

The Nucleus As A QCD Laboratory

G. A. Miller, U. W. Seattle

Outline

QCD View of the Nucleus- made of nucleons

QCD View of Nucleon (structure & shape)-
bound nucleon \neq free nucleon-not much

EMC effect & Drell Yan DY

Conventional hadron dynamics fails EMC/DY

nuclear modification of nucleon verified

3 models and consequences

Discovery of color transparency(CT) and observation of small size components in pions in the coherent diffraction: $\pi + A \rightarrow \text{jet}_1 + \text{jet}_2 + A$

Lessons for CT in π and ρ production

Why is the nucleus the way it is?

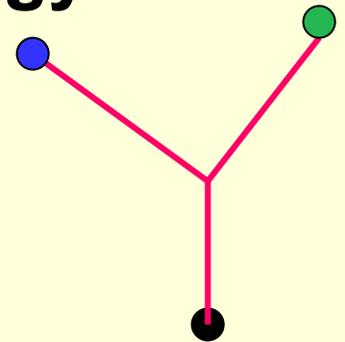
- $M(A) = Z M_p + N M_n$ **0.1% accuracy**
- nucleus is made of nucleons
- QCD says quarks and gluons

Puzzle – why?

Strong coupling QCD- SCQCD (Kogut & Susskind) GAMiller PRC39,1563

**Leading term - gluon electric field energy $\sim L$
length of **flux line****

**inert color singlets at rest- small
corrections yield Fermi motion, int's**



Finding corrections due to quarks, gluons vital

QCD view of the nucleon

- vacuum is bubbling cauldron of $q \bar{q}$ pairs
- nucleon is color singlet of quarks, gluons
- many configurations
- size: sometimes small, mostly average, sometimes **HUGE**
- Point Like Configs. PLC don't interact
- use nucleus to observe, change fluctuations

Phenomenological view of nucleon- need relativistic model of free wave function

- 3 quark anti-symmetric
- relative variables, frame independent
- eigenstate of spin operator- rotational invariant
- reduces to non-relativistic if $m \rightarrow \infty$

$$\Psi = \Phi(M_0^2) u(p_1) u(p_2) u(p_3 = K) \psi(s_i, t_i) \text{ Terentev, Coester}$$

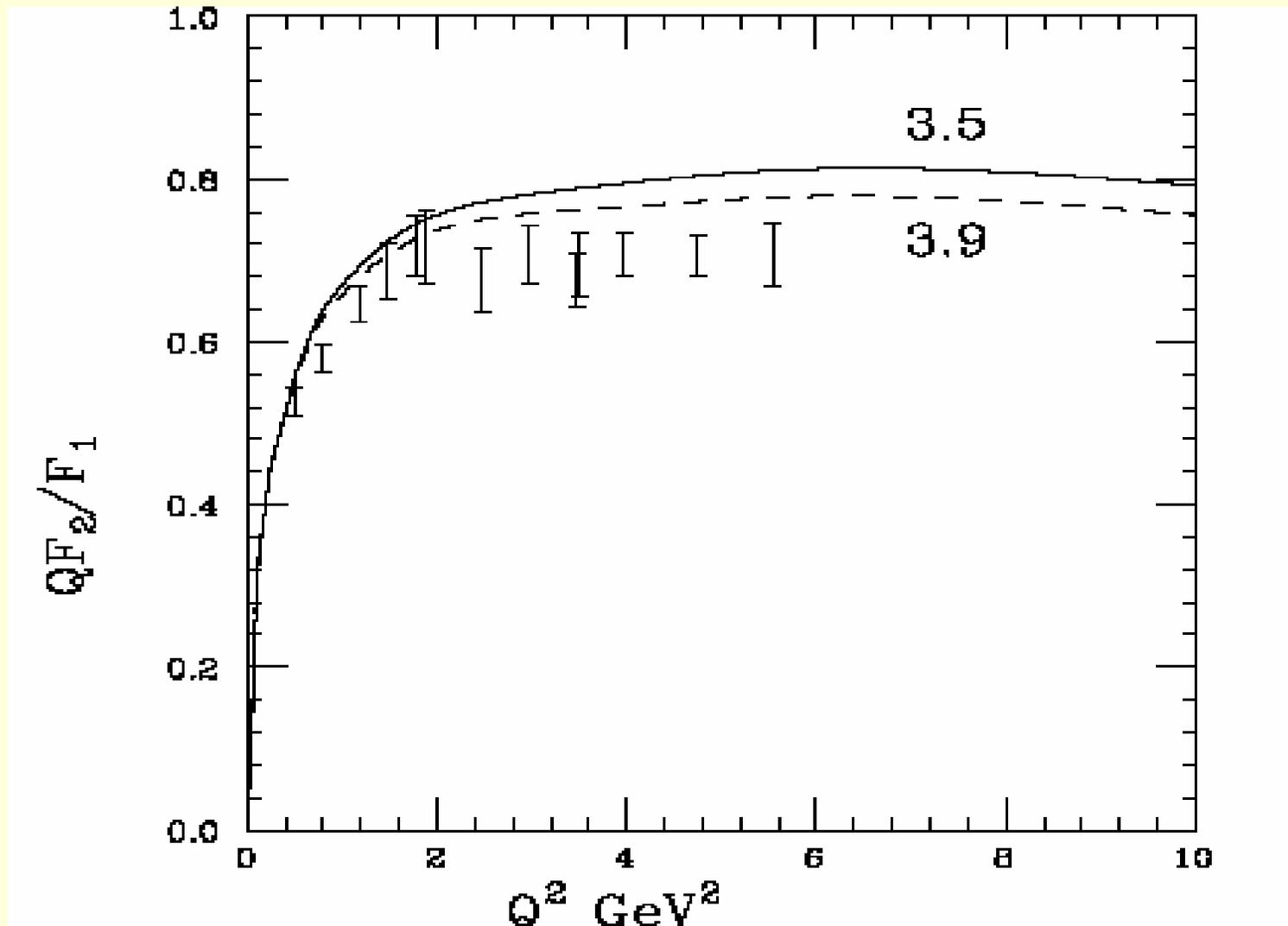
spatial dist DIRAC SPINORS spin-ispin color amp

Schlumpf Mom space wf $\Phi(M_0) = N / (M_0^2 + \beta^2)^\gamma$

$$\beta = 0.607 \text{ GeV} \quad \gamma = 3.5 \quad m = 0.267 \text{ GeV}$$

$$M_0^2 = s(p_1, p_2, p_3)$$

Ratio: Pauli/Dirac form factors calculation '95 data 2000



Relativistic Explanation-Proton

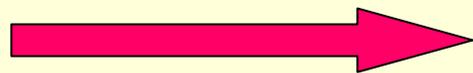
J^+ acts on third quark, other two have 0 spin

$$u(K, s) = \begin{pmatrix} (E(K) + m)|s\rangle \\ \boldsymbol{\sigma} \cdot \mathbf{K}|s\rangle \end{pmatrix}$$

$\sigma_y|s\rangle$: quark spin \neq proton ang mom

lower components $\equiv L_z \neq 0$

In calculating overlap, K is of order Q



Q $F_2/F_1 \approx$ constant

Spin-dependent density

- **Spin dependent densities**
probability that quark has given momentum \mathbf{K} and spin in direction \mathbf{n}

$$\hat{\rho}(\mathbf{K}, \mathbf{n}) = \int \frac{d^3r}{(2\pi)^3} e^{i\mathbf{K}\cdot\mathbf{r}} \bar{\psi}(\mathbf{r}) \frac{\hat{Q}}{e} (\gamma^0 + \boldsymbol{\gamma} \cdot \mathbf{n} \gamma_5) \psi(\mathbf{0})$$

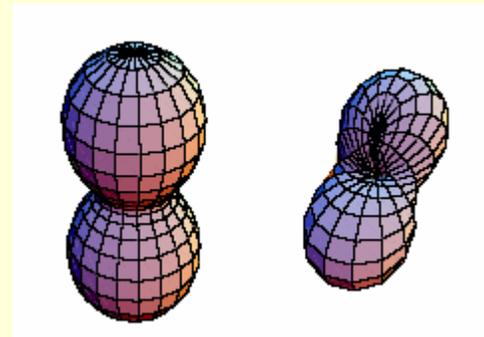
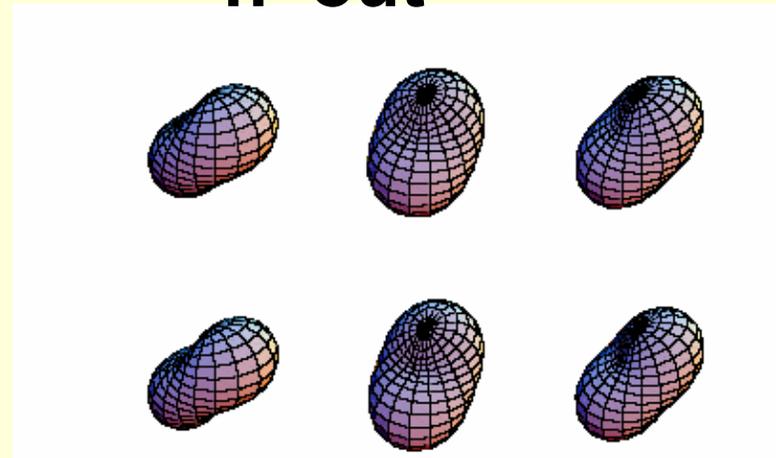
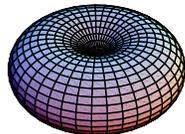
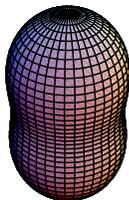
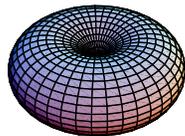
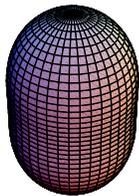
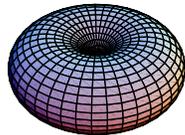
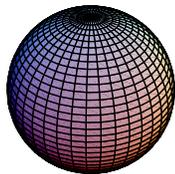
take matrix elements in proton at rest

Shapes of the proton

n parallel

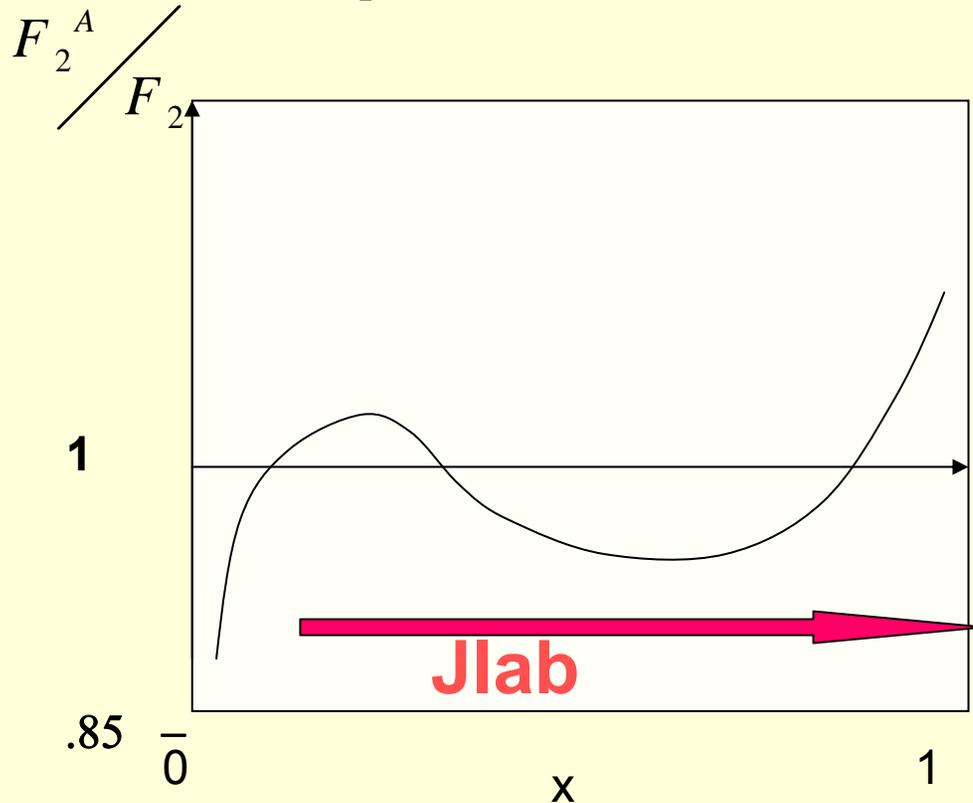
$-n$ parallel

n out



lattice calculations- Negele looking

Deep Inelastic Nuclear Scattering Experiments EMC, SLAC, NMC



$$\frac{F_2^A(x)}{A F_2^N(x)} = 1 + g_{F_2}(x) \mathcal{G}(A)$$

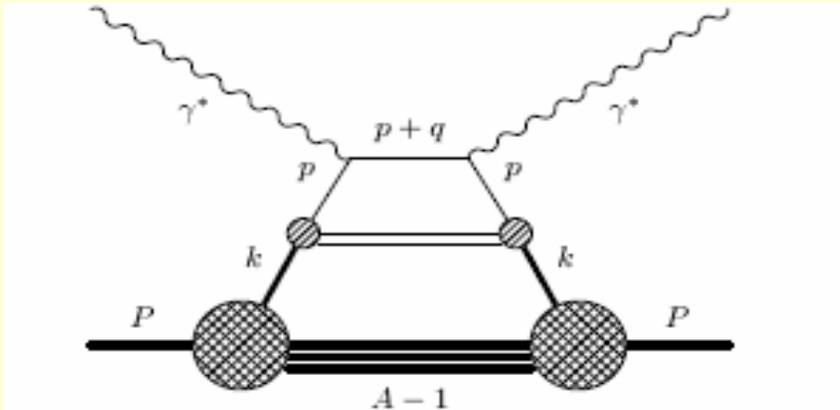
Chen Detmold '05

Bruell

Nucleon structure is modified: valence quark momentum depleted, sea or gluon enhanced. **How do quarks work in a nucleus?**

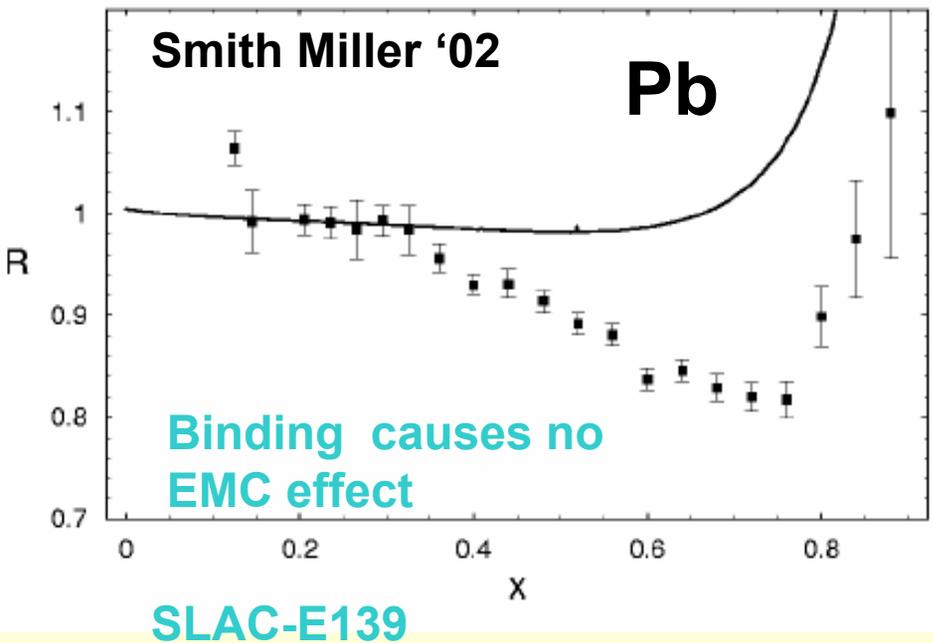
EMC – “Everyone’s Model is Cool (1985)”

Deep Inelastic scattering from nuclei- nucleons only free structure function



$$\frac{F_{2A}(x_A)}{A} = \int_{x_A}^A dy f_N(y) F_{2N}(x_A/y)$$

$$y = A k^+ / P^+$$



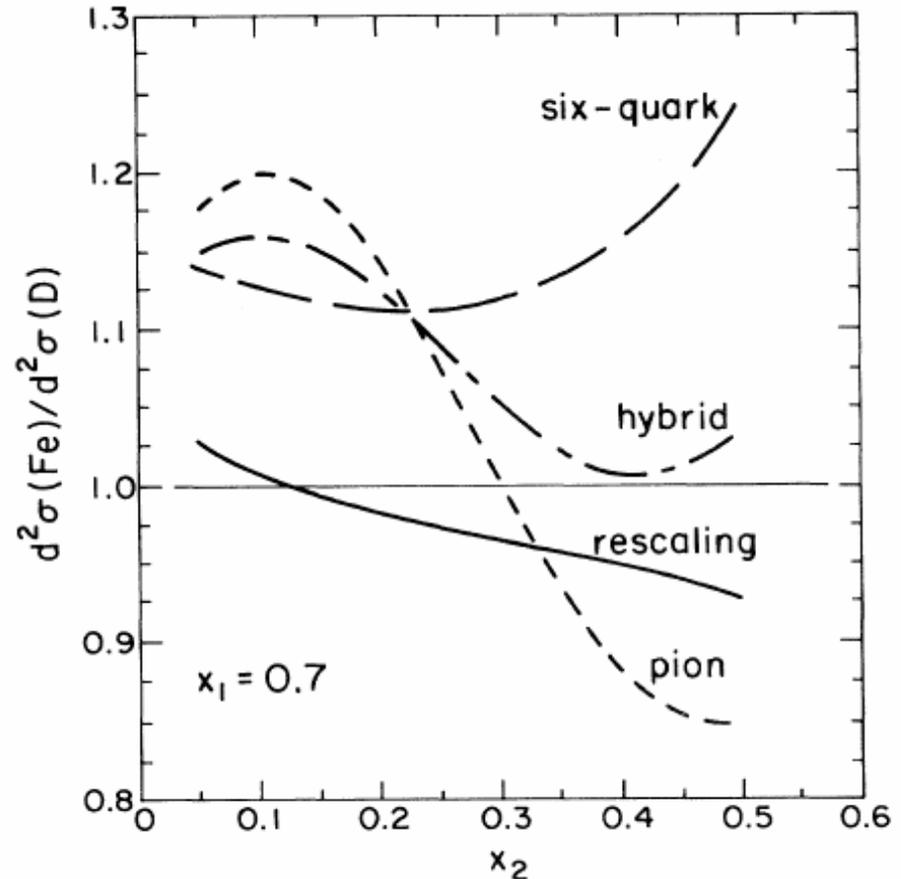
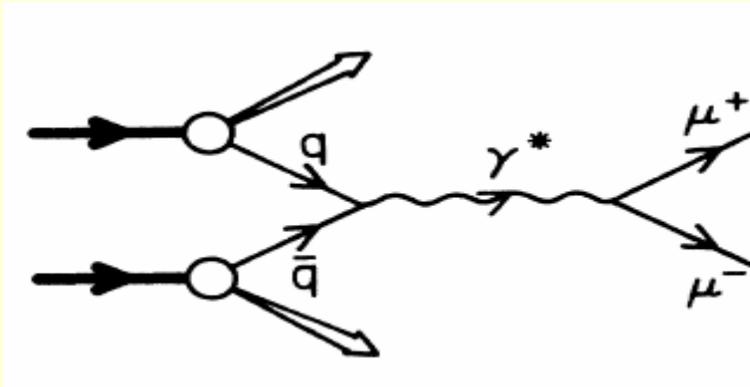
- Hugenholz van Hove theorem nuclear stability implies (in rest frame) $P^+ = P^- = M_A$
- $P^+ = A(M_N - 8 \text{ MeV})$
- average nucleon $k^+ = M_N - 8 \text{ MeV}$, $y \rightarrow 1$
- $F_{2A}/A \sim F_{2N}$ no EMC effect

Nucleons and pions

$$P_A^+ = P_N^+ + P_\pi^+ = M_A$$
$$P_\pi^+ / M_A = .04, \text{ explain EMC}$$

try Drell-Yan, Bickerstaff, Birse, Miller 84

proton(x_1) nucleus(x_2)

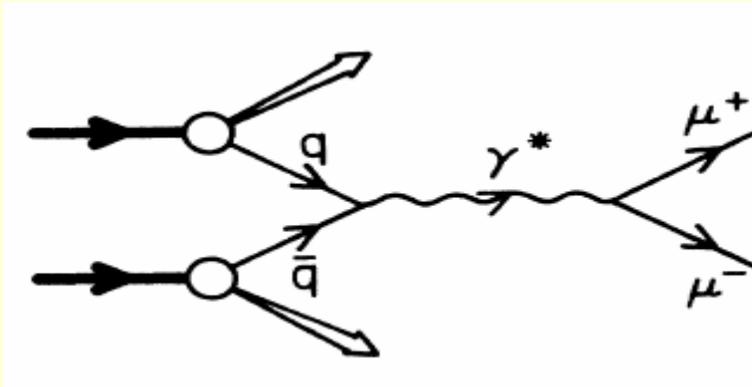


Nucleons and pions

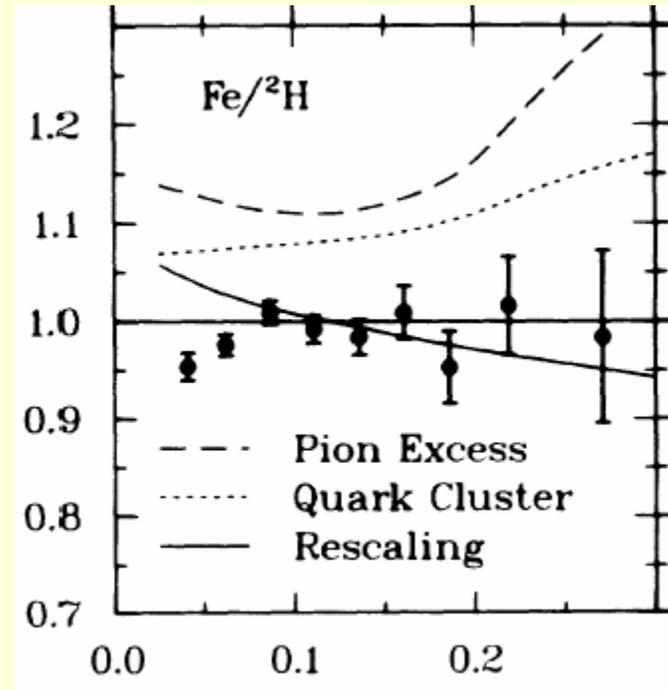
$$P_A^+ = P_N^+ + P_\pi^+ = M_A$$

$$P_\pi^+ / M_A = .04, \text{ explain EMC}$$

Drell-Yan, E772

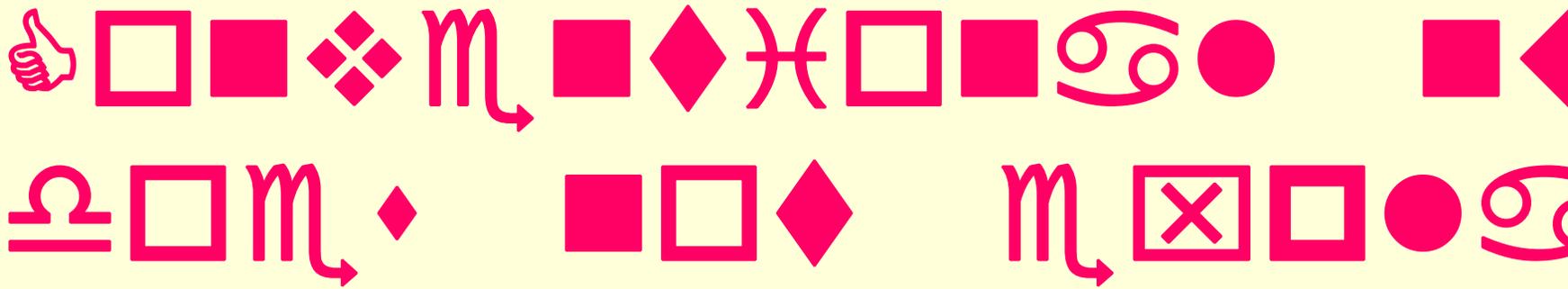


No one's
model is cool



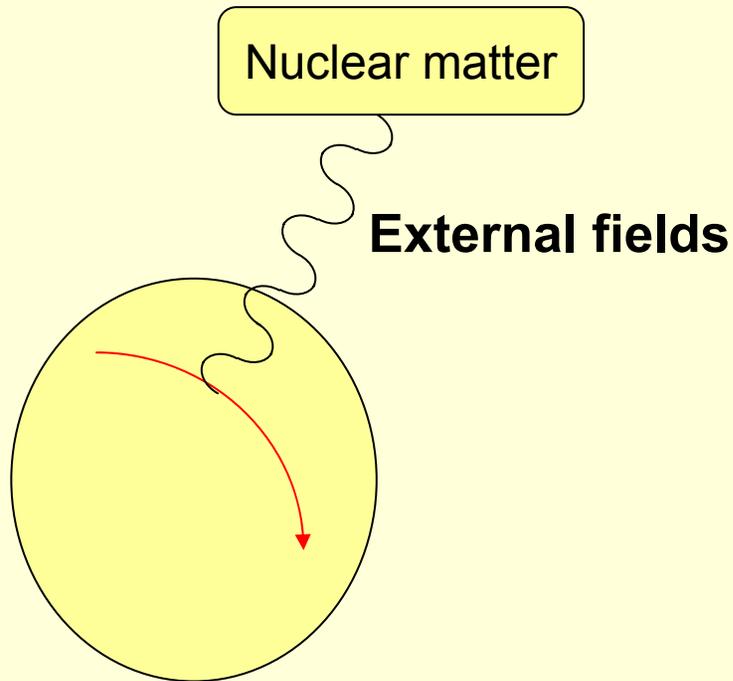
π
fails

Bertsch, Frankfurt, Strikman “crisis in nuclear theory” conventional physics does not work



-
- It's ~ easy to explain one or the other
 - Intrinsic structure of nucleon is changed
 - start with models-requirements
 - Model free distributions (valence, sea, support)
 - Consistency with nuclear properties
 - Describe deep inelastic and di-muon production data- valence plus sea
 - Predict new phenomena based on medium modified nucleons

Nucleon in medium- 3 models



1. **QMC- quarks in nucleons (MIT bag, NJL) exchange mesons with nuclear medium**
2. **CQSM- quarks in nucleons (soliton) exchange infinite pairs of pions, vector mesons with nuclear medium, sea**
3. **Suppression of point-like-configurations Frankfurt, Strikman**

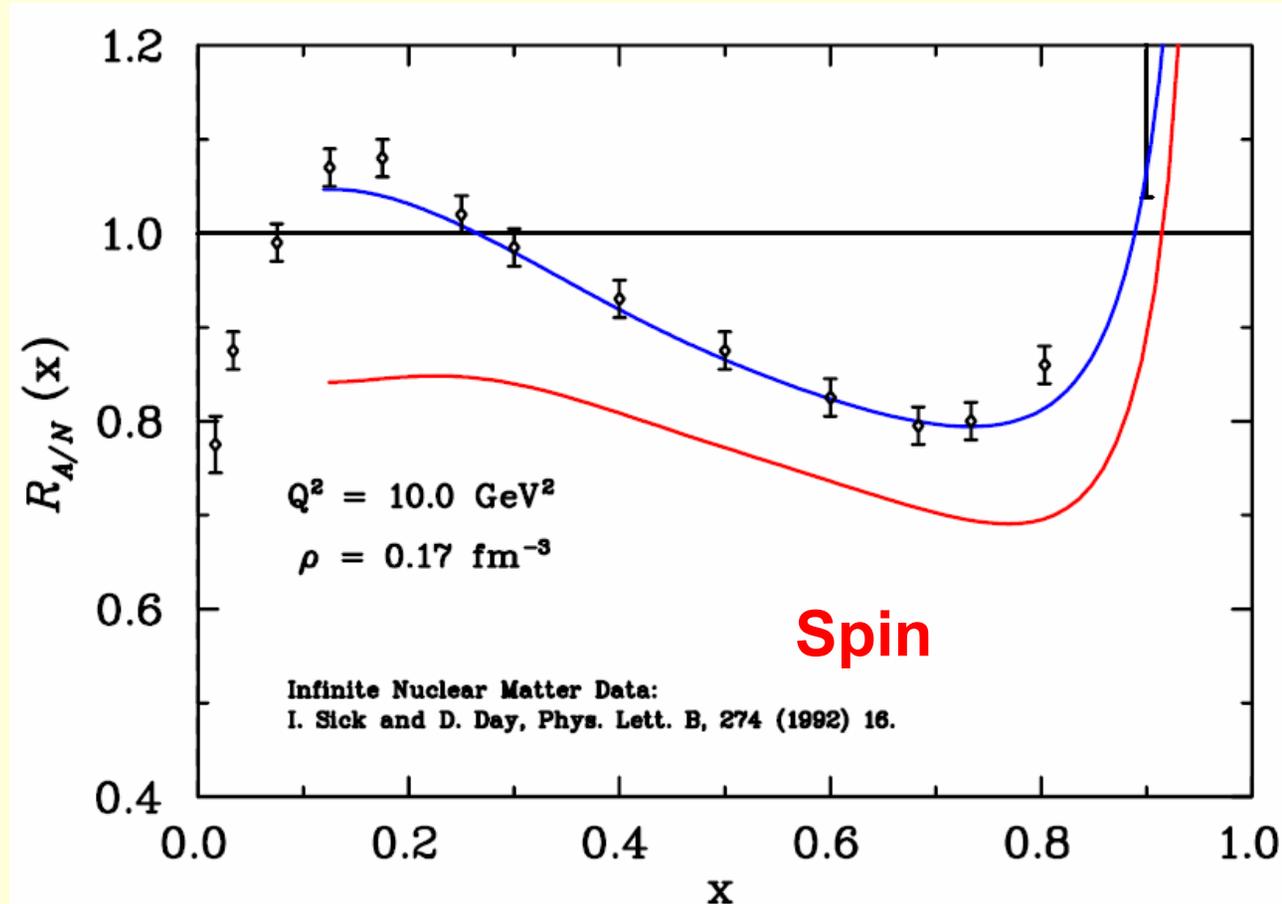
Spin experiments enhance EMC?

- g_{1n} , g_{1p} in nuclei

Bentz, Cloet, Thomas

ratio of g_1
medium
to free

Infinite Nuclear
Matter



Quark Soliton Model —

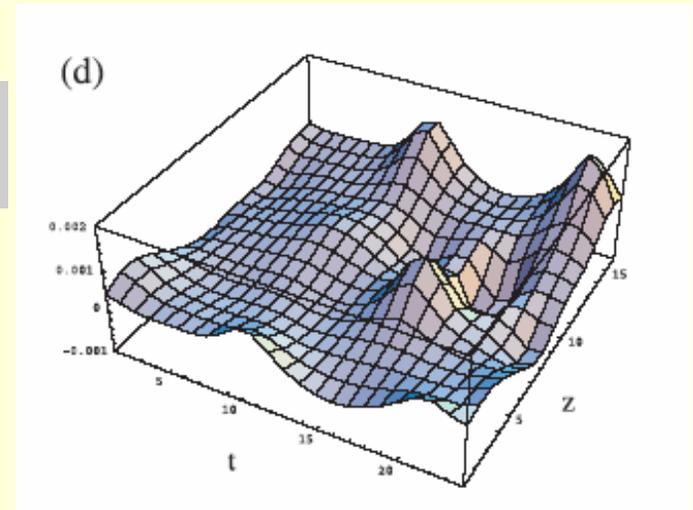
Diakonov, Petrov, Polykov, **Gamberg, Weigel**

- Instanton dominated vacuum
- quarks with spontaneously generated masses interact with pions

Negele et al hep-lat/9810053
topological charge density

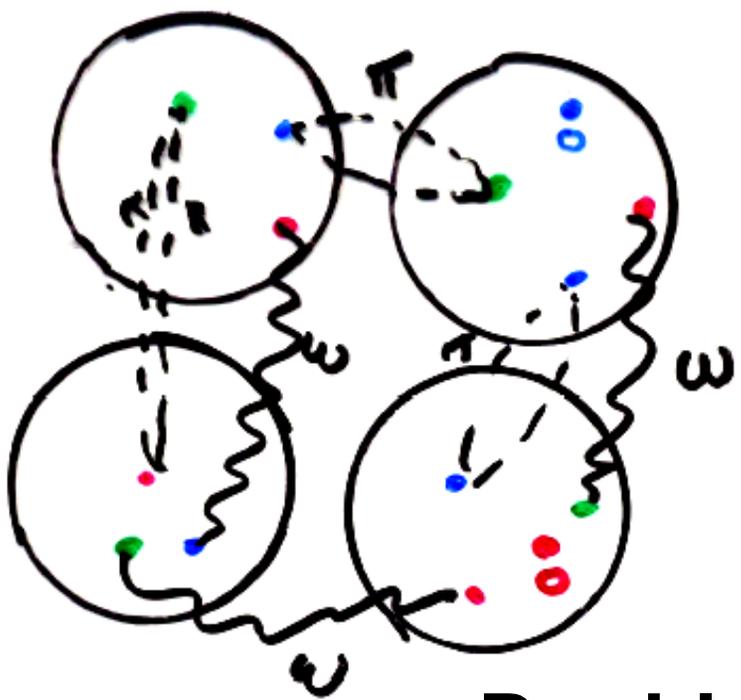
$$\mathcal{L}_{\text{eff}} = \bar{q} \left[i \not{\partial} - M \exp(i \gamma_5 \pi^A \lambda^A / F_\pi) \right] q,$$

- Nucleon is soliton in pion field $\pi(r)$
- $M=420$ MeV
- good nucleon properties, distribution functions rest and infinite momentum frames



Chiral Quark Soliton Model of Nucleus-

Smith, Miller

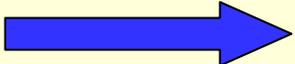


2π exchange – attraction

ω (vector meson) exchange -

repulsion

Double self consistency

profile function and k_f 

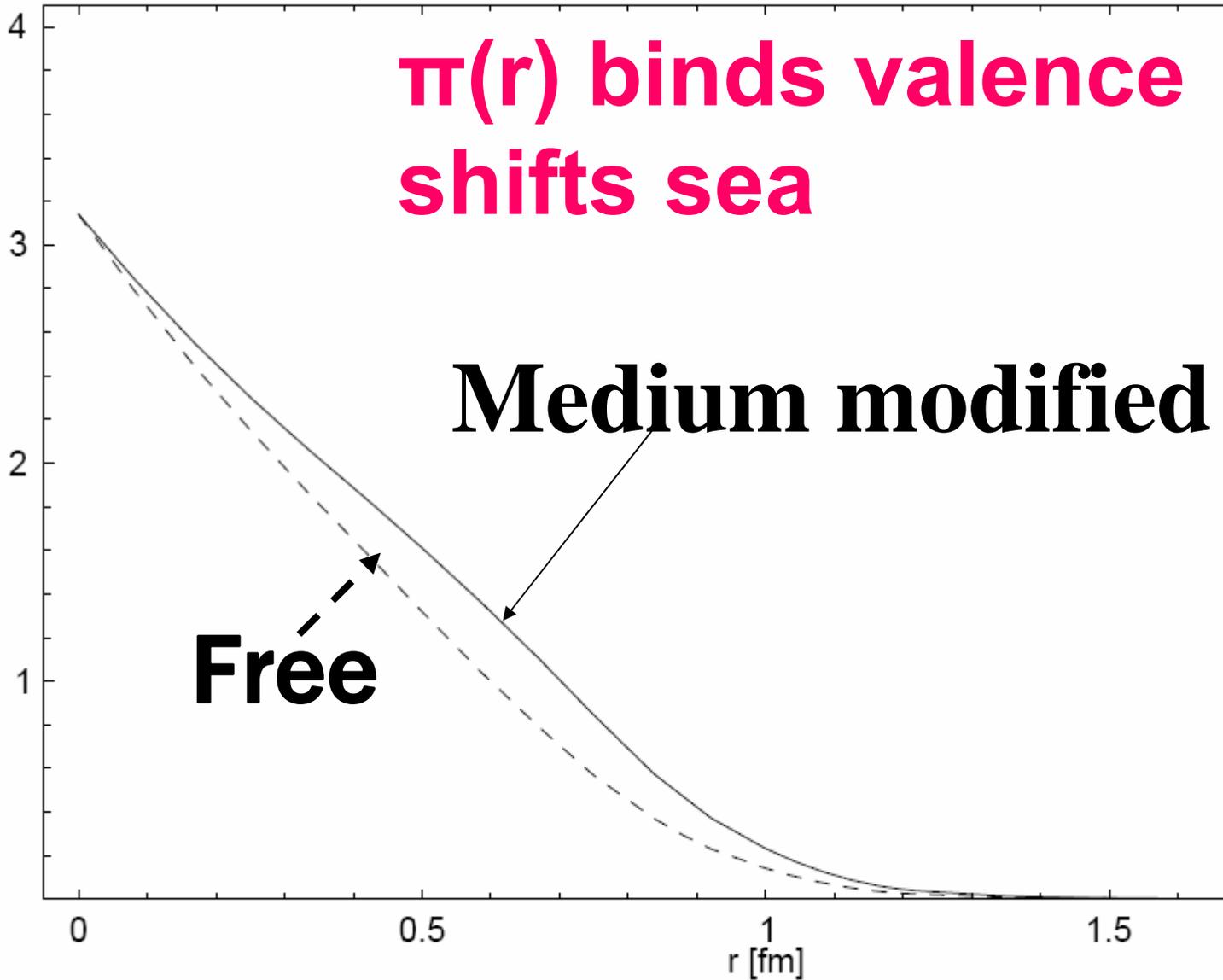
good nuclear saturation

Profile Function

$\pi(r)$ binds valence
shifts sea

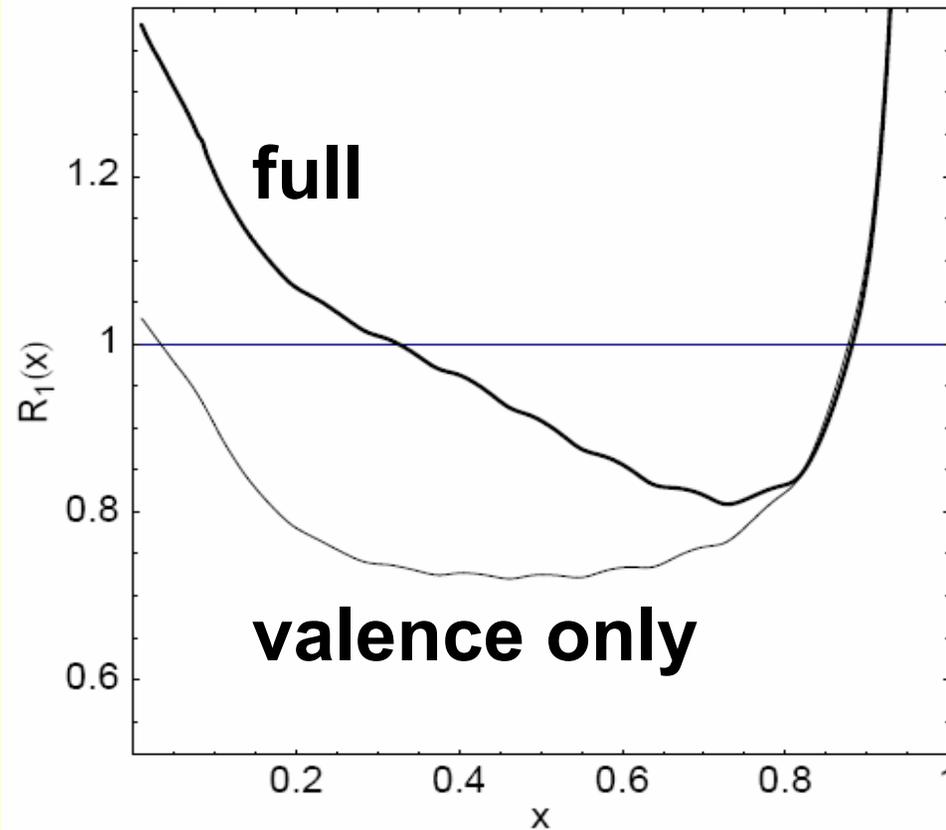
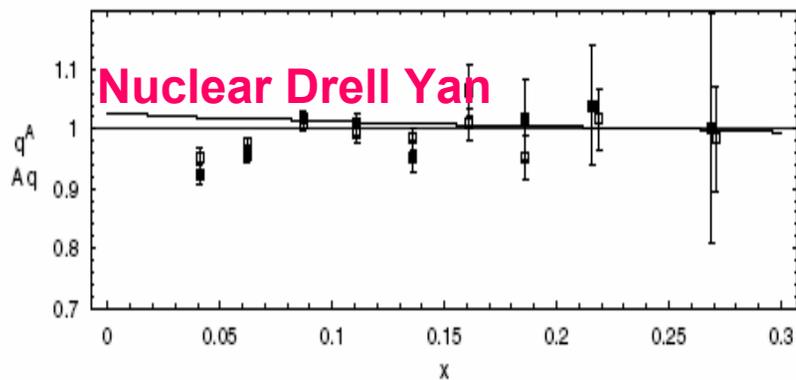
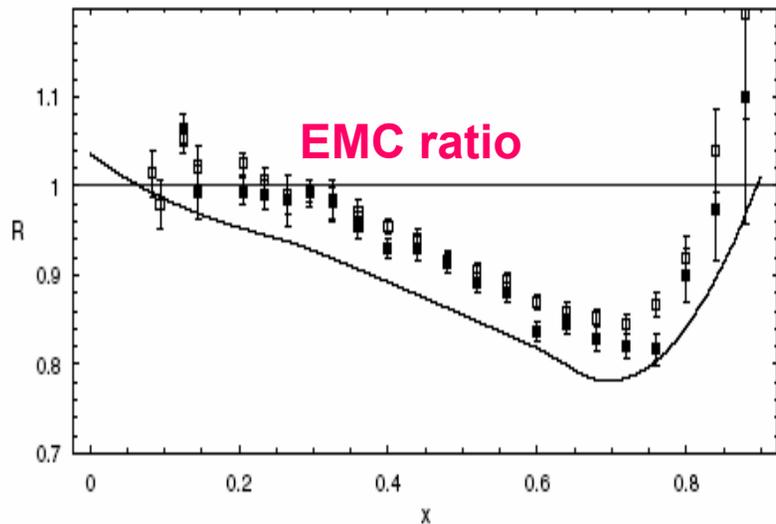
Medium modified

Free



Results Smith & Miller '03,04,05

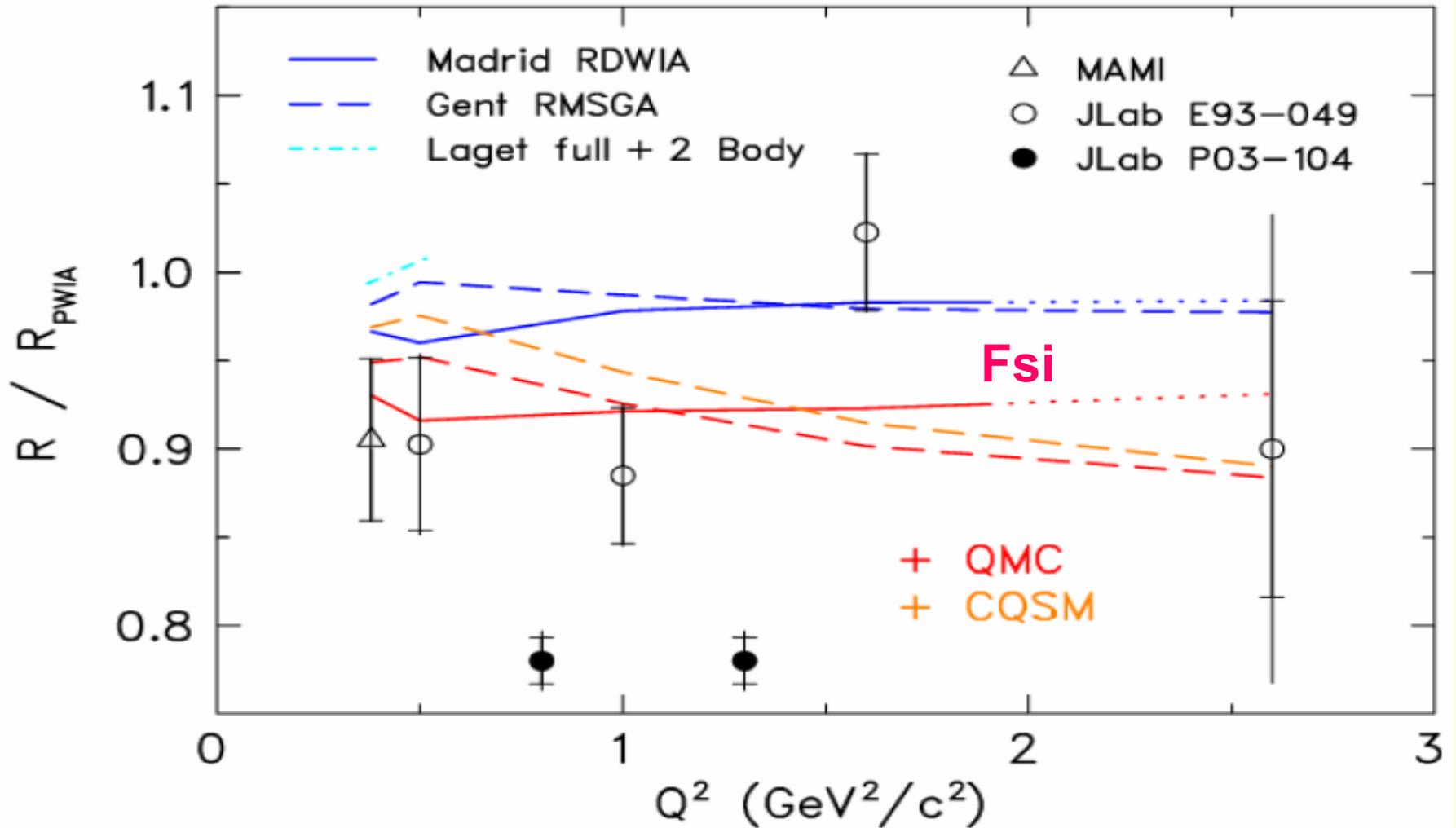
g_1 ratio



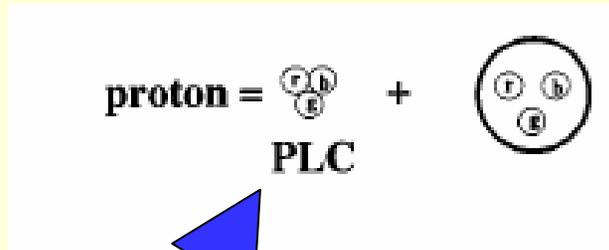
sea is not much modified

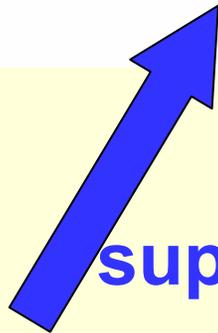
Polarization transfer in $^4\text{He}(e,e'p)$ Nucleon form factors in medium – G_E/G_M ratios

Strauch

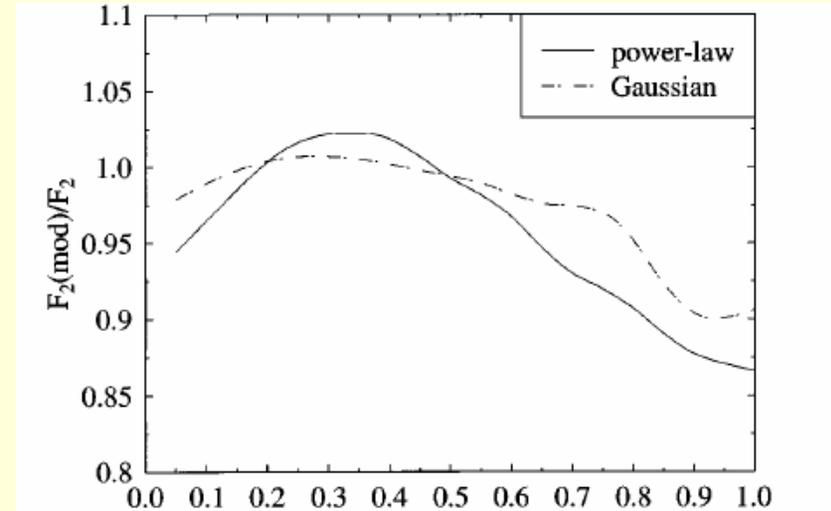


Suppression of Point Like Configurations

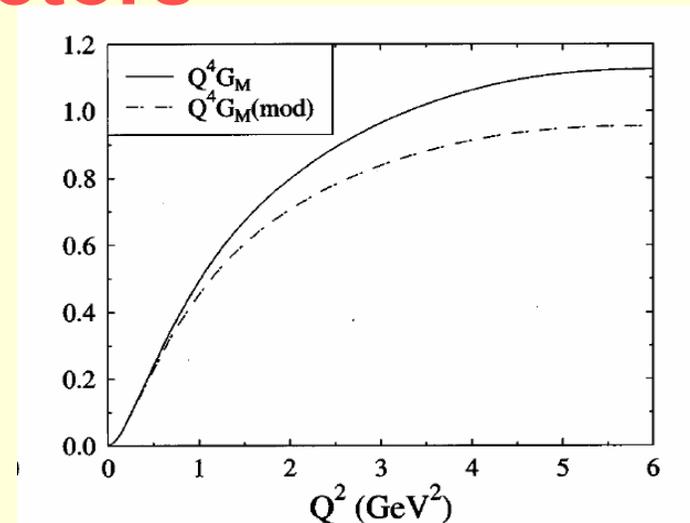
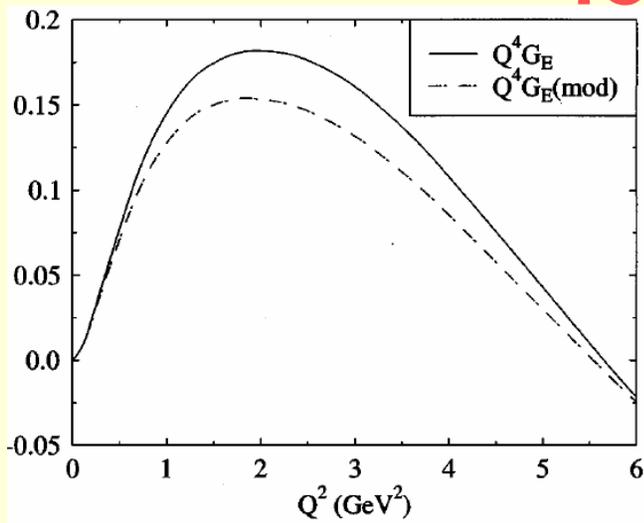


 suppressed

DIS



form factors

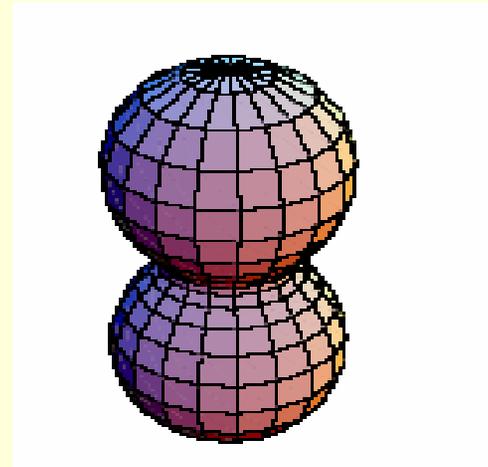


Medium modified form factors -

Challenge:

- Should be there in any model-how to really nail it experimentally ???

high accuracy data, independent assessment of FSI



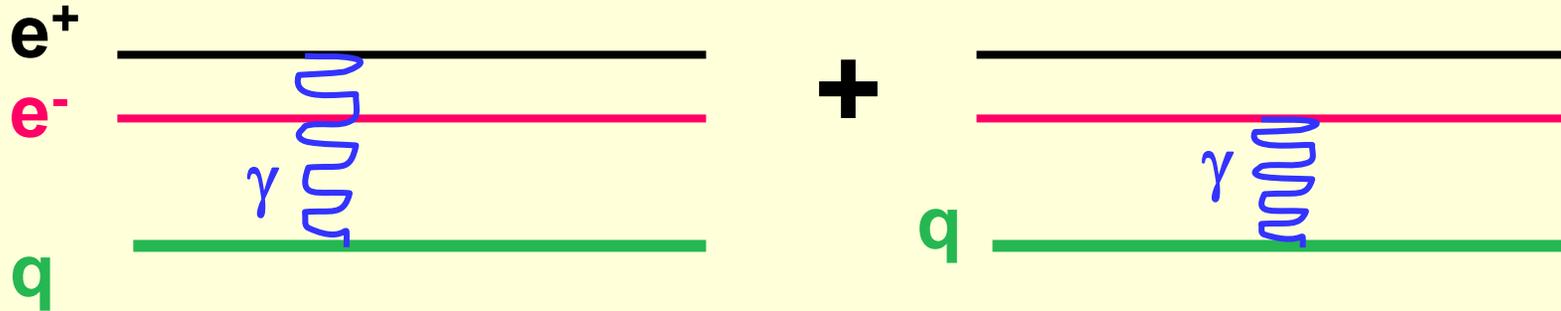
Suppression of PLC in reactions – Color Transparency

Reduced initial, final state interactions in high Q^2 **quasielastic** nuclear reactions (p, Xp), $(e, e'p)$, (e, e', π) , $(\pi + A \rightarrow \text{jet} + \text{jet} + A, \text{FermiLab})$

WHY?

1. high Q^2 hadronic **exclusive** reactions proceed by PLC formation-Brodsky, Mueller '82
2. PLC have small scattering amplitudes-gluon emission amplitudes cancel- **coherent**
3. PLC expands as it moves
Jennings & Miller '90, '91

Charge neutrality and coherence



Same final state exclusive:

$$V = e q / r_+ - e q / r_- = e q (r_- - r_+) / (r_+ r_-) \quad \text{dipole}$$

COHERENCE – does your experiment maintain coherence?

Strong int'n- two gluon

exchange → dipole?
inclusive – square amplitudes first then add,

no cancellation

Gluonic strong interaction

$$\sigma = C d^2$$

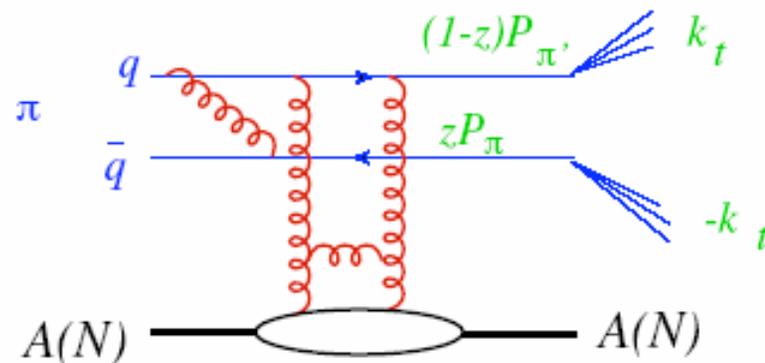
$\lambda/d^2 \sim$ sometimes called Q_{eff}^2

$$\pi + N(A) \rightarrow \text{"2 high } p_t \text{ jets"} + N(A)$$

Mechanism:

Pion approaches the target in a **frozen** small size $q\bar{q}$ configuration and scatters **elastically** via interaction with $G_{\text{target}}(x, Q^2)$.

- ❖ First attempt of the theoretical analysis of πN process - Randa 80 - power law dependence of p_t of the jet (wrong power)
- ❖ First attempt of the theoretical analysis of πA process - Brodsky et al 81 - exponential suppression of p_t spectra, weak A dependence ($A^{1/3}$)
- ❖ pQCD analysis - Frankfurt, Miller, MS 93; elaborated arguments related to factorization 2003



a dominant term

1993 predictions Frankfurt, Miller, Strikman

$$M(A) = A e^{t R(A)} M(N) , \sigma(A) \sim A^{4/3} + O(1/k^2) \sim A^{1.55}$$

$$\frac{d\sigma(z)}{dz} \propto \phi_\pi^2(z) \approx z^2(1-z)^2 \quad \text{where } z = E_{jet_1}/E_\pi.$$

$$k_t \text{ dependence: } \frac{d\sigma}{d^2k_t} \propto \frac{1}{k_t^n}, n \approx 8 \text{ for } x \sim 0.02$$

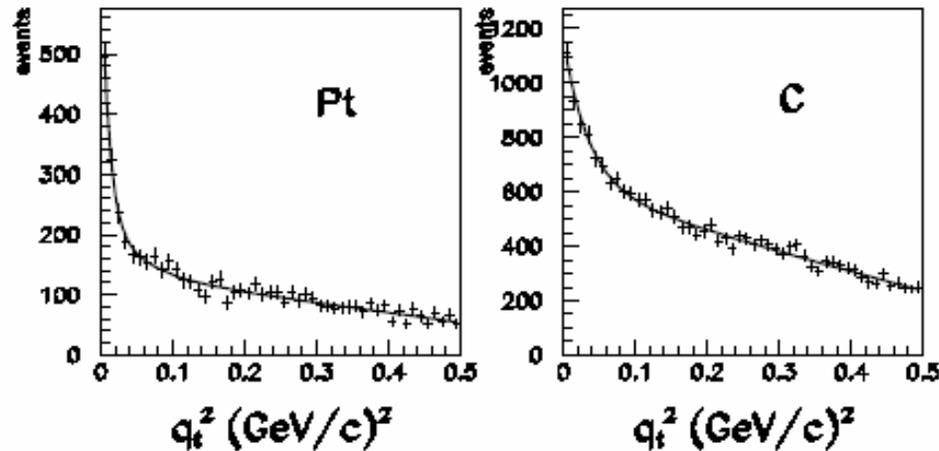
$$k_t > 1.5 \text{ GeV}/c$$

Naive expectation $M(A) \sim A^{1/3}$ (nuclear path length), **inelastic diffraction FMS93: $M(A) \sim A^{.7}$**

E791 results

The E-791 (FNAL) data $E_{inc}^\pi = 500\text{GeV}$ (D.Ashery et al, PRL 2000)

♡ Coherent peak is well resolved:



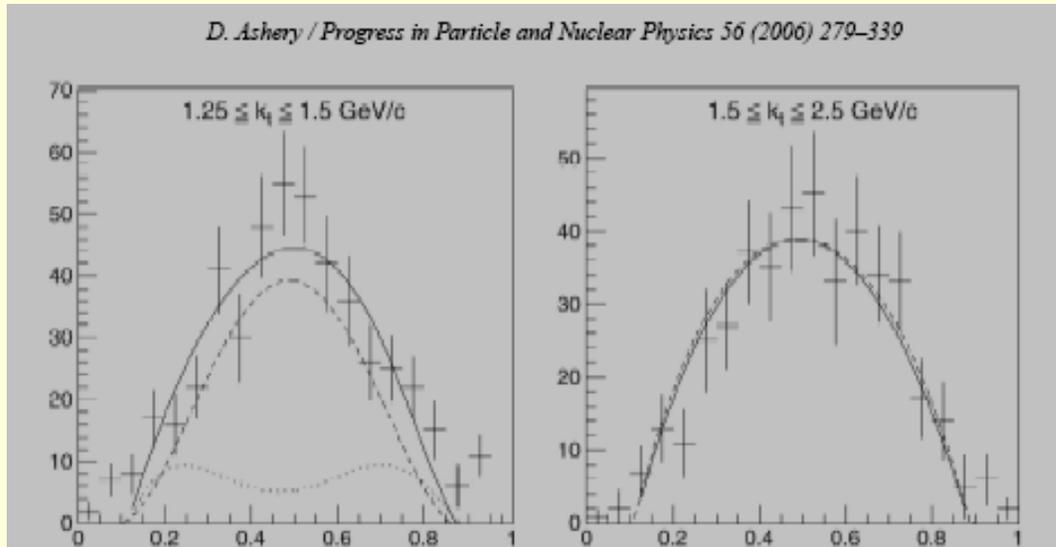
♡♡ Observed A-dependence $A^{1.61 \pm 0.08}$ $[C \rightarrow Pt]$

FMS prediction $A^{1.54}$ $[C \rightarrow Pt]$ for large k_t & extra small enhancement for intermediate k_t .

For soft diffraction the Pt/C ratio is ~ 7 times smaller!!

More E791

z dependence

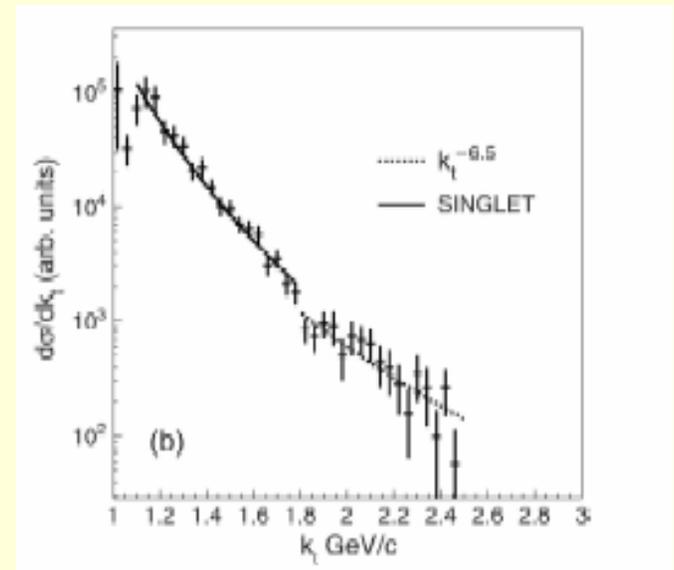


z

z

Consistent
with $(z(1-z))^2$

k_t dependence



$d\sigma/dk_t \sim k_t^{-7}$ theory

E791 summary

- **Color transparency discovered**
- **seen clearly for $k_t=1.8, 2.3$ GeV/c**
- **corresponds to $Q^2=3.2, 5.3$ GeV²**
- **p_π is large –no expansion**
- **small effects at Jlab6 should be strong signals at Jlab12**

Color Transparency in π reactions

- **(e,e' π) – hope to make pionic PLC**
- **normal sized pion does not interact with PLC hadron-chiral transparency**

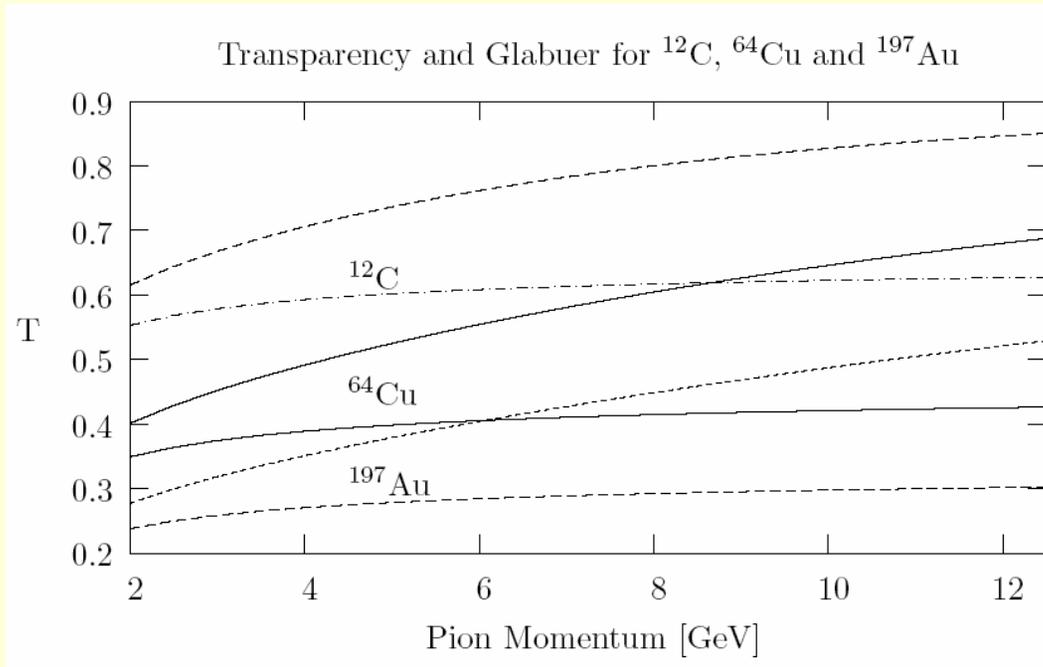
PRC 55,909 (97) Lee + FMS

- **consequence: point like “ ρ ” configurations do **not** decay to two π**

Pion color transparency Jlab 6,12

$(e,e', \pi): \gamma^*$ makes pion PLC (expands)

E01-107



**Larson,
Miller,
Strikman
'06**

Good at 6 (theory ~ data), better at 12

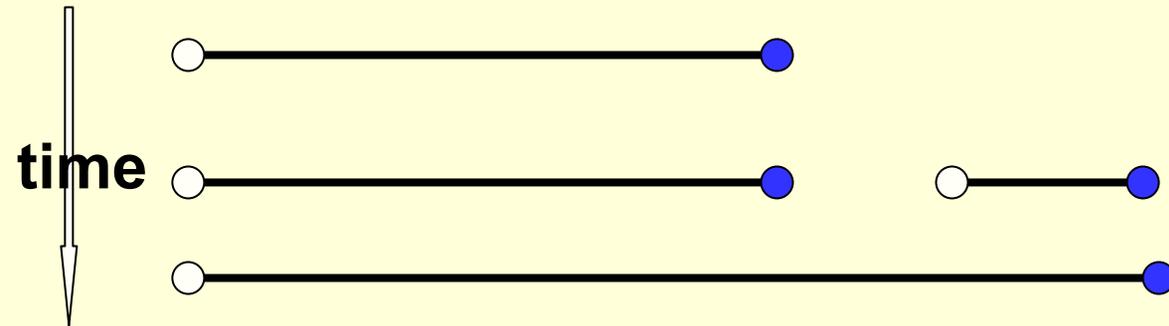
Summary

- nucleon structure is modified by nucleus
 - minimum model requirements- EMC, DY, nuclear saturation
 - predict new phenomena
 - needed –experimental tests –form factors in medium, ($eA \rightarrow e' X N$) spectator tag
- BONUS**
- color transparency for mesons!

Remainder are spares

QCD view of Nucleus?

- Kinetic energy via meson cloud flux tube breaks



- Interactions by meson exchange
confinement, flux string, color singlet clusters
leading order: inert nucleons sit

SCQCD

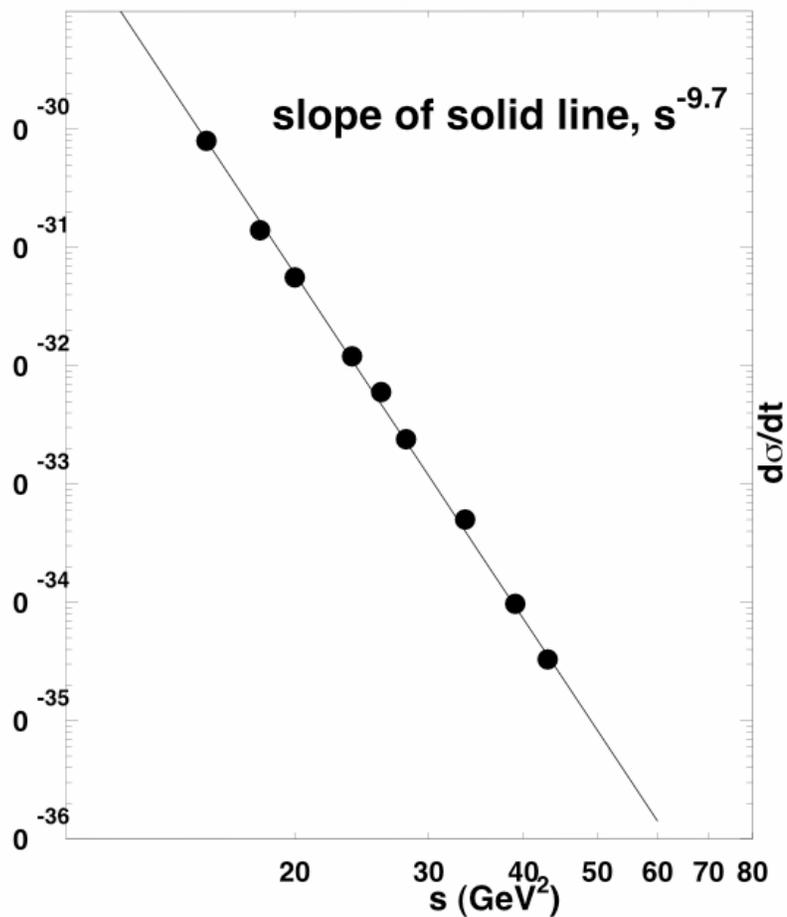


meson exchange model
of nuclei, GAM
PRC39,1563

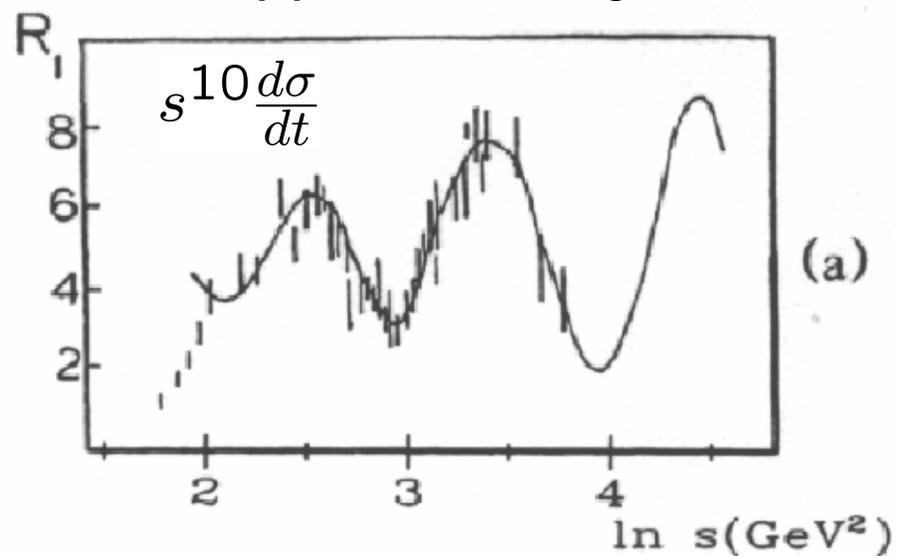
**quark, gluon effects
hard to find, but vital**

QCD Oscillations and Nuclear Filtering

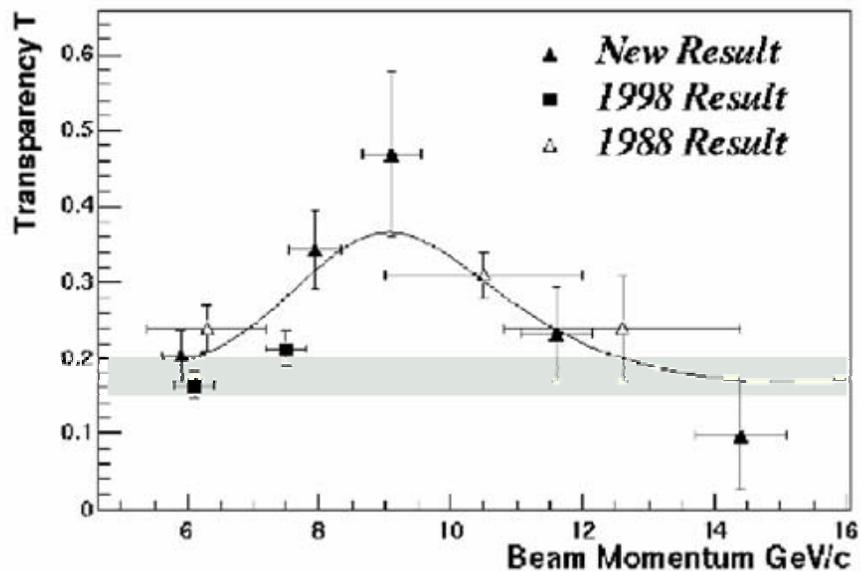
p-p scattering at 90° CM angle



p-p elastic scattering



BNL A(p,2p)



Quark Meson Coupling Model – Guichon, Thomas, Saito plus more

Nuclear matter

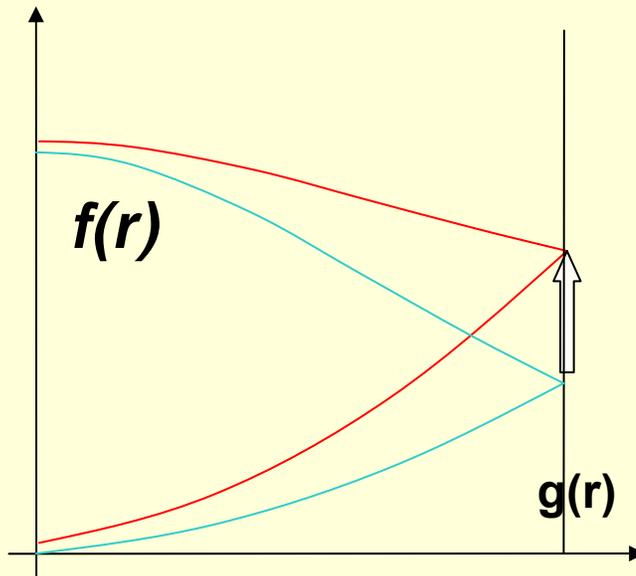
External fields σ, ω

$$m_q \triangleright m_q - g_\sigma \sigma \text{ (attraction)}$$

$$E_q \triangleright E_q + g_\omega \omega \text{ (repulsion)}$$

Quark field

$$\psi_q(x) = e^{iE_q t} \begin{pmatrix} f(r) \\ i\vec{\sigma} \cdot \hat{r} g(r) \end{pmatrix} \chi_{1/2}$$

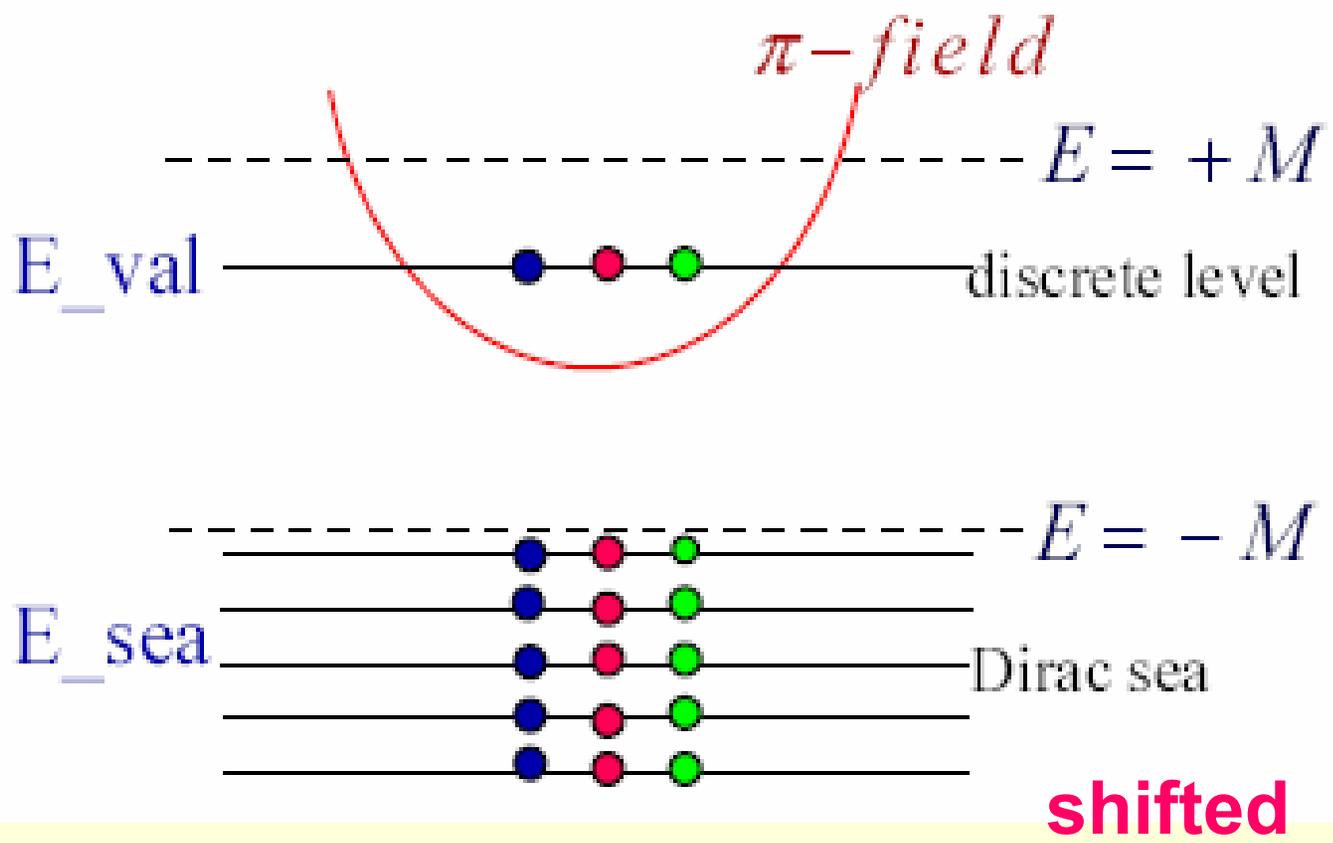


← scalar field effect, lower component loc enhanced

Single nucleon modification by nuclei

- Does it make sense?
- Neutron in nucleus is modified, **lifetime** changed from **15 minutes** to **forever**
- Binding changes energy denominator, suppresses $|pey\rangle$ component
- Change energy denominator change wave fun
- Strong fields **polarize** nucleons- analog of Stark effect, induces **dipole** moment of atom
- Nuclei: no direction - monopole polarization

Quark energy levels in π field



Enhancing EMC-spin independent

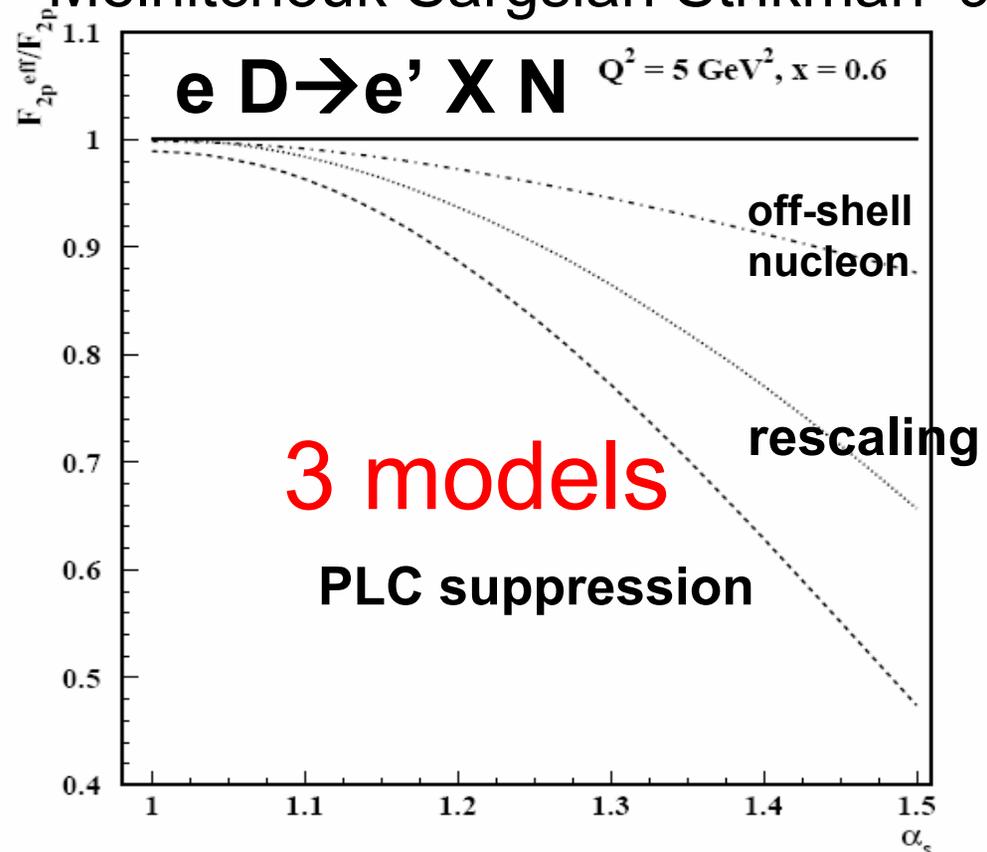
Tagged structure functions (measurement of a nucleon from the target fragmentation region in coincidence with the outgoing electron) with the goal of directly observing the presence of non-nucleonic degrees of freedom in droplets of superdense matter.

Ratio
bound to free F_2

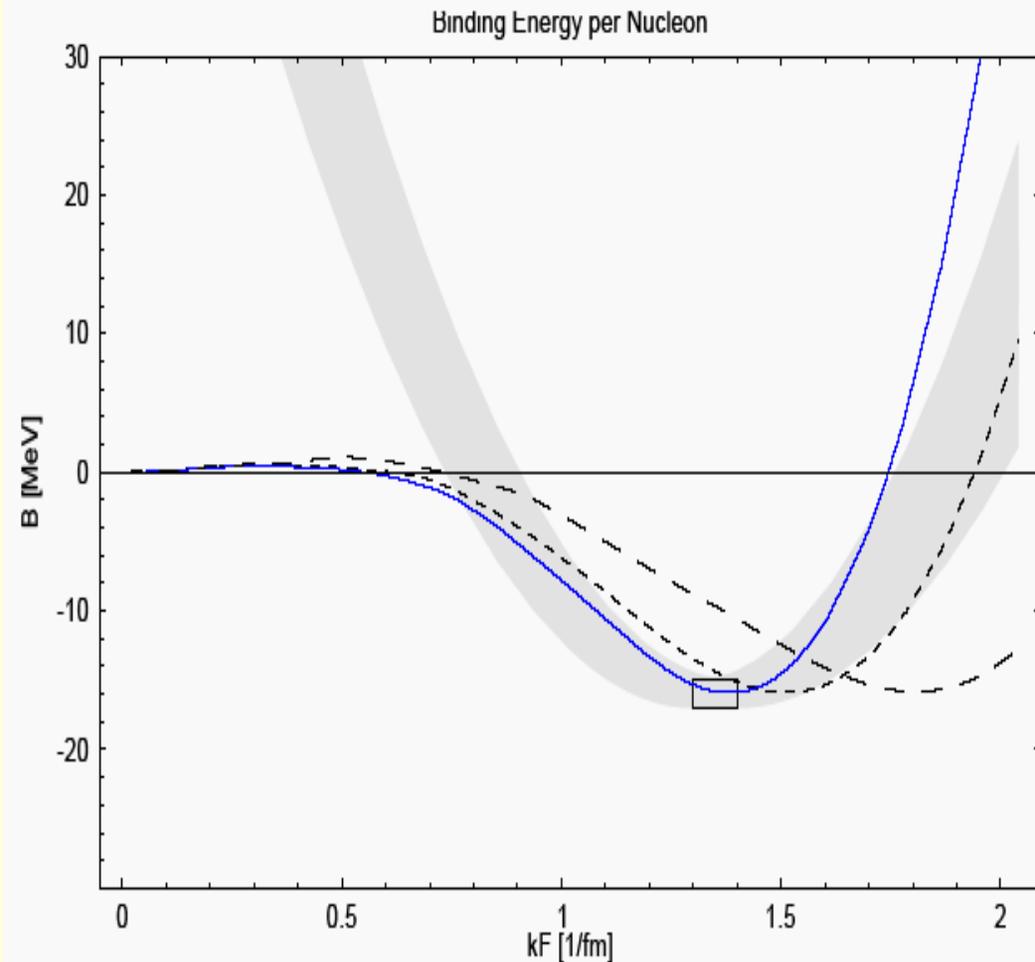
$$\alpha_s = \frac{E_s - p_z^s}{M}$$

BoNuS expt Jlab- n/p sf

Melnitchouk Sargsian Strikman '97



Results – Nuclear Matter

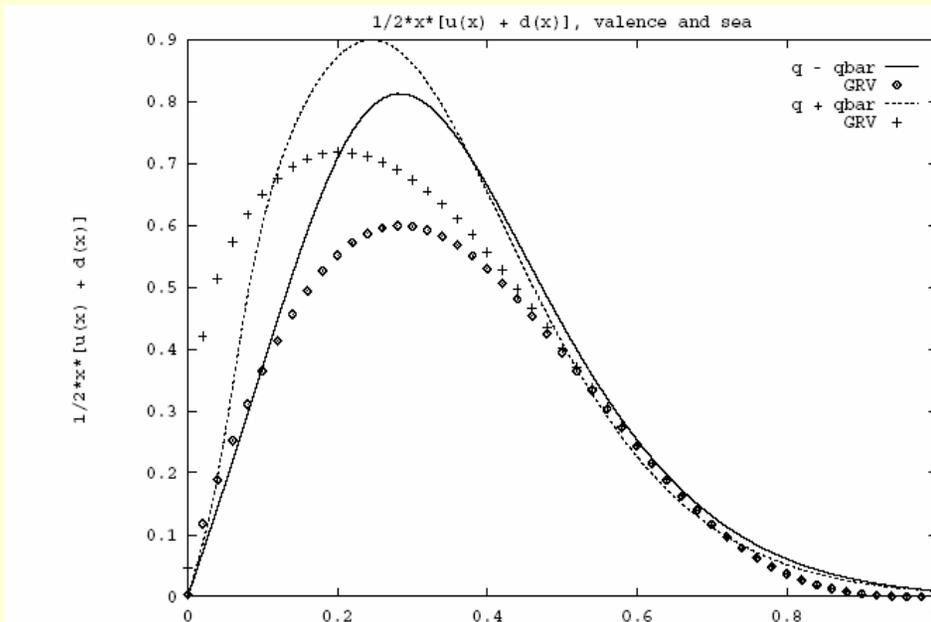


Smith-Miller

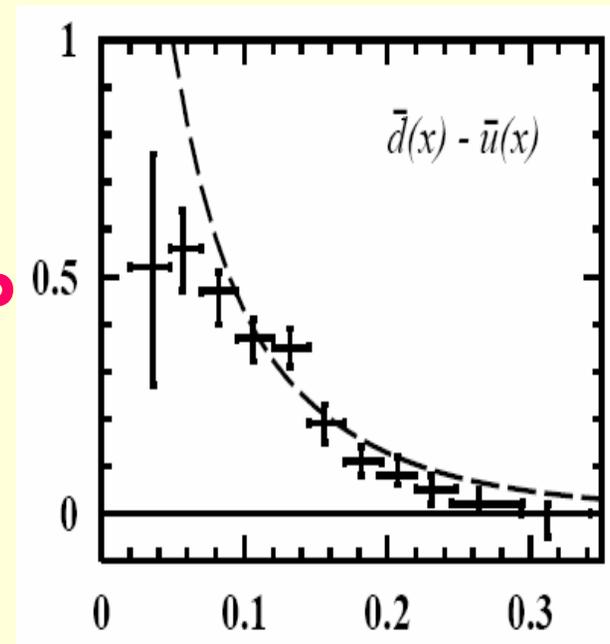
$-\langle\bar{\psi}\psi\rangle_0^{1/3}$ [MeV]	$g_v^2/4\pi$	k_F [fm ⁻¹]	K [MeV]
225	7.22	1.81	291.7
210	8.96	1.51	312.5
200	10.55	1.38	348.5
-	10.47	1.42	560

Quark Soliton Model

- Twist-2 pdfs (low scale $\Lambda=600$ MeV UV cutoff) - gluon's carry 30 % momentum, sea
- QCD evolve to higher Q^2
- Sum rules, support and positivity
- Pdfs: rest and infinite momentum frames

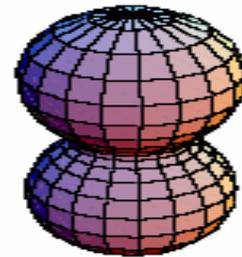
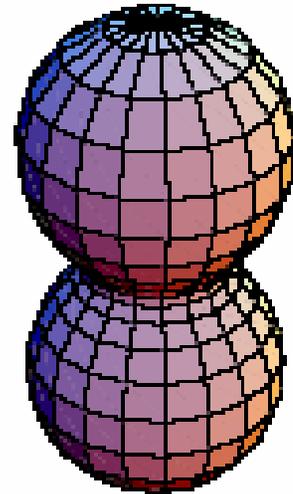


DPP



Closer look needed! Lower components LoC

- LoC account for QF_2/F_1
- LoC gives non-spherical shape of proton
- Medium modifies LoC
- Medium modifies shape



**Challenge to experiment-
measure either**

Suppression of Point Like Configurations- Frankfurt, Strikman



place in medium:

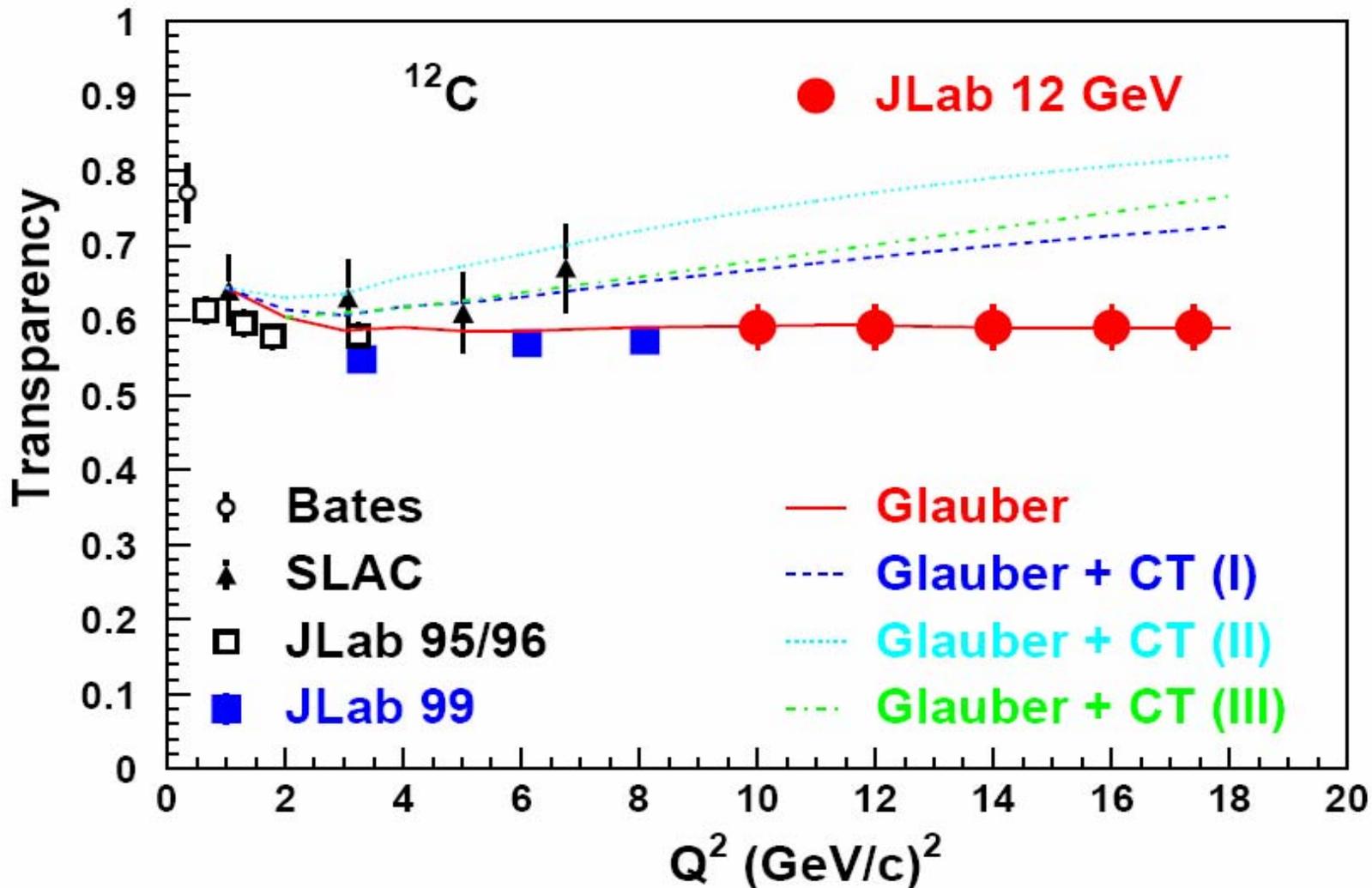
normal size components attracted energy goes down

PLC does not interact- color screening

energy denominator increased, PLC suppressed

quarks lose momentum in medium

Color transparency in (e,e'p) enhancement



Color transparency in double scattering- suppression

