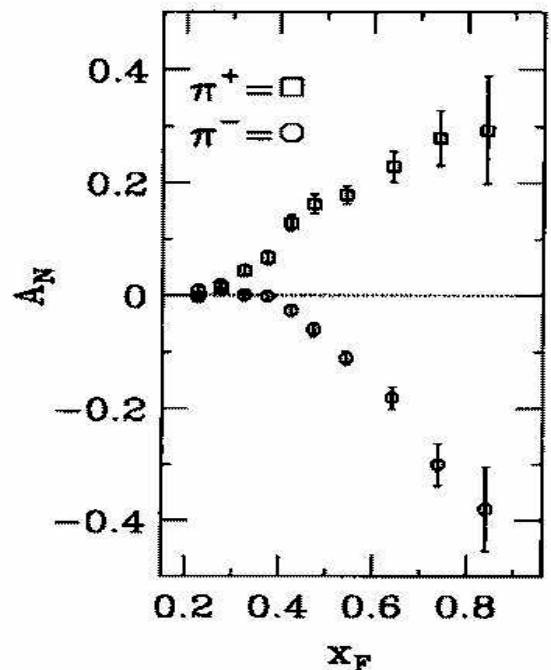


B.Q. Ma, I. Schmidt and J. J. Yang,

Phys.Rev. D65 (2002) 034010

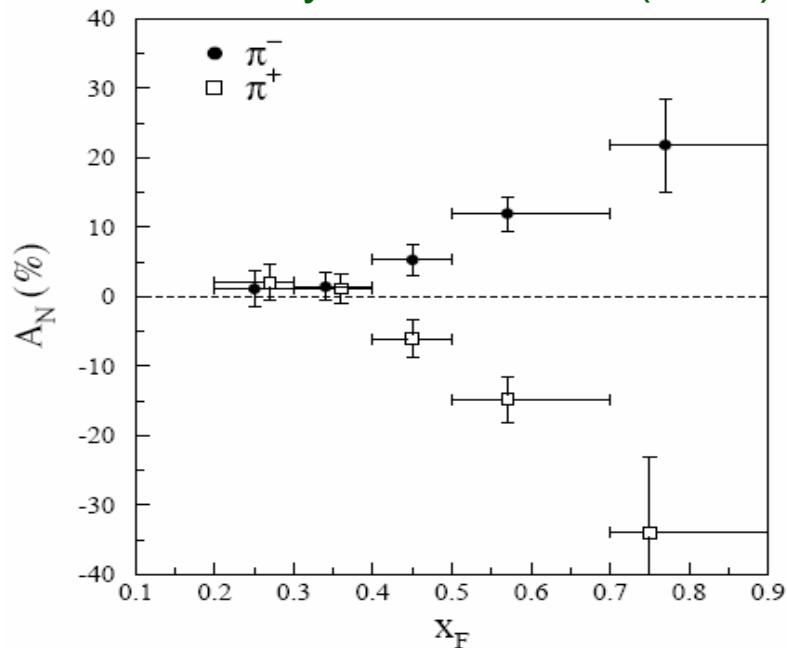
$p^\uparrow p \rightarrow \pi X$

FNAL E704: Phys.Lett. B264 (1991) 462.

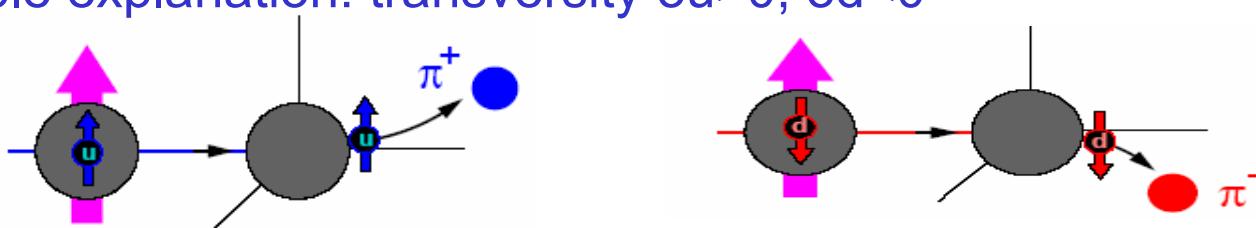


$\bar{p}^\uparrow p \rightarrow \pi X$

E704: Phys.Rev.Lett. 77 (1996) 2626.

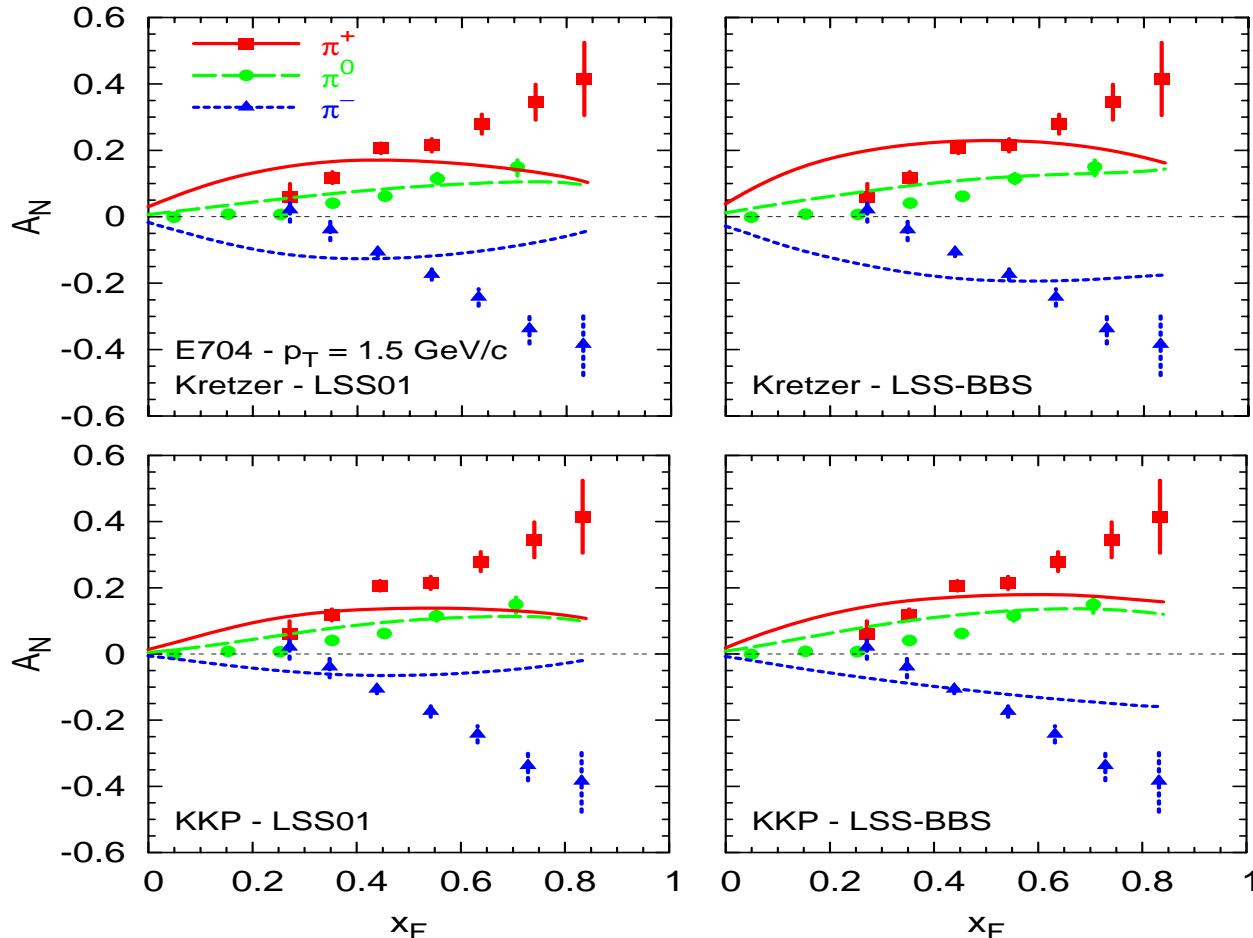


One possible explanation: transversity $\delta u > 0$, $\delta d < 0$



Suppression of the Collins mechanism

M.Anselmino *et al*, Phys.Rev. D71 (2005) 014002 [hep-ph/0408356]



Sivers effect is not suppressed by the intrinsic partonic motion.

All Eight Quark Distributions Are Probed in Semi-Inclusive DIS

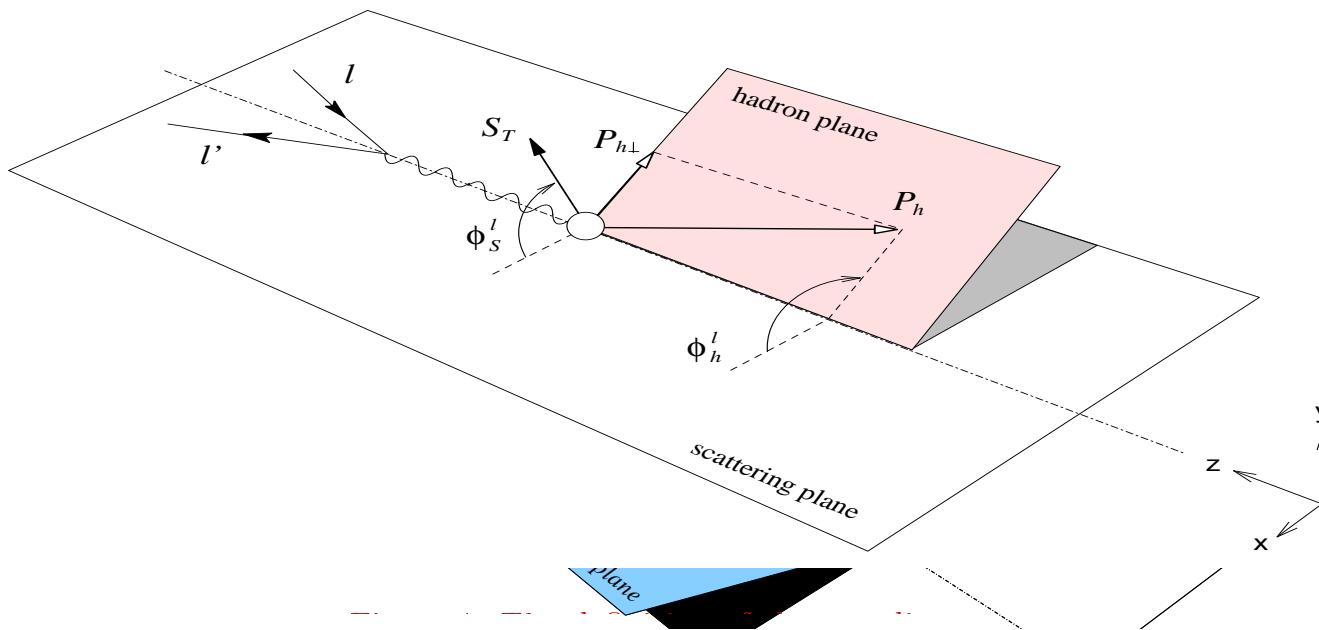
D. Boer, R. Jakob, and P.J. Mulders, NPB564, 471 (2000) [hep-ph/9907504].

$$\left[\frac{d\sigma(lH \rightarrow l'hX)}{d\Omega dx dz d^2 q_T} \right]_{UU} = \frac{\alpha^2 x z^2 s}{Q^4} \sum_{q,\bar{q}}$$

$f_1 =$		$\{(1 - y + y^2/2)e_q^2 \mathcal{F}[f_1 D_1]$	Unpolarized
$h_1^\perp =$		$+ (1 - y)e_q^2 \cos(2\phi) \mathcal{F}\left[(2\hat{h} \cdot p_T \hat{h} \cdot k_T - p_T \cdot k_T) \frac{h_1^\perp H_1^\perp}{M_1 M_2}\right]$	
$h_{1L}^\perp =$		$- S_L (1 - y)e_q^2 \sin(2\phi) \mathcal{F}\left[(2\hat{h} \cdot p_T \hat{h} \cdot k_T - p_T \cdot k_T) \frac{h_{1L}^\perp H_1^\perp}{M M_h}\right]$	Transversity/Collins
$h_{1T} =$		$- S_T (1 - y)e_q^2 \sin(\phi + \phi_S) \mathcal{F}\left[\hat{h} \cdot k_T \frac{h_1 H_1^\perp}{M_h}\right]$	
$f_{1T}^\perp =$		$+ S_T (1 - y + y^2/2)e_q^2 \sin(\phi - \phi_S) \mathcal{F}\left[\hat{h} \cdot p_T \frac{f_{1T}^\perp D_1}{M}\right]$	Sivers
$h_{1T}^\perp =$		$- S_T (1 - y)e_q^2 \sin(3\phi - \phi_S) \mathcal{F}\left[(4(\hat{h} \cdot p_T)^2 \hat{h} \cdot k_T - 2\hat{h} \cdot p_T p_T \cdot k_T - p_T^2 \hat{h} \cdot k_T) \frac{h_{1T}^\perp H_1^\perp}{2M^2 M_h}\right]$	
$g_{1L} =$		$+ \lambda_e S_L y(1 - y/2)e_q^2 \mathcal{F}[g_1 D_1]$	Polarized beam and target
$g_{1T} =$		$+ \lambda_e S_T y(1 - y/2)e_q^2 \cos(\phi - \phi_S) \mathcal{F}\left[\hat{h} \cdot p_T \frac{g_{1T} D_1}{M}\right]\}$	

S_L and S_T : Target Polarizations; λ_e : Beam Polarization

Target Single-Spin Asymmetry in SIDIS

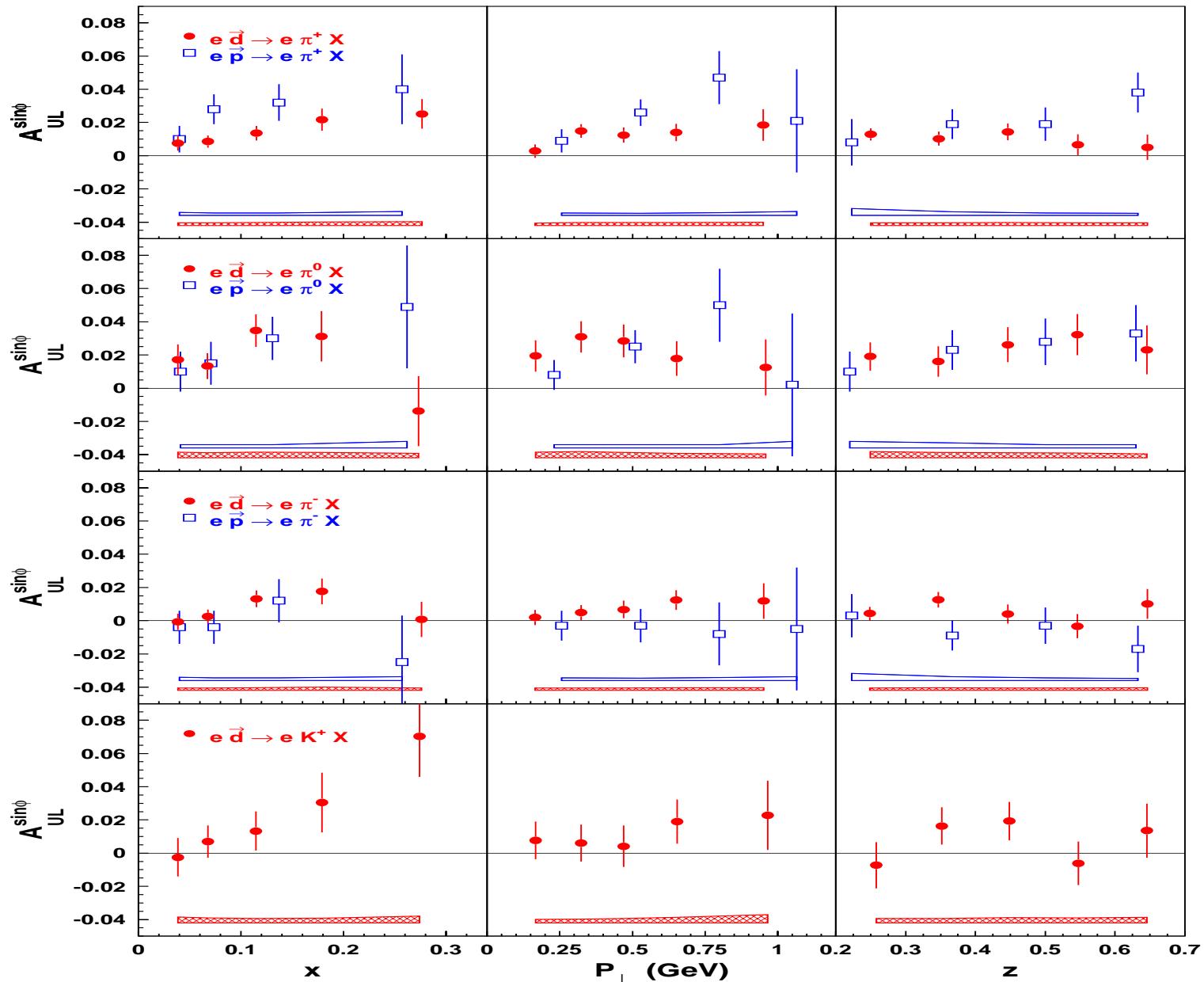


$$\begin{aligned}
 A_{UT}^{uw, gauss} \propto & \quad A(< p_T >, < k_T >) |S_T| (1 - y) \sin(\phi_h + \phi_S) \sum e_q^2 h_1^q H_{1q}^{\perp h(1/2)} \text{ Collins term} \\
 + & \quad B(< p_T >, < k_T >) |S_T| (1 - y + \underbrace{y^2/2}_{\text{plane}}) \sin(\phi_h - \phi_S) \sum e_q^2 f_{1T}^{\perp q} D_{1q}^{h(1/2)} \text{ Sivers term}
 \end{aligned}$$

p_T/k_T : Intrinsic transverse momentum of quark/fragmentation

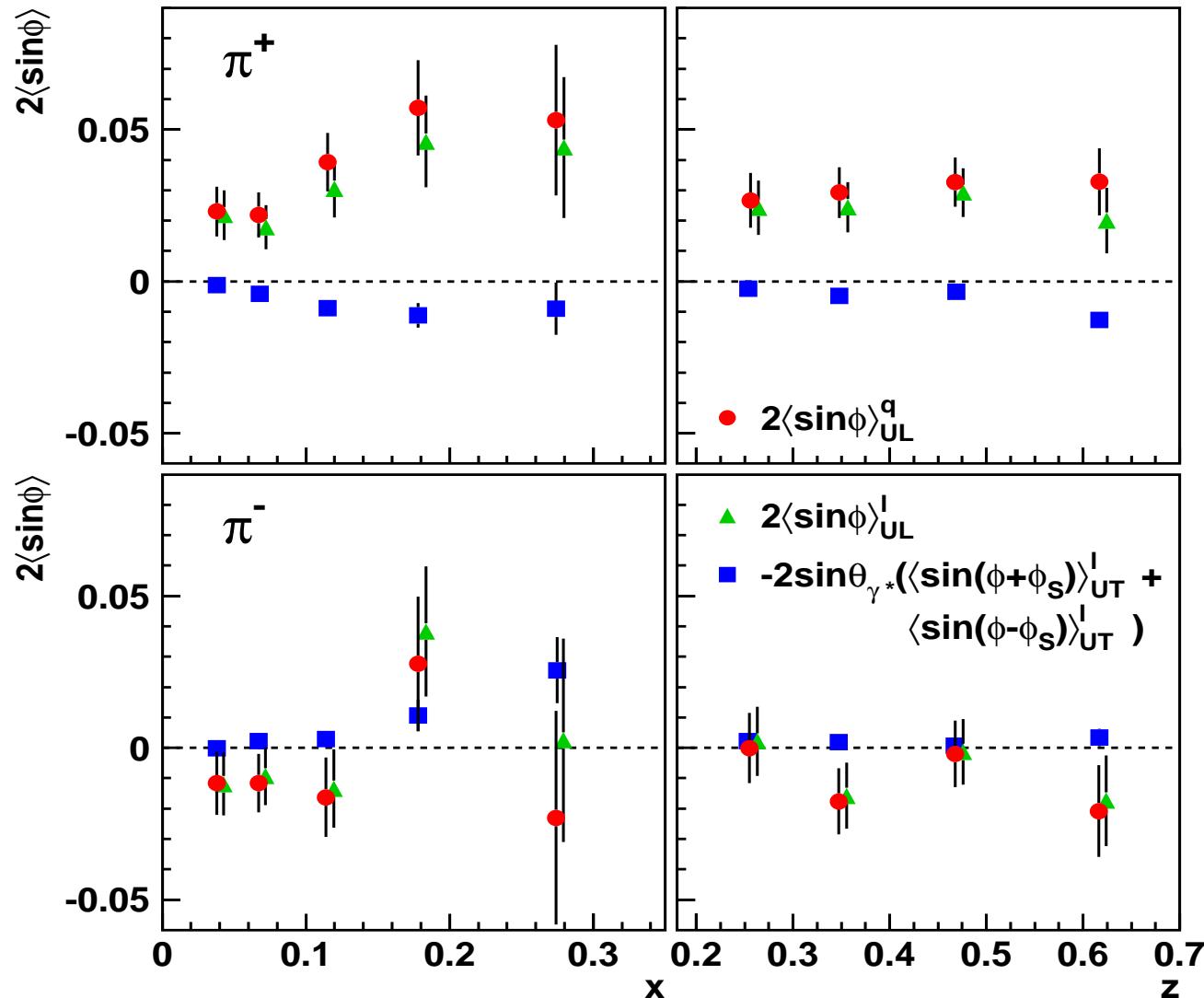
The angles are defined relative to the virtual photon direction.

$A_{UL}^{\sin\phi}$ from HERMES



$A_{UL}^{\sin \phi}$ from HERMES

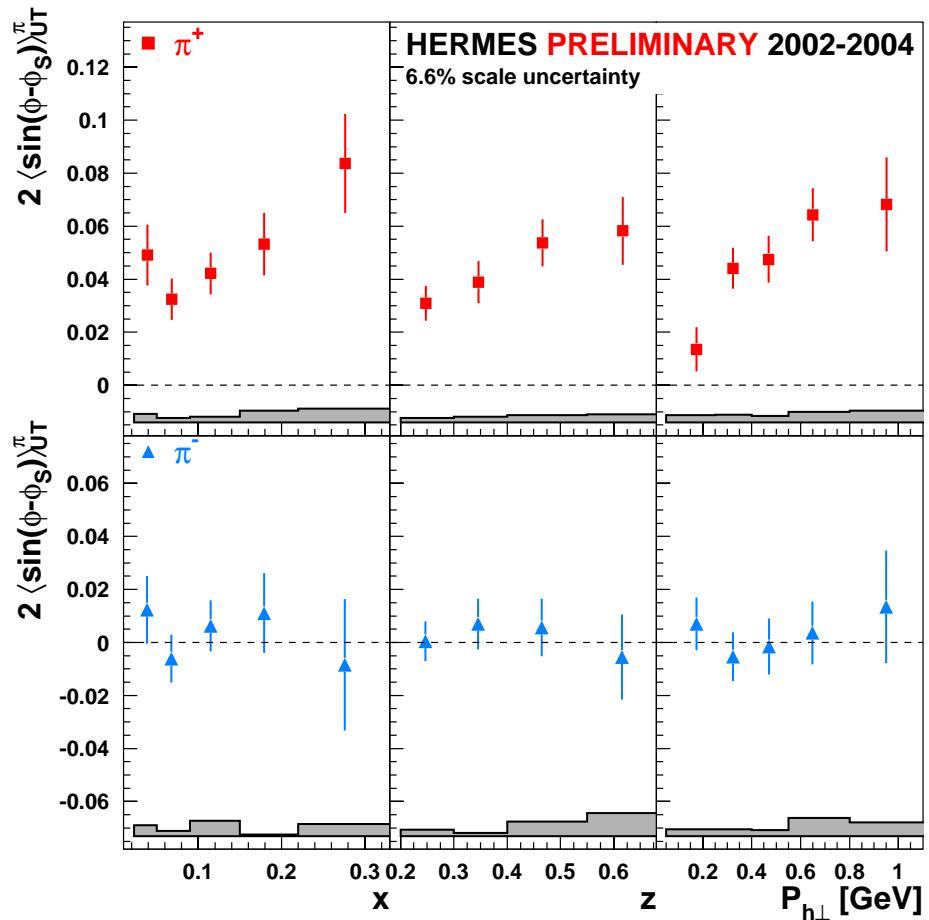
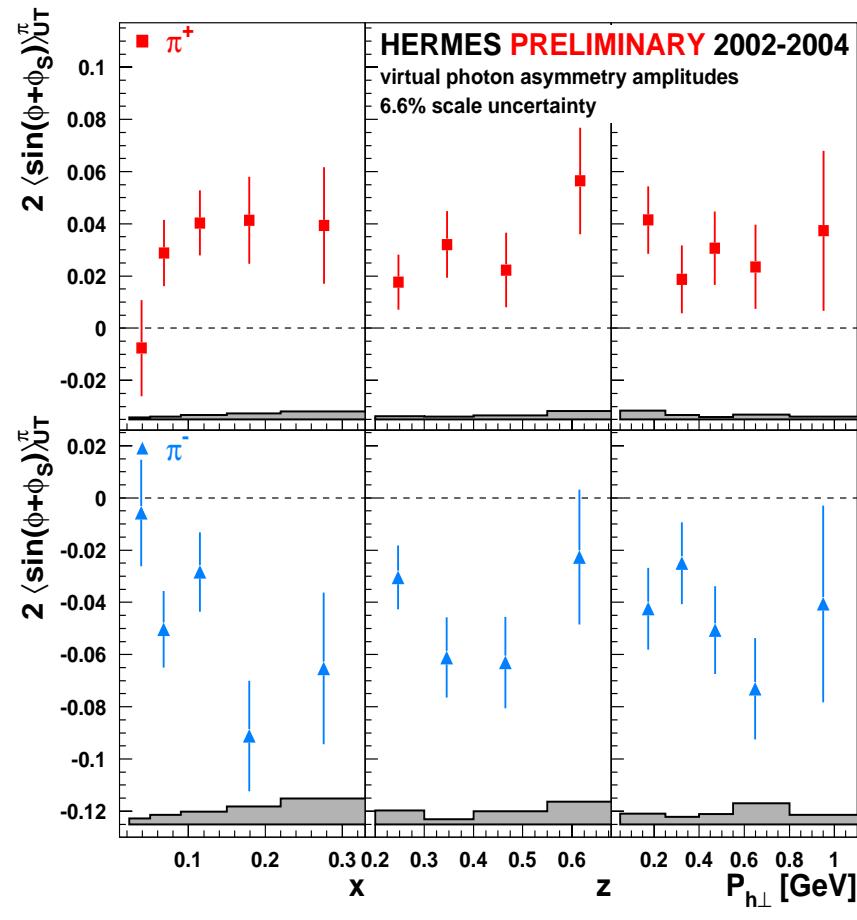
turned out to be dominated by high twist effect



HERMES data: Collins and Sivers Moments

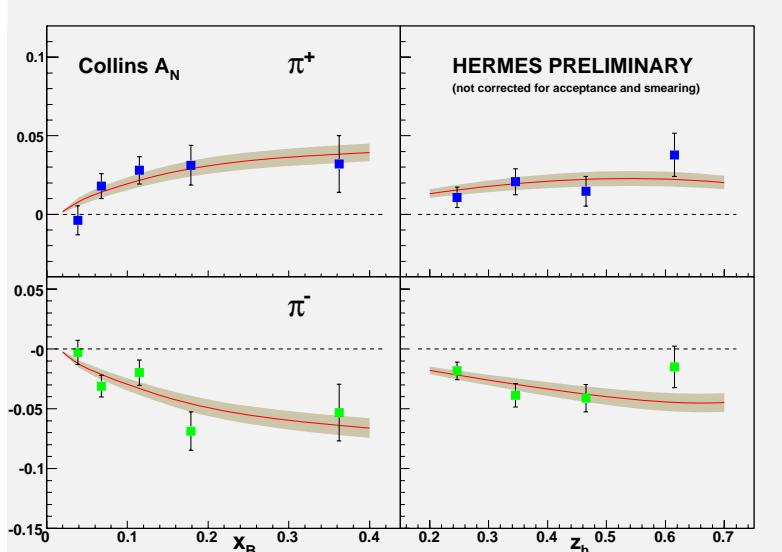
$$2 < \sin \phi_{Collins} >_{UT}^{\pi}$$

$$2 < \sin \phi_{Sivers} >_{UT}^{\pi}$$

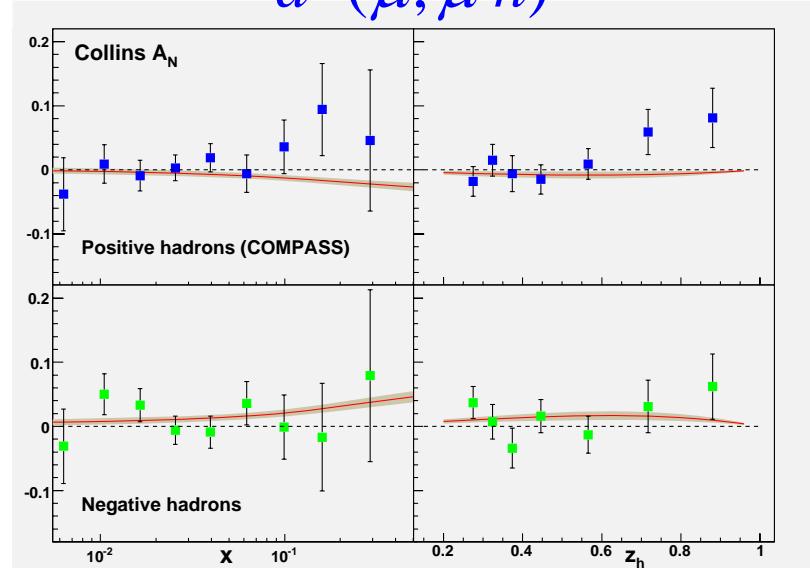


Extraction of Collins functions from HERMES data

Fits to the Hermes data
 $p^\uparrow(e, e'\pi)$



“Prediction” of the Compass data
 $d^\uparrow(\mu, \mu'h)$



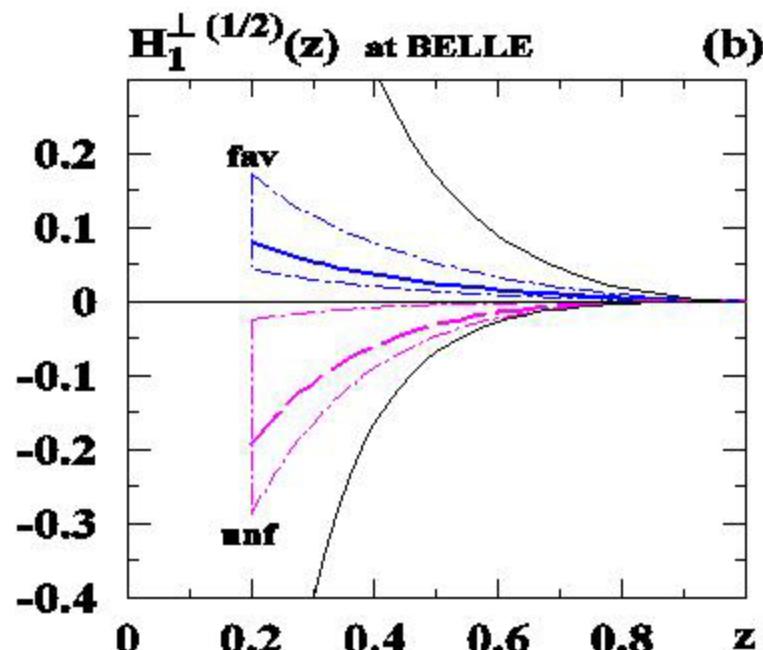
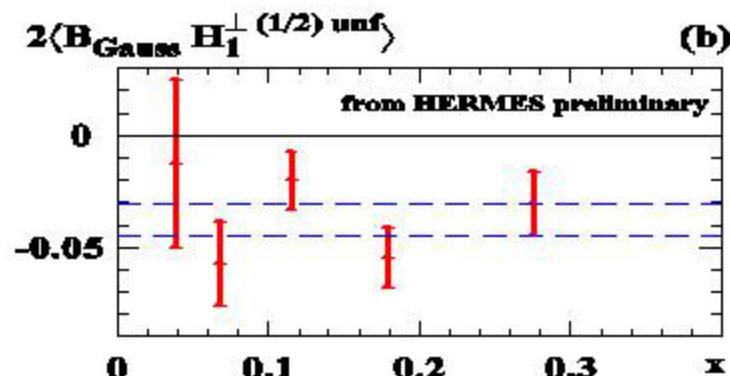
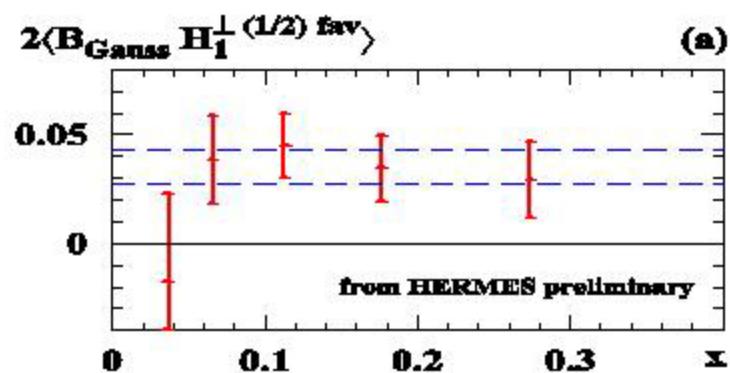
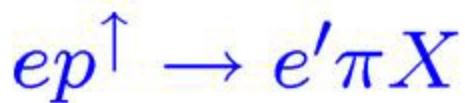
Assuming $H_1^{\perp, fav}(z) = C_{fav} z(1-z) D_1^{fav}(z); \quad H_1^{\perp, unfav}(z) = C_{unfav} z(1-z) D_1^{fav}(z)$

$$C_{fav} = -0.29 \pm 0.04, \quad C_{unfav} = 0.33 \pm 0.04$$

W. Vogelsang & F. Yuan, Phys.Rev.D72(2005)054028 [hep-ph/0507266]

$$H_1^{\perp, unfavored} / H_1^{\perp, favored} \approx -1$$

Favored/Unfavored Collins fragmentation functions



Efremov, Goeke, and Schweitzer, Phys.Rev. D73 (2006) 094025

SIDIS and e^+e^- data are consistent within uncertainties.

Collins Asymmetry in Pion SIDIS

$$H^+ \equiv H_u^{\pi^+} = H_{\bar{u}}^{\pi^-} = H_{\bar{d}}^{\pi^+} = H_d^{\pi^-}$$

$$H^- \equiv H_{\bar{u}}^{\pi^+} = H_u^{\pi^-} = H_d^{\pi^+} = H_{\bar{d}}^{\pi^-}$$

$$H_s^\pi \equiv H_s^{\pi^+} = H_s^{\pi^-} = H_{\bar{s}}^{\pi^+} = H_{\bar{s}}^{\pi^-}$$

$$A_p^{\pi^+} \propto \frac{(4\delta u + \delta \bar{d})H^+ + (\delta d + 4\delta \bar{u})H^- + (\delta s + \delta \bar{s})H_s^\pi}{(4u + \bar{d})D^+ + (d + 4\bar{u})D^- + (s + \bar{s})D_s^\pi}$$

$$A_p^{\pi^-} \propto \frac{(4\delta u + \delta \bar{d})H^- + (\delta d + 4\delta \bar{u})H^+ + (\delta s + \delta \bar{s})H_s^\pi}{(4u + \bar{d})D^- + (d + 4\bar{u})D^+ + (s + \bar{s})D_s^\pi}$$

$$A_n^{\pi^+} \propto \frac{(4\delta d + \delta \bar{u})H^+ + (\delta u + 4\delta \bar{d})H^- + (\delta s + \delta \bar{s})H_s^\pi}{(4d + \bar{u})D^+ + (u + 4\bar{d})D^- + (s + \bar{s})D_s^\pi}$$

$$A_n^{\pi^-} \propto \frac{(4\delta d + \delta \bar{u})H^- + (\delta u + 4\delta \bar{d})H^+ + (\delta s + \delta \bar{s})H_s^\pi}{(4d + \bar{u})D^- + (u + 4\bar{d})D^+ + (s + \bar{s})D_s^\pi}$$

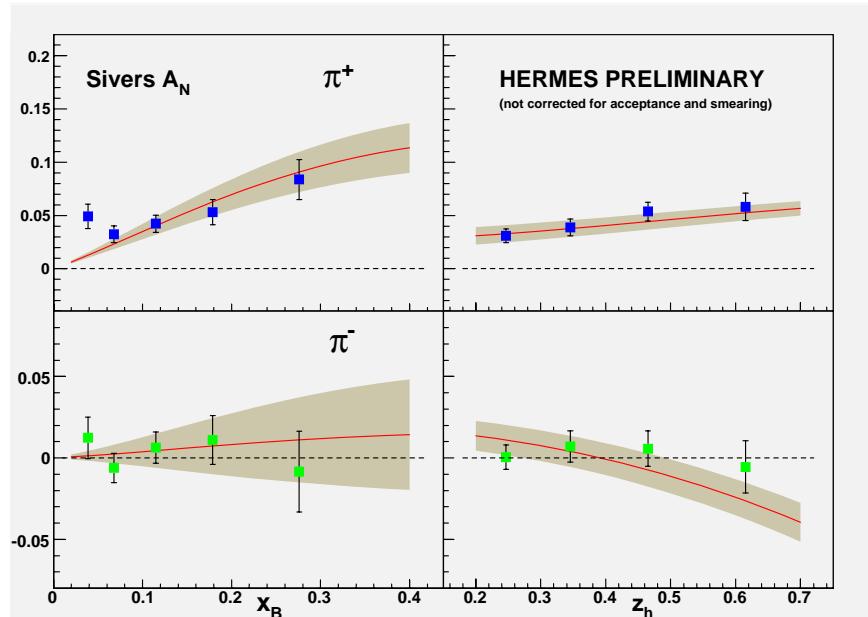
$H = H_1^{\perp(1/2)}$

for unweighted Collins moments

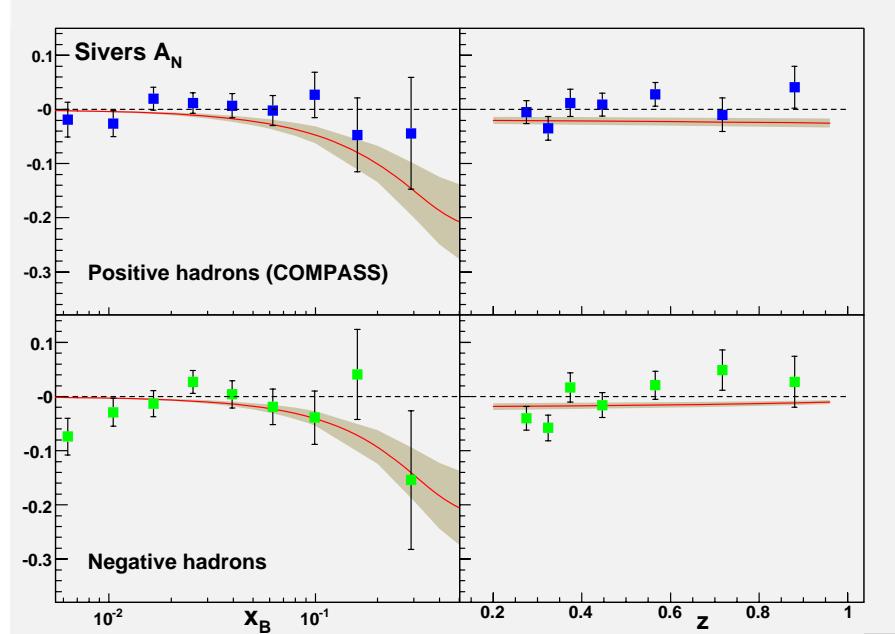
$$\frac{H^-}{H^+} = \frac{A_p^{\pi^-}}{A_p^{\pi^+}} \cdot \frac{D^-}{D^+} \approx -1 \text{ with } u \text{ quark dominance}$$

Extraction of Sivers function from HERMES data

Fits to the Hermes data



“Prediction” of the Compass data



Assuming $f_{1T}^{\perp,u}(x) = S_u x(1-x)u(x)$; $f_{1T}^{\perp,d}(x) = S_d x(1-x)u(x)$

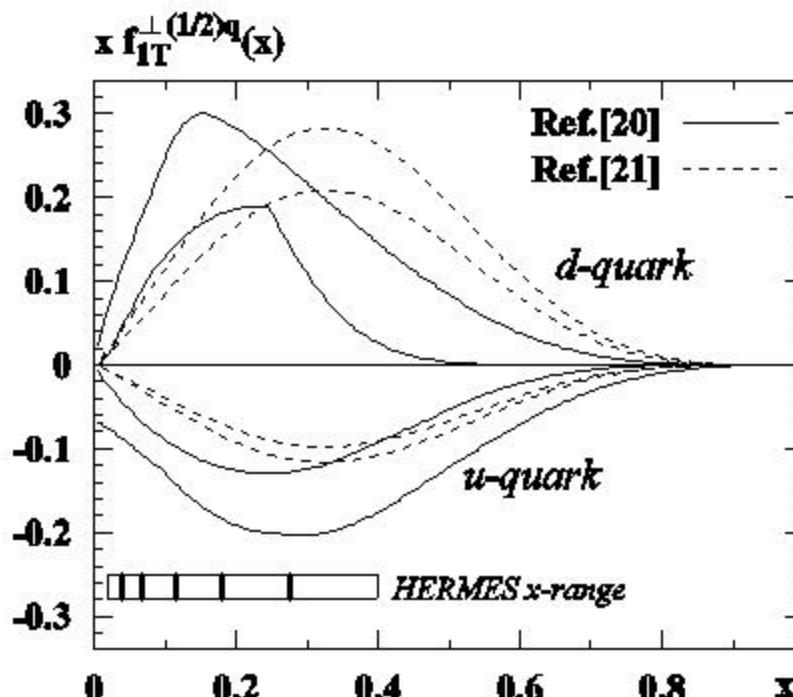
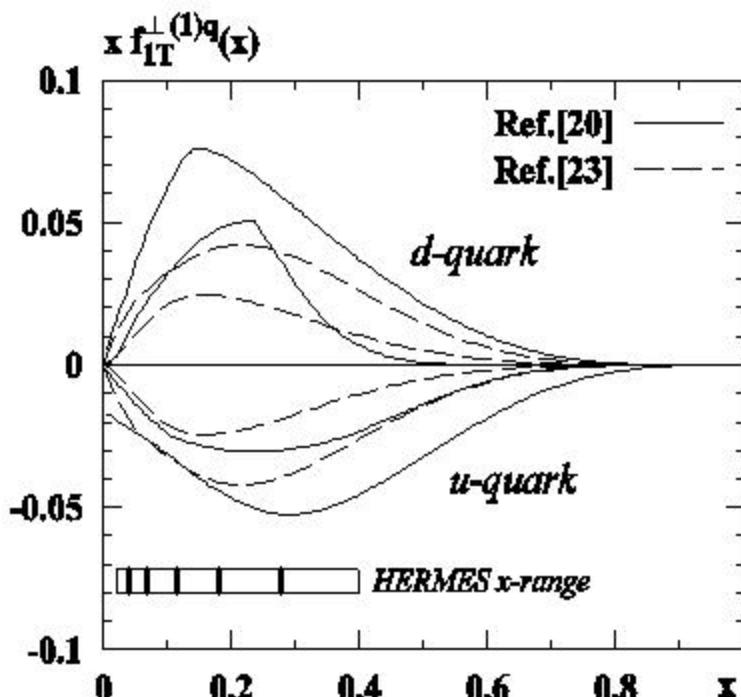
$$S_u = -0.81 \pm 0.07, \quad S_d = 1.86 \pm 0.28$$

Vogelsang and Yuan, Phys.Rev.D72(2005)054028 [hep-ph/0507266]

Striking flavor dependence of the Sivers function

Comparing extractions of Sivers functions

M.Anselmino et al, hep-ph/0511017



Ref.[20] M.Anselmino et al, Phys.Rev.D72(2005)094007[hep-ph/0507181]

Ref.[21] W.Vogelsang & F.Yuan, Phys.Rev.D72(2005)054028[hep-ph/0507266]

Ref.[23] J.C.Collins et al, hep-ph/0510342

Satisfactory qualitative agreement between different models

Sivers Asymmetry in Pion SIDIS

$$A_p^{\pi^+} \propto \frac{(4f_{1T}^{\perp,u} + f_{1T}^{\perp,\bar{d}})D^+ + (f_{1T}^{\perp,d} + 4f_{1T}^{\perp,\bar{u}})D^- + (f_{1T}^{\perp,s} + f_{1T}^{\perp,\bar{s}})D_s^\pi}{(4u + \bar{d})D^+ + (d + 4\bar{u})D^- + (s + \bar{s})D_s^\pi}$$

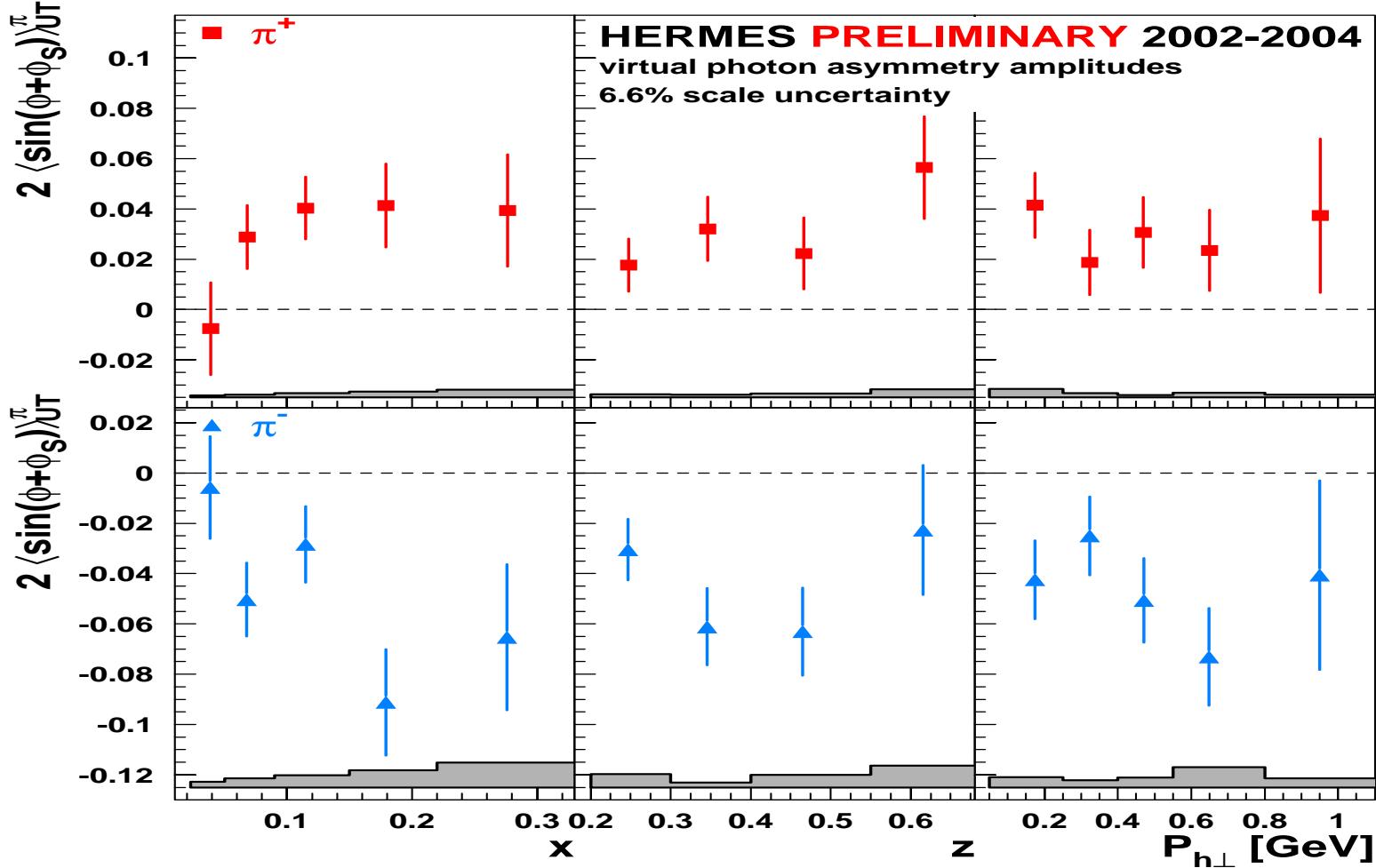
$$A_p^{\pi^-} \propto \frac{(4f_{1T}^{\perp,u} + f_{1T}^{\perp,\bar{d}})D^- + (f_{1T}^{\perp,d} + 4f_{1T}^{\perp,\bar{u}})D^+ + (f_{1T}^{\perp,s} + f_{1T}^{\perp,\bar{s}})D_s^\pi}{(4u + \bar{d})D^- + (d + 4\bar{u})D^+ + (s + \bar{s})D_s^\pi}$$

$$A_n^{\pi^+} \propto \frac{(4f_{1T}^{\perp,d} + f_{1T}^{\perp,\bar{u}})D^+ + (f_{1T}^{\perp,u} + 4f_{1T}^{\perp,\bar{d}})D^- + (f_{1T}^{\perp,s} + f_{1T}^{\perp,\bar{s}})D_s^\pi}{(4d + \bar{u})D^+ + (u + 4\bar{d})D^- + (s + \bar{s})D_s^\pi}$$

$$A_n^{\pi^-} \propto \frac{(4f_{1T}^{\perp,d} + f_{1T}^{\perp,\bar{u}})D^- + (f_{1T}^{\perp,u} + 4f_{1T}^{\perp,\bar{d}})D^+ + (f_{1T}^{\perp,s} + f_{1T}^{\perp,\bar{s}})D_s^\pi}{(4d + \bar{u})D^- + (u + 4\bar{d})D^+ + (s + \bar{s})D_s^\pi}$$

$$A_p^{\pi^-} \approx 0 \Rightarrow \frac{f_{1T}^{\perp,u}}{f_{1T}^{\perp,d}} \approx -\frac{D^+}{4D^-} \approx -2$$

Collins $P_{h\perp}$ dependence



$A_p^{\pi^\pm} \propto P_{h\perp}?$

Current Status

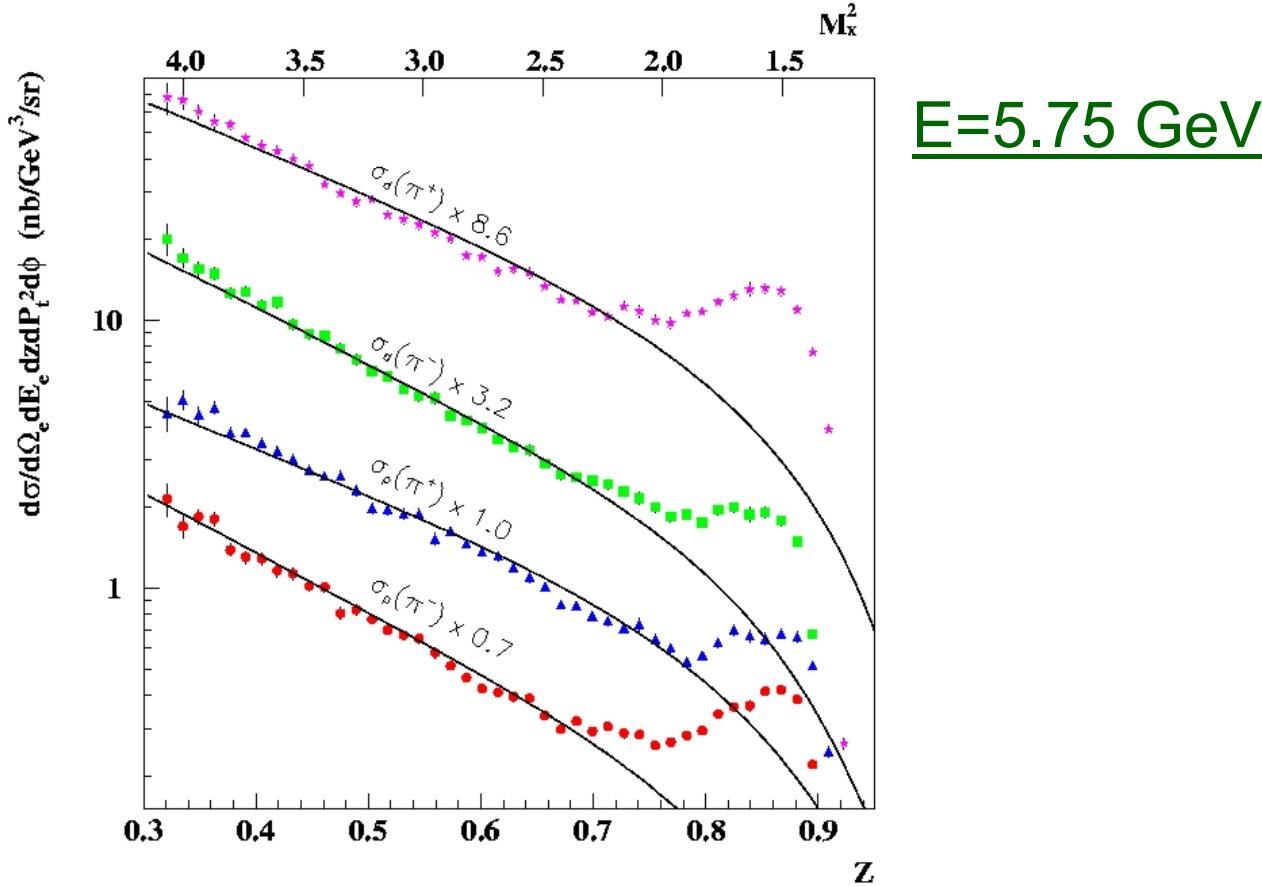
- Proton data show very large transverse asymmetry, which initiated the excitement on transversity. But more likely, it was due to Sivers effect instead of Collins effect involving transversity.
- HERMES longitudinal data being described very well by various of models turned out to be dominated by high-twist effect.
- HERMES transverse data show some surprising features, for example in Collins H^-/H^+ , Sivers f_{1T}^u/f_{1T}^d , and P_{hT} dependence. The current constraint on the transversity is pretty loose, and the x , z and P_T distributions are coupled together.
- More data especially with controlled kinematics are essential for cross check, multi-dimension binning, transversity extraction, ...

The way of learning is a way of correcting.

Is SIDIS applicable at JLab?

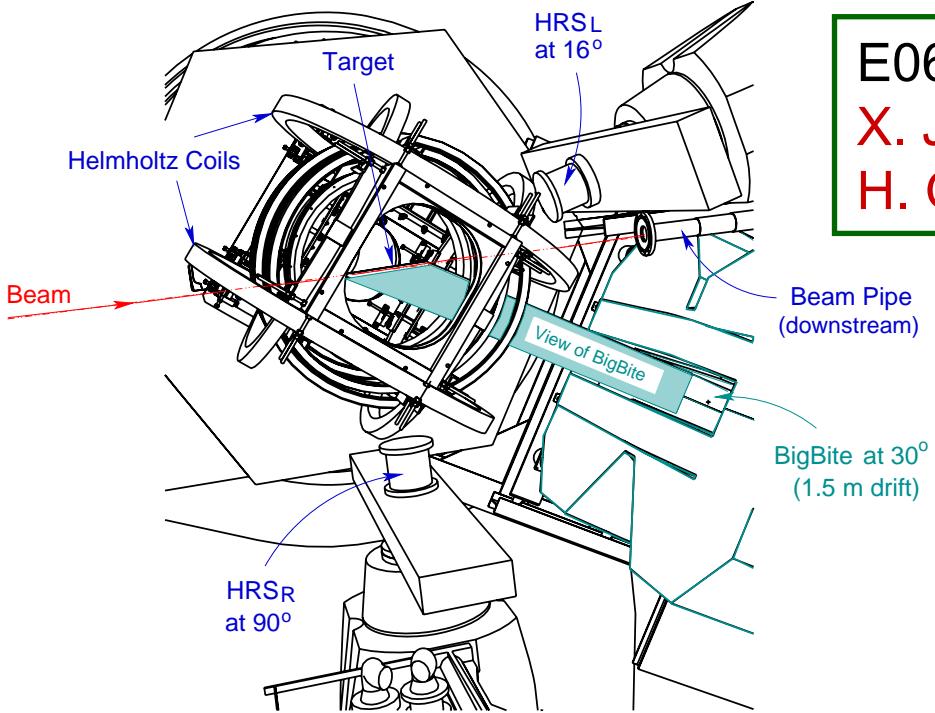
Preliminary results from Hall-C E00-108

$p(e, e'\pi^\pm)$ and $d(e, e'\pi^\pm)$ at $x = 0.3$



Data beyond Δ region are well described by LO SIDIS ansatz.

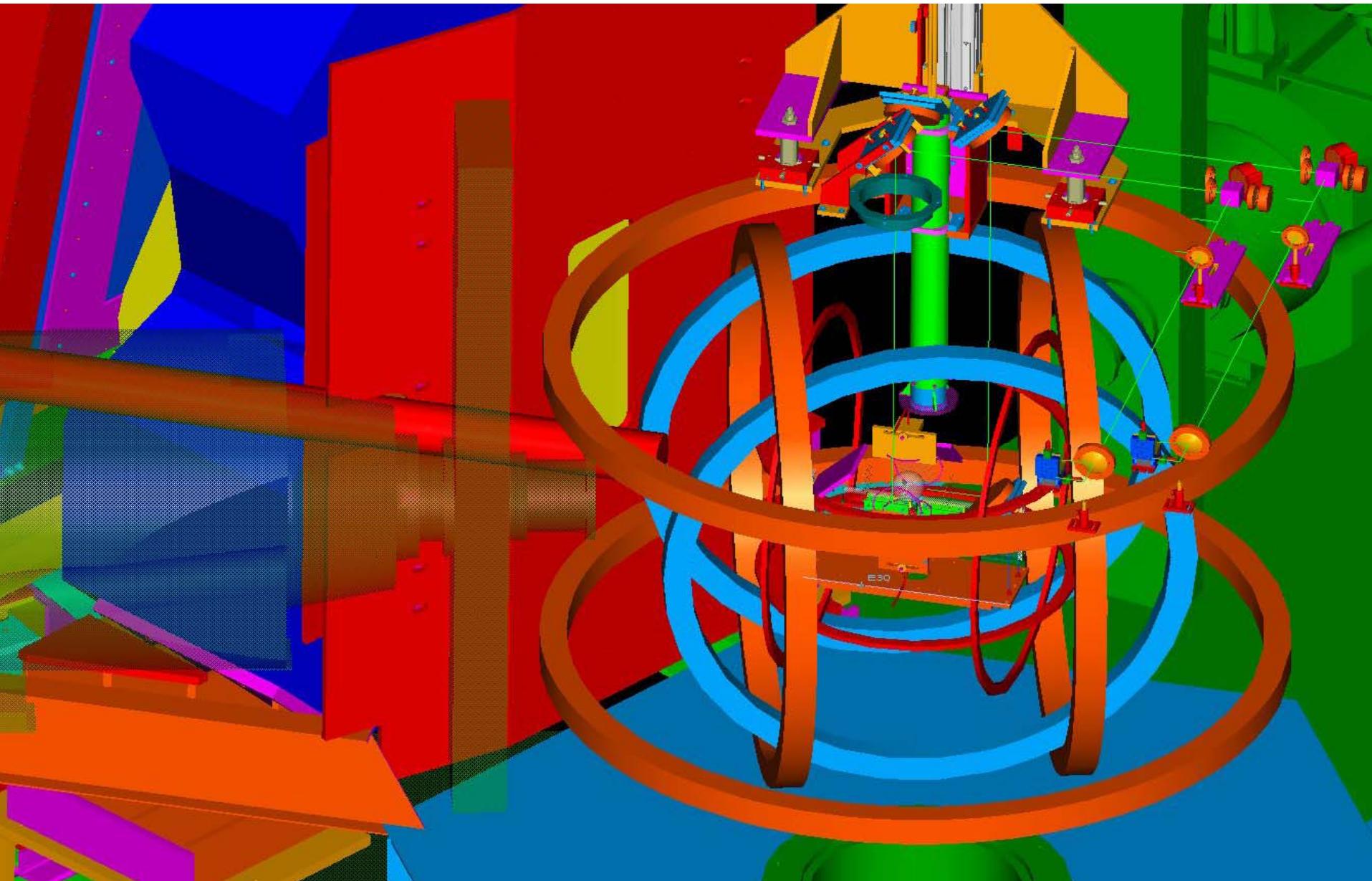
${}^3\text{He}^\uparrow(\text{e}, \text{e}'\pi^{+/-})\text{x}$ at Hall-A



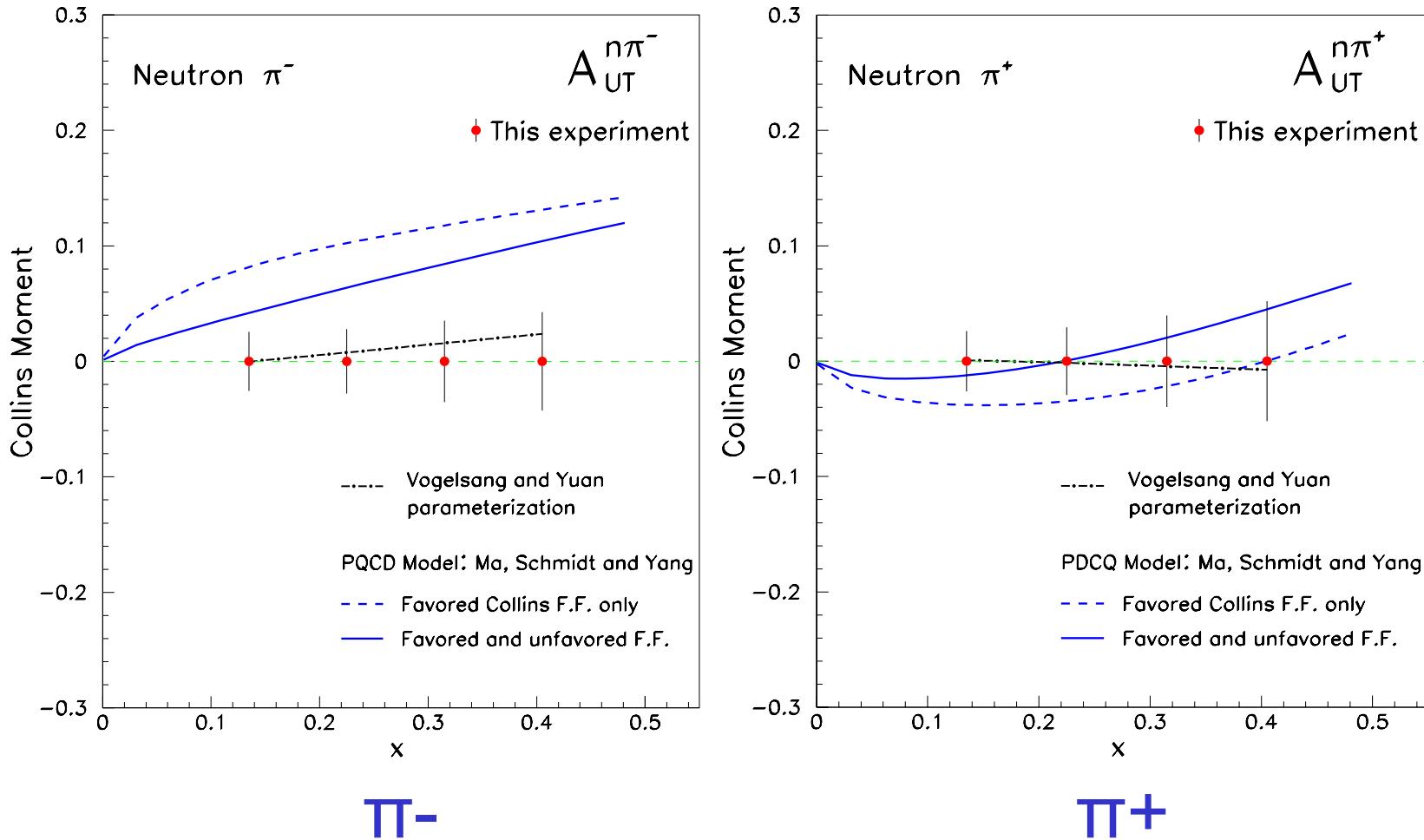
E06-010/06-011 Spokespersons:
X. Jiang, J.P. Chen, E. Cisbani,
H. Gao, J.C. Peng

- **Beam**
 - 6 GeV, 15 μA e^- beam
- **Target**
 - Optically pumped Rb-K spin-exchange ${}^3\text{He}$ target, 50 mg/cm^2 , ~42% polarization, transversely polarized with tunable direction
- **Electron detection**
 - BigBite spectrometer, Solid angle = 60 msr, $\theta_{\text{Lab}} = 30^\circ$
- **Charged pion detection**
 - HRS spectrometer, $\theta_{\text{Lab}} = -16^\circ$

Polarized ^3He target with vertical coils

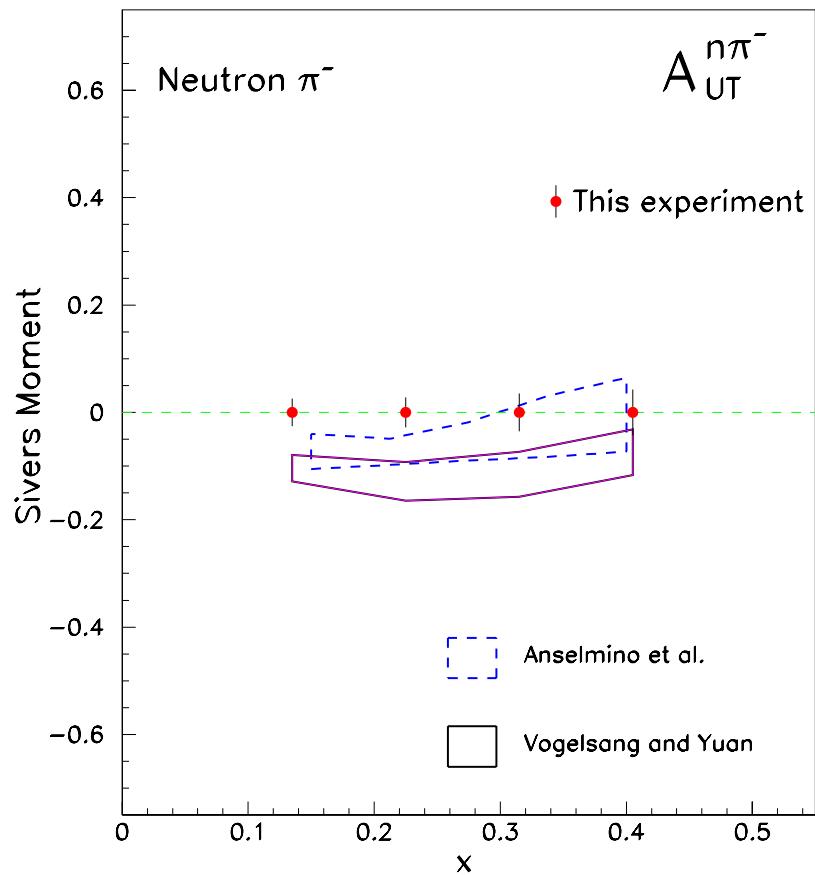


Predictions of Collins asymmetry on neutron

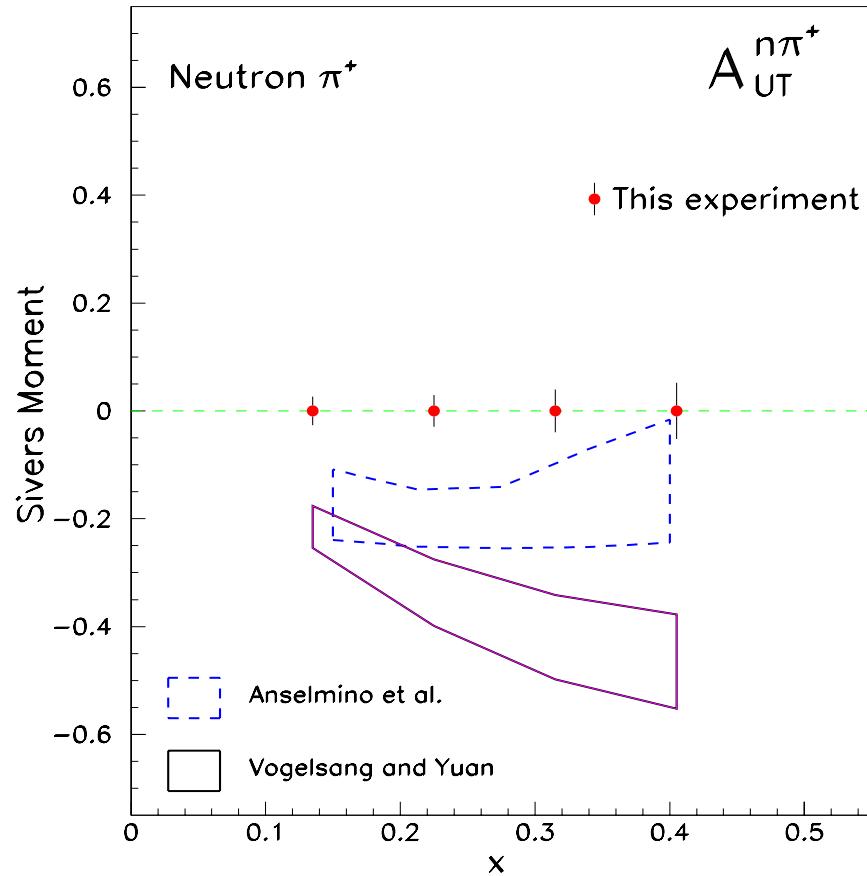


The errors with approved beam time will be 33% higher.

Predictions of Sivers asymmetry on neutron



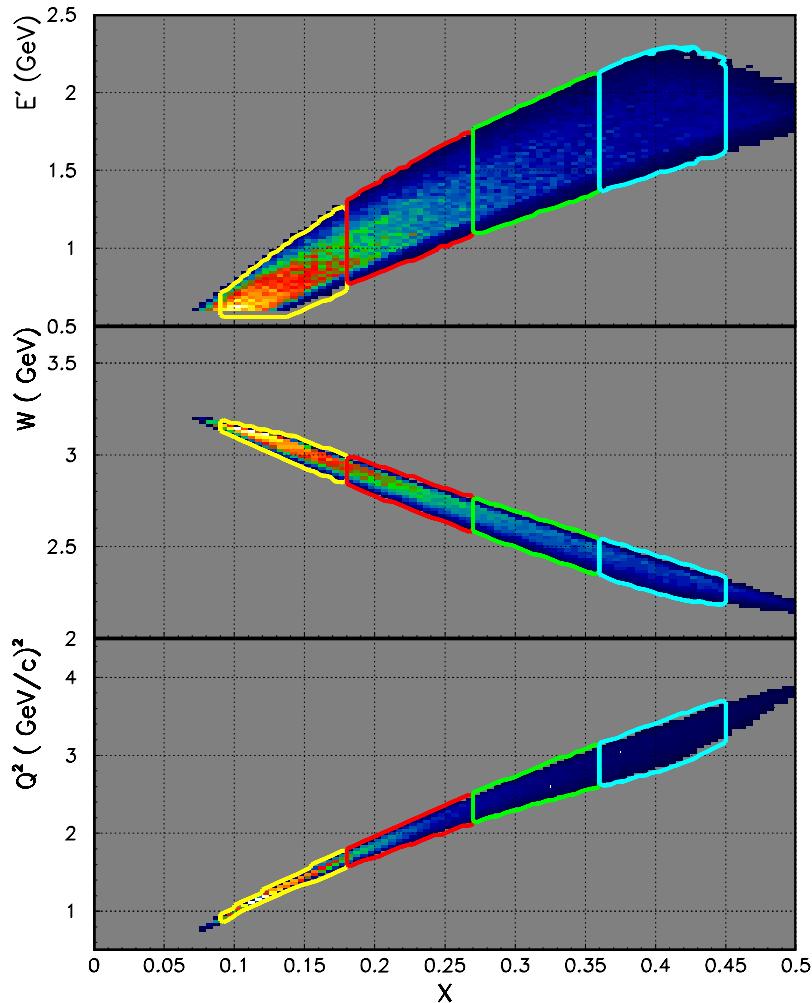
π^-



π^+

The errors with approved beam time will be 33% higher.

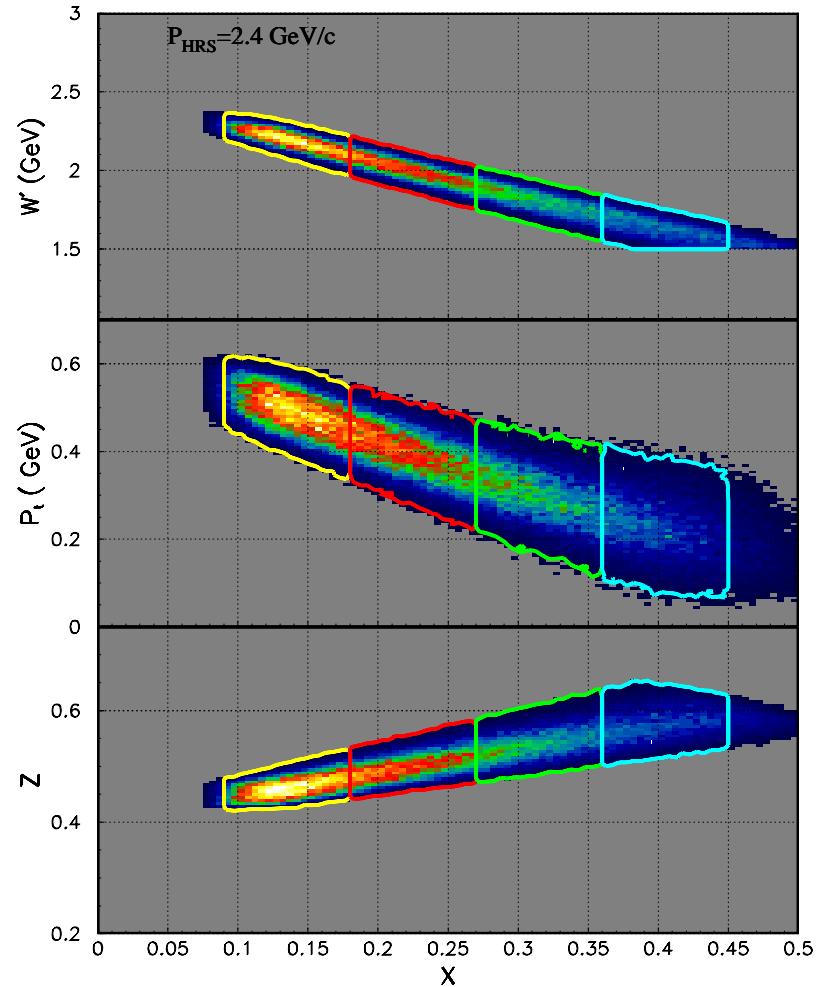
Kinematic Coverage at 6 GeV



$$\langle x \rangle = 0.135, 0.225, 0.315, 0.405$$

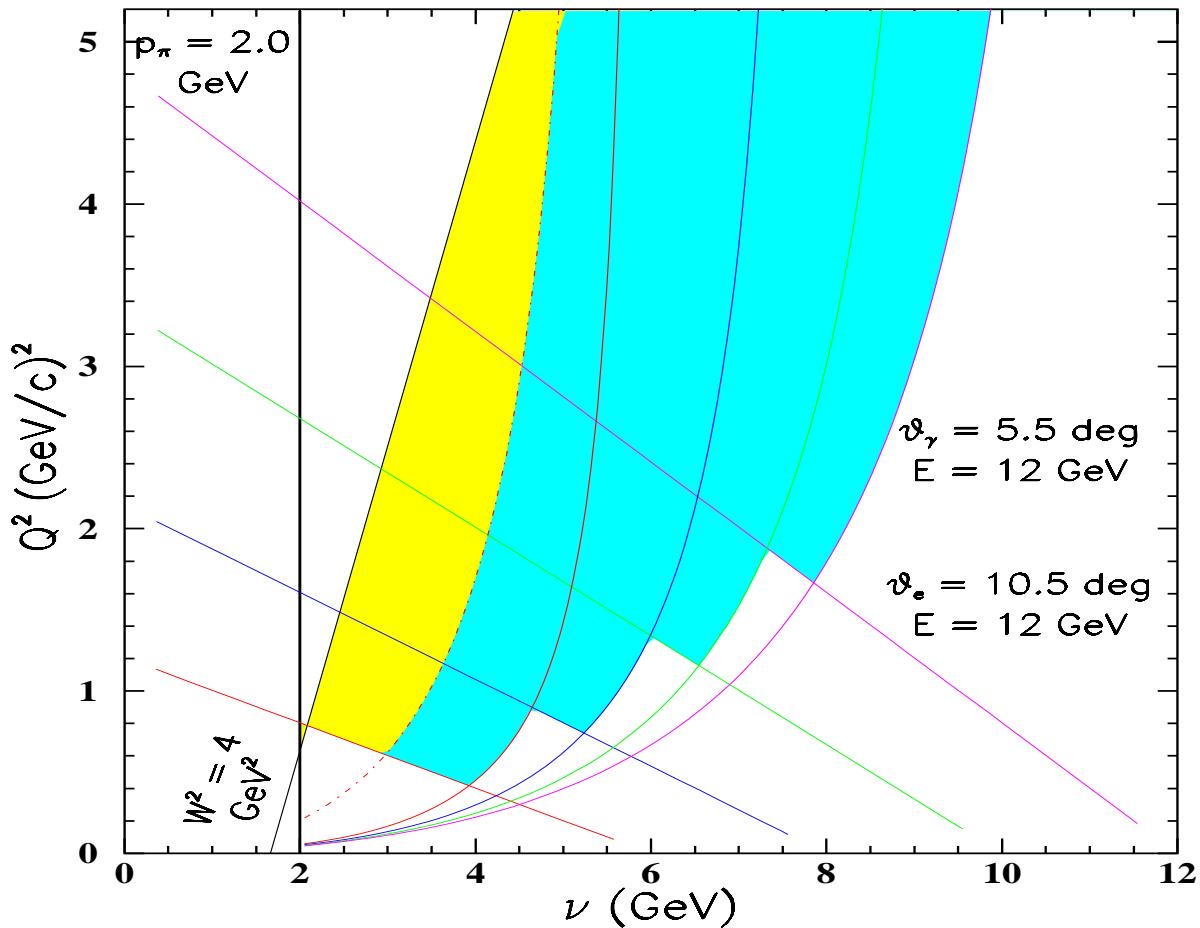
$$\langle z \rangle = 0.473, 0.515, 0.558, 0.601$$

X is strongly correlated with Q^2



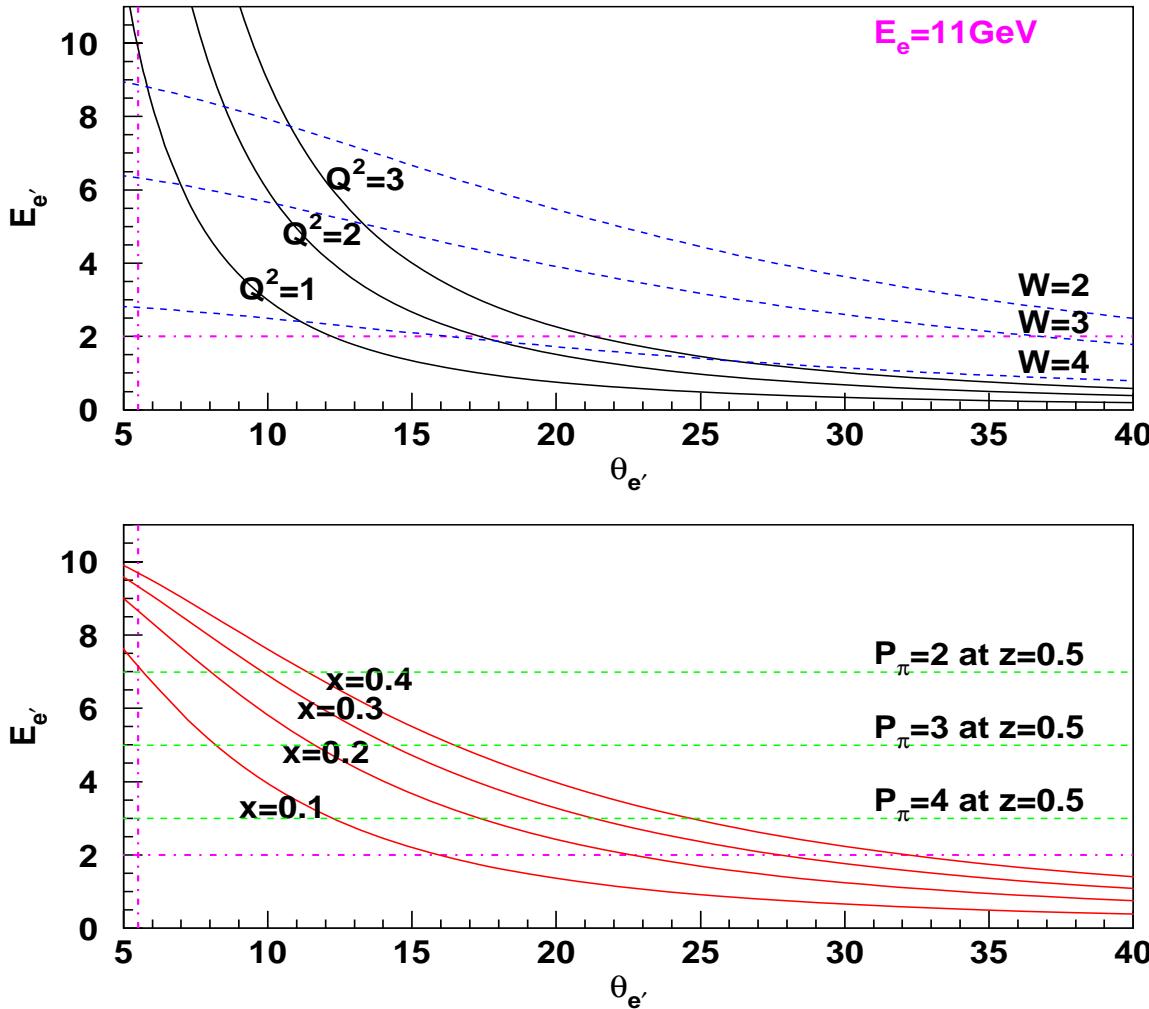
Kinematic Coverage w HMS(e)+SHMS(h)

Hall C CDR (2002): R. Ent and C.E. Keppel



Higher beam energy with JLab upgrade offer larger phase space.

Kinematical Coverage w SHMS(e)+HMS(h)



$$Q^2 = 4E_e E_{e'} \sin^2(\theta_{e'}/2)$$

$$W = \sqrt{M^2 + 2M(E_e - E_{e'}) - Q^2}$$

$$x = \frac{Q^2}{2M(E_e - E_{e'})}$$

$$z = \frac{E_\pi}{E_e - E_{e'}}$$

Larger $\theta_{e'}$, $E_{e'}$ \rightarrow larger x , Q^2 ; smaller W , W' , θ_q , σ

Kinem. Ex: x-dependence at fixed Q

E' (GeV)	θ_e (deg)	x	W (GeV)	Q^2 (GeV 2)	y	θ_q (deg)	P_π (GeV)	θ_π (deg)	z	$ P_T $ (GeV)	W' (GeV)
4.80	12.5	$0.22^{-0.04}_{+0.10}$	3.16	2.50	0.56	-9.34	3.10	-13.1	0.50	0.20	2.31
6.20	11.0	$0.28^{-0.06}_{+0.19}$	2.72	2.51	0.44	-13.54	2.40	-18.4	0.50	0.20	2.00
7.50	10.0	$0.38^{-0.10}_{+0.50}$	2.22	2.51	0.32	-19.82	1.74	-13.1	0.50	0.20	1.65

$E=11\text{GeV}$

- SHMS(e) + HMS(h) Due to δP

- Same central Q^2, z, P_T

- $\Phi_{\text{Sivers}} > \pm 47^\circ$; $\Phi_{\text{Collins}} > \pm 58^\circ$

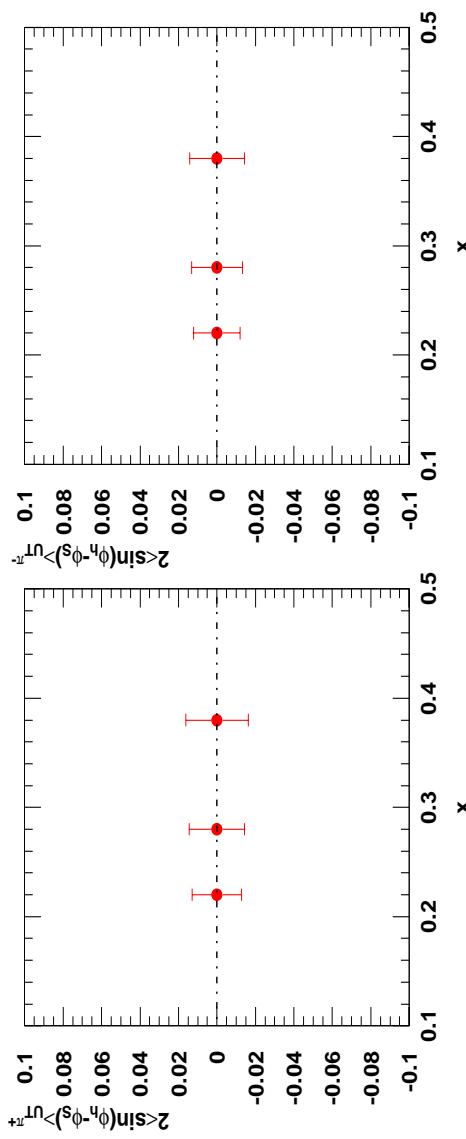
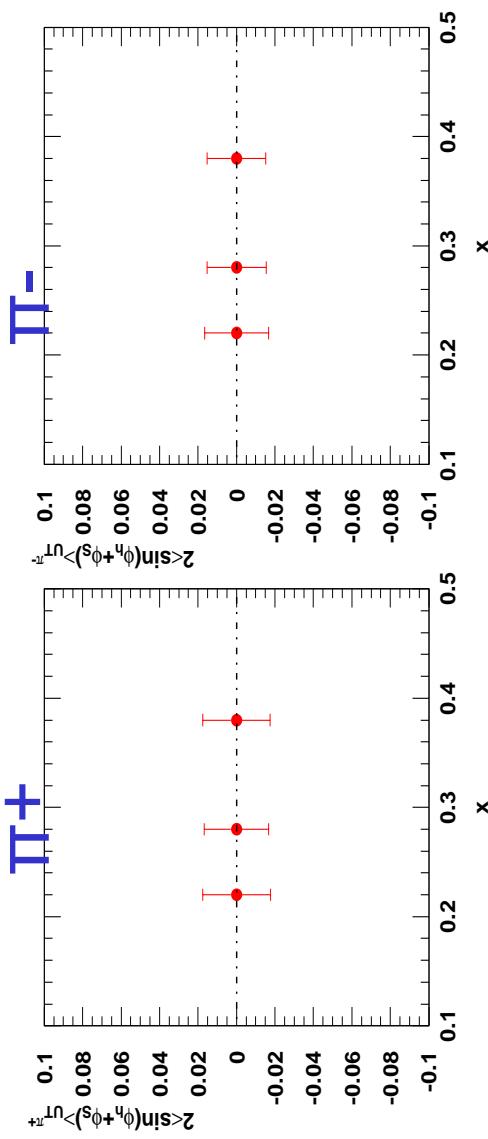
--Full Sivers/Collins angle coverage
with two target polarization direction

$$\phi_s \approx \frac{\pm 0.050}{\sin(\theta_e - \theta_q)}$$

$$\phi_{\text{Sivers}} \equiv \phi_h - \phi_s \approx \arcsin \frac{\pm 0.085 P_h}{P_\perp}$$

$$\phi_{\text{Collins}} \equiv \phi_h + \phi_s$$

Projected Results of Collins/Sivers Moments



- Statistical uncertainty for He raw asymmetry: ~0.1%
- Statistical uncertainty for neutron moments: ~2%

Systematic Uncertainties for SSA

- Statistical uncertainty for He raw asymmetry: ~0.1%

$$A_{meas} = \frac{N^+ - N^-}{N^+ + N^-}$$

- Spin-correlated luminosity: 0.1% in A \rightarrow 0.2% in x

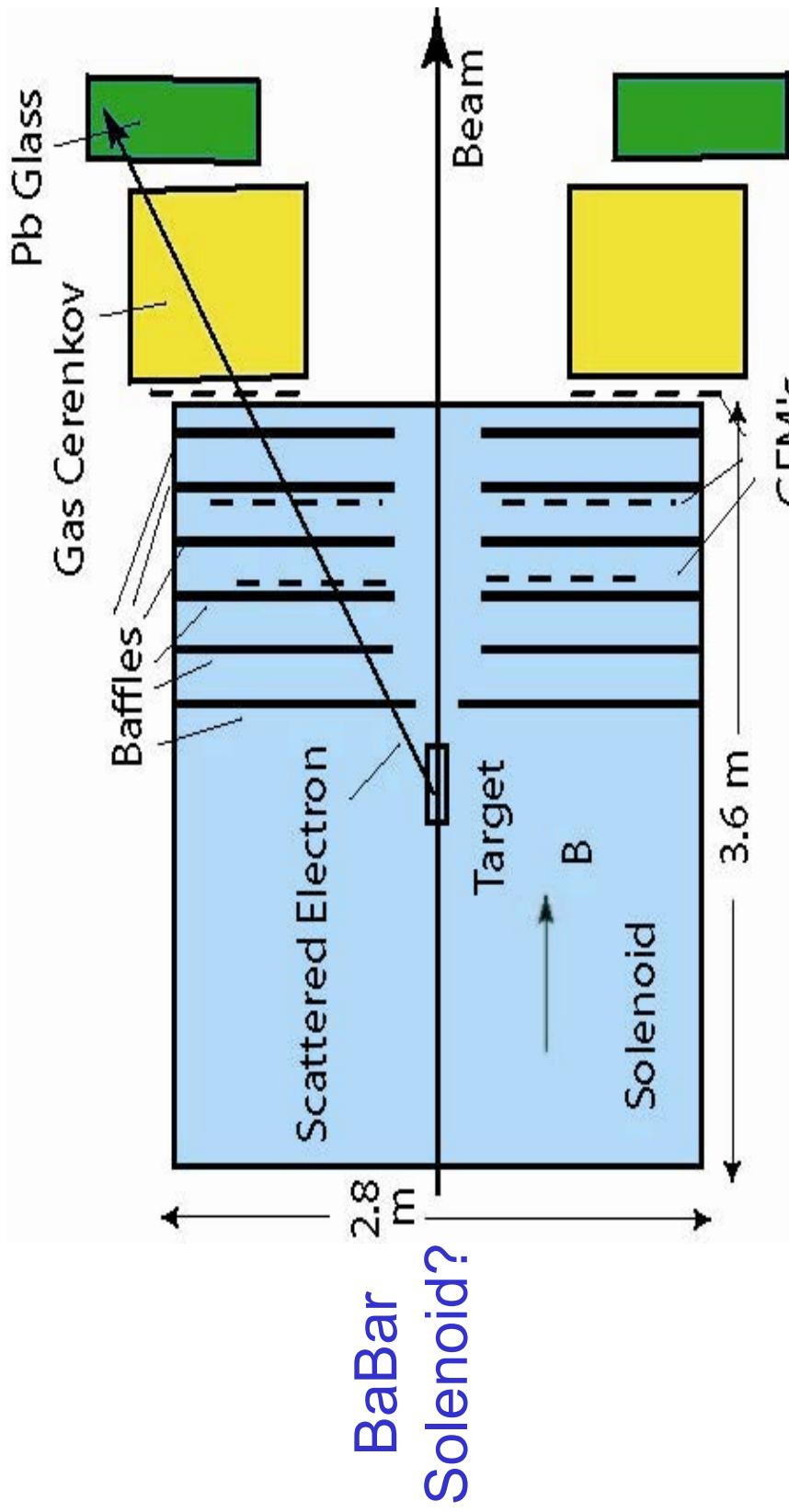
$$A_{true} = \frac{N^+ - N^- \cdot \frac{(1+x)}{(1+x)}}{N^+ + N^- \cdot \frac{(1+x)}{(1+x)}}, \quad \delta_x A \sim 0.5|x|$$

- Target polarization: 3% in y, 0.1% in A \rightarrow A < 3.4%

$$A_{true} = (1 + y) \cdot \frac{N^+ - N^-}{N^+ + N^-}, \quad \delta_y A = |y| A$$

Solenoid Option with 11 GeV beam

From J.P. Chen's talk at USTC in China, Aug. 2006



- Acceptance 10-30 times HMS+SHMS

- PID: Gas Cherenkov + Shower Counter

• Challenge: polarized ${}^3\text{He}$ target inside the solenoid

Summary

- HERMES transverse data show some surprising features, for example in Collins H^-/H^+ , Sivers f_{1T}^u/f_{1T}^d , and P_{hT} dependence. The current constraint on the transversity is pretty loose, and the x, z and P_T distributions are coupled together.
- More data especially with controlled kinematics are essential for cross check, multi-dimension binning and transversity extraction, ...
- The A-rated Hall A transversity experiment with polarized ${}^3\text{He}$ target will measure the pion(kaon) SIDIS target single-spin asymmetry on neutron with 6 GeV beam.
- JLab upgrade provides much larger phase space for SIDIS with higher beam energy. A few 12 GeV SIDIS experiments has been proposed, ex $\cos 2\phi$ measurement in Hall B, dbar/uubar and R measurement in Hall C using unpolarized target.
- Hall C with HMS/SHMS and especially ${}^3\text{He}$ target can contribute to the transversity program by studying target single-spin asymmetry of SIDIS at controlled kinematics, for example at fixed Q^2, x, z , and small P_T , complementary to Hall B's single-spin asymmetry program.
- The Hall A solenoid option with high luminosity and large acceptance sounds attracting.