

The Pion Form Factor

Tanja Horn

University of Maryland
for the F_{π} -2 Collaboration

- Pion Form Factor in pQCD
- The transition to the asymptotic regime
 - > Pion Electroproduction
 - > Cross Section Extraction
- Results and new directions

Hall C Summer Workshop, 19 Aug 2005



$F_{\pi}-2$ Collaboration

R. Ent, D. Gaskell, M.K. Jones, D. Mack, J. Roche, G. Smith, W. Vulcan, G. Warren

Jefferson Lab, Newport News, VA, USA

G.M. Huber, V. Kovaltchouk, G.J. Lolos, C. Xu

University of Regina, Regina, SK, Canada

H. Blok, V. Tvaskis

Vrije Universiteit, Amsterdam, Netherlands

E. Beise, H. Breuer, C.C. Chang, T. Horn, P. King, J. Liu, P.G. Roos

University of Maryland, College Park, MD, USA

W. Boeglin, P. Markowitz, J. Reinhold

Florida International University, FL, USA

J. Arrington, R. Holt, D. Potterveld, P. Reimer, X. Zheng

Argonne National Laboratory, Argonne, IL, USA

H. Mkrtchyan, V. Tadevosn

Yerevan Physics Institute, Yerevan, Armenia

S. Jin, W. Kim

Kyungook National University, Taegu, Korea

M.E. Christy, L.G. Tang

Hampton University, Hampton, VA, USA

J. Volmer

DESY, Hamburg, Germany

T. Miyoshi, Y. Okayasu, A. Matsumura

Tohoku University, Sendai, Japan

**B. Barrett, A. Sarty, K. Aniol, D. Margaziotis, L. Pentchev, C. Perdrisat, I. Niculescu, V. Punjabi,
E. Gibson**

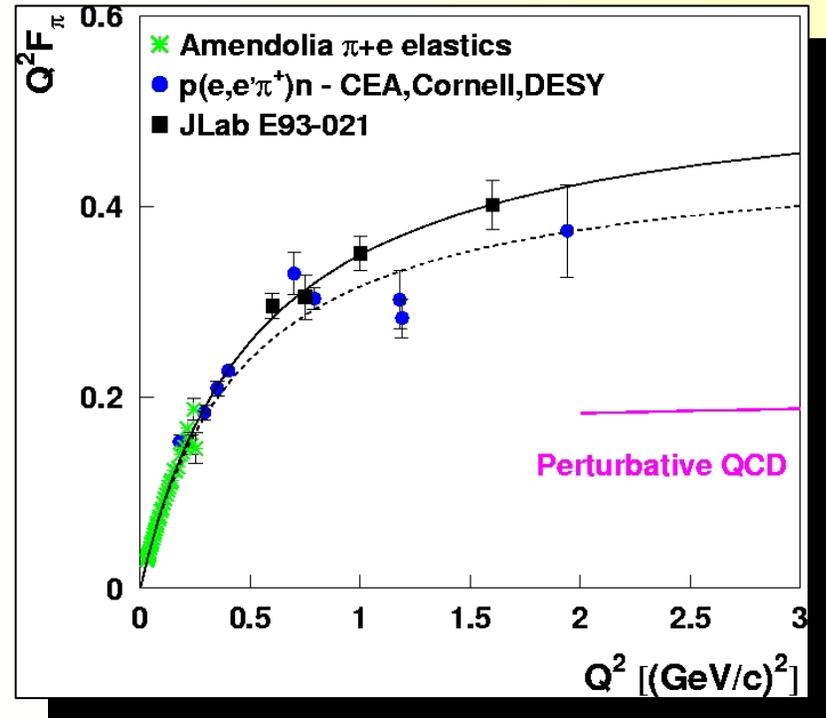
Hadronic Form Factors in QCD

- Fundamental issue: Quantitative description of hadrons in terms of underlying constituents.
 - Theory: QCD describes strong interactions
 - Degrees of freedom: quarks and gluons
- However, consistent analysis of different length scales in a single process not easy.
- Studies of short/long distance scales
 - Theory - QCD framework, GPD's and effective models
 - Lattice calculations - still in progress
 - Experiments - form factors, neutral weak nucleon structure, charge structure of 2-quark systems

Pion Form Factor in QCD

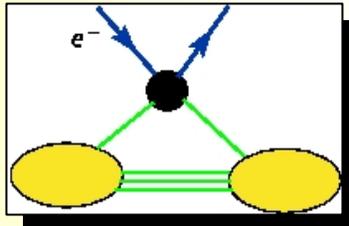
- Why pions? - Simplest QCD system ($q\bar{q}$) - "Hydrogen Atom of QCD"
- Good observable for study of interplay between hard and soft physics in QCD
- Large Q^2 behavior predicted by Brodsky-Farrar

$$F_{\pi} \rightarrow \frac{8\pi f_{\pi}^2}{Q^2}$$



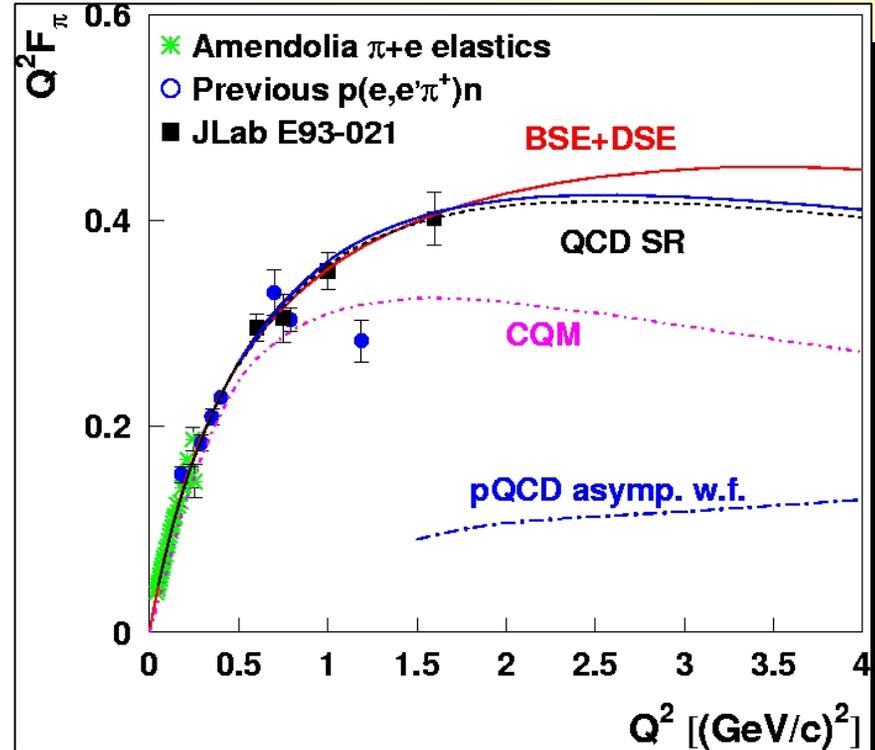
- At small Q^2 vector meson dominance gives accurate description with normalization $F_{\pi}(0)=1$ by charge conservation - data fits well so where is pQCD?

Nonperturbative Physics



Feynman Mechanism

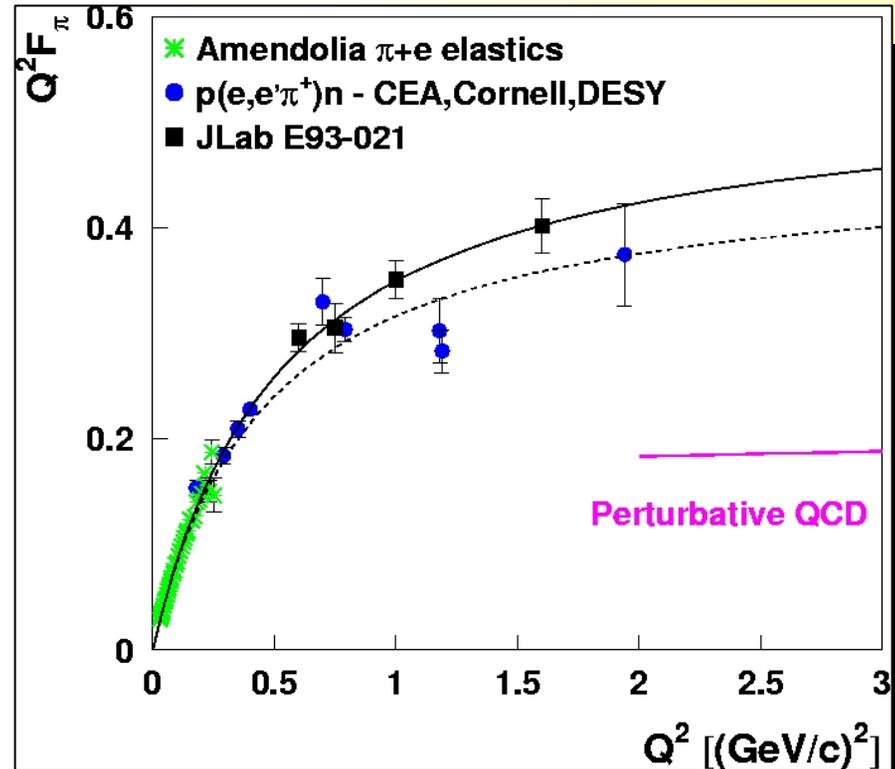
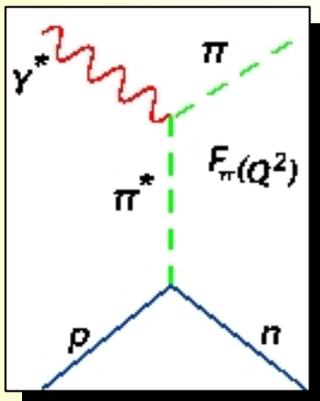
- At moderate Q^2 nonperturbative corrections to pQCD can be large
 - Braun et al calculate $\sim 30\%$ at $Q^2=1 \text{ GeV}^2$ to F_π
- Need a description for **transition to asymptotic behavior**
- Variety of effective models on the market - how do we know which one is "right"? - **experimental studies to constrain models**



Effective models and pQCD prediction of F_π

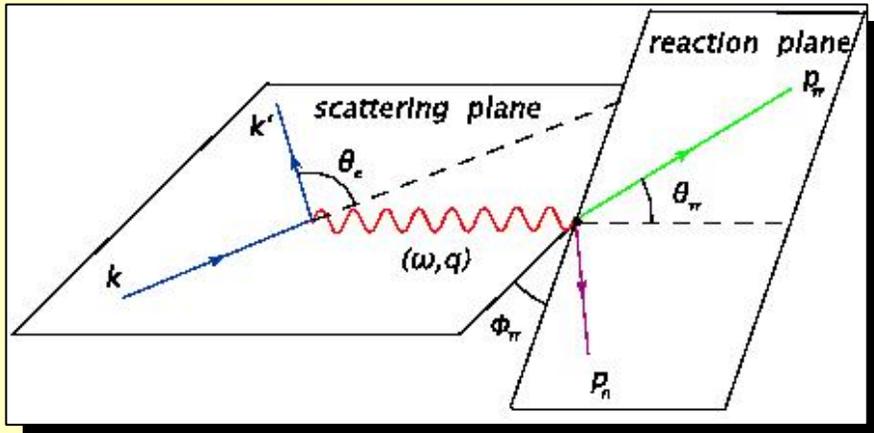
Pion Form Factor via Electroproduction

- Charge radius well known from π^+e scattering
- No "free pion" target - to extend measurement of F_π to larger Q^2 values use "virtual pion cloud" of the proton
- Method check - Extracted results are in good agreement with π^+e data



J. Volmer et al. Phys Rev. Lett. 86 (2001) 1713-1716

Extraction of the Pion Form Factor



- Extraction of F_π requires a model incorporating pion electroproduction

- In t-pole approximation:

$$\sigma_L \propto \frac{-t g^2_{\pi NN} F^2_\pi(Q^2)}{(t - m^2_\pi)^2}$$

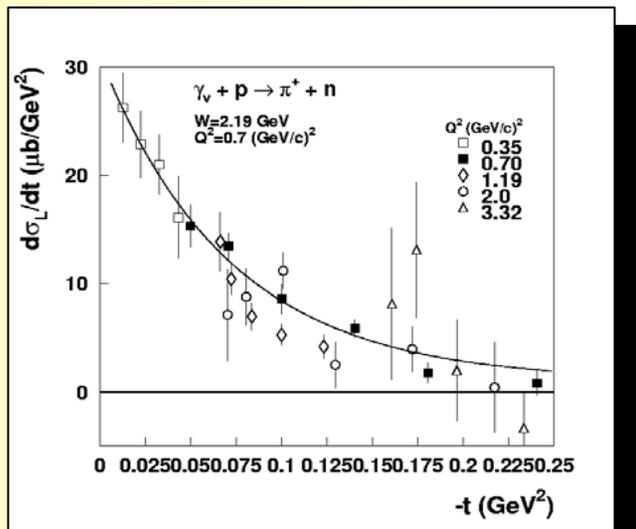
- Want smallest possible $-t$ for proximity to π -pole
- Need to know t -dependence
- Pole dominance tested using π^+/π^- from $D(e, e'\pi)$ - if pure pole then $\frac{\sigma_L^{\pi^+}}{\sigma_L^{\pi^-}} = 1$

$$\frac{d^2\sigma}{dt d\varphi} = \epsilon \frac{d\sigma_L}{dt d\varphi} + \frac{d\sigma_T}{dt d\varphi} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt d\varphi} \cos\varphi_\pi + \epsilon \frac{d\sigma_{TT}}{dt d\varphi} \cos 2\varphi_\pi$$

Extracting F_π from σ_L data

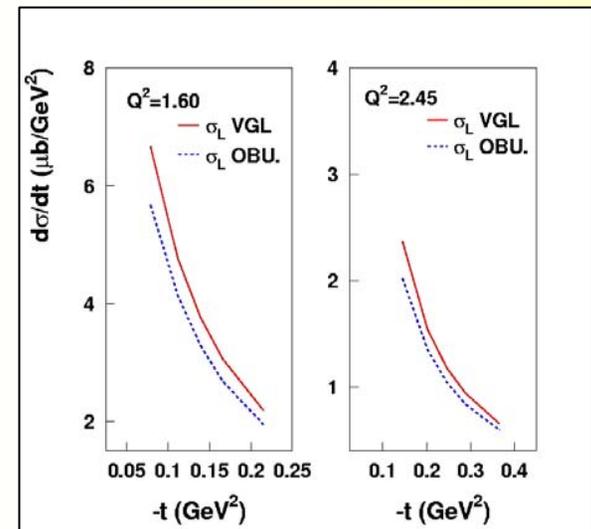
- DESY (Brauel et al) used Born term model for t-dependence of the data
- $F_{\pi-1}/F_{\pi-2}$ at JLab use VGL/Regge model - F_π is the only free parameter adjusted at each Q^2 to reproduce σ_L data
- New cross section calculation by I. Obukhovsky et al - includes baryon s-poles by nonlocal extension of contact term, include quark form factor with $\Lambda_q=0.95$

P. Brauel, ZP C3, 101 (1978)



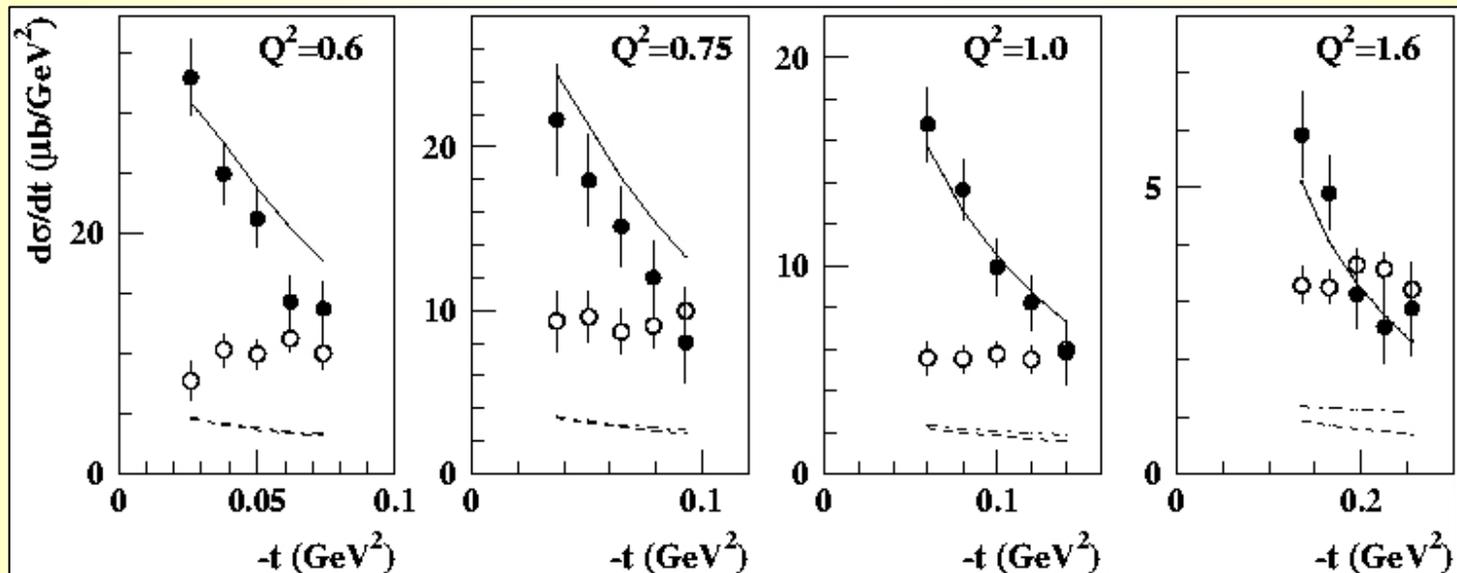
I. Obukhovsky et al hep-ph/0506319

M. Vanderhaeghen, M Guidal, J-M Laget Phys Rev C57 (1998)



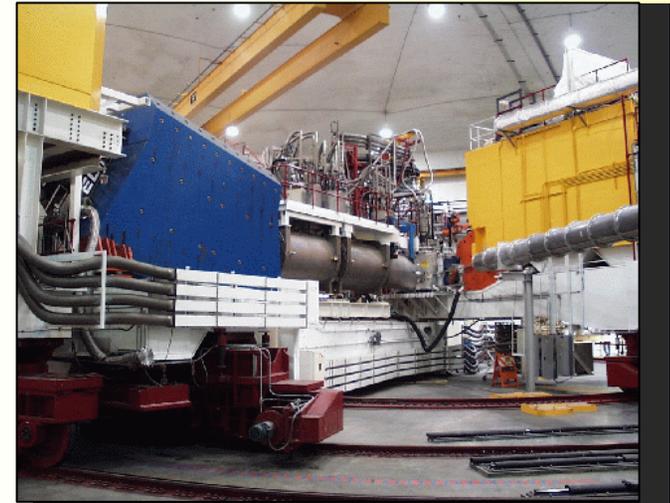
F_{π^-1} (E93-021)

- Data taken in 1998, thesis students: [J. Volmer](#) and [K. Vansyoc](#)
- $Q^2=0.6-1.6 \text{ GeV}^2$ at $W=1.95 \text{ GeV}$
- Transverse cross section smaller and slightly steeper t -dependence in σ_L than in Regge model - attributed to resonance background contribution



$F_{\pi}-2$ (E01-004)

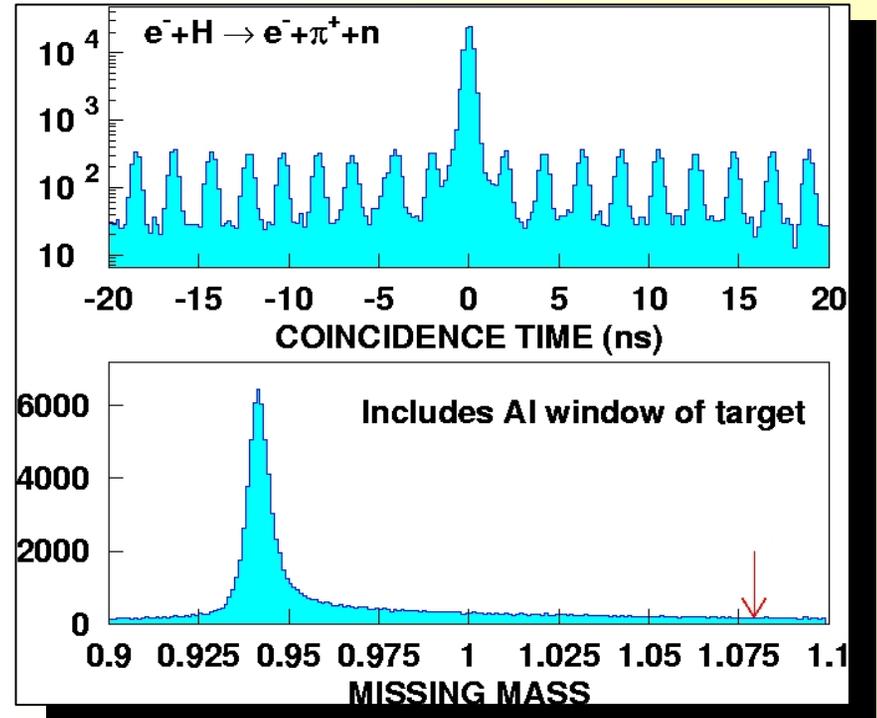
- Successfully completed in Hall C in 2003
- Extension of E93-021 ($F_{\pi}-1$)
 - Completed in 1997 - J. Volmer et al PRL 86 (2001)
- New data at higher W
- Constraint on soft models for F_{π} at higher Q^2
- Repeat $Q^2=1.60 \text{ GeV}^2$ closer to $t=m_{\pi}$ pole allows study of model dependence in extraction of F_{π}



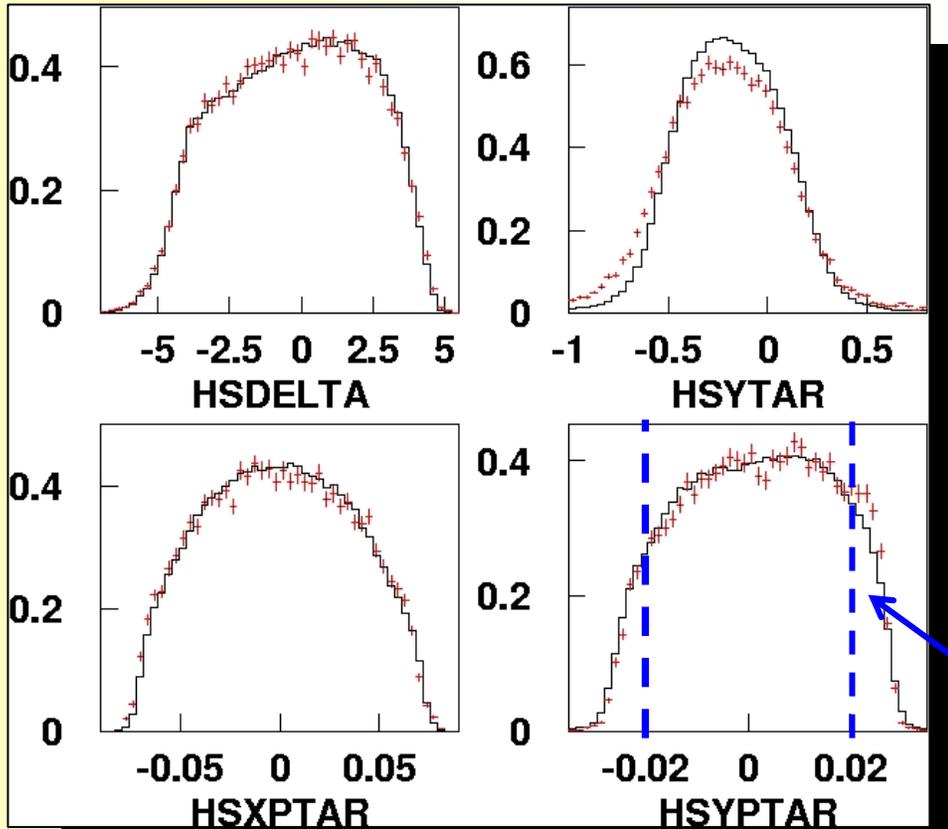
Exp	Q^2 (GeV/c) ²	W (GeV)	$ t $ (GeV/c) ²	E_e (GeV)
$F_{\pi}-1$	0.6-1.6	1.95	0.03-0.150	2.445-4.045
$F_{\pi}-2$	1.6,2.5	2.22	0.093,0.189	3.779-5.246

Good Event Selection

- Coincidence measurement between charged pions in HMS and electrons in SIS
- π^+ detected in HMS - Aerogel Cerenkov and Coincidence time for PID
 - π^- selected in HMS using Gas Cerenkov
- Electrons in SOS - identified by Cerenkov / Calorimeter
- After PID cuts almost no random coincidences



Acceptance Studies

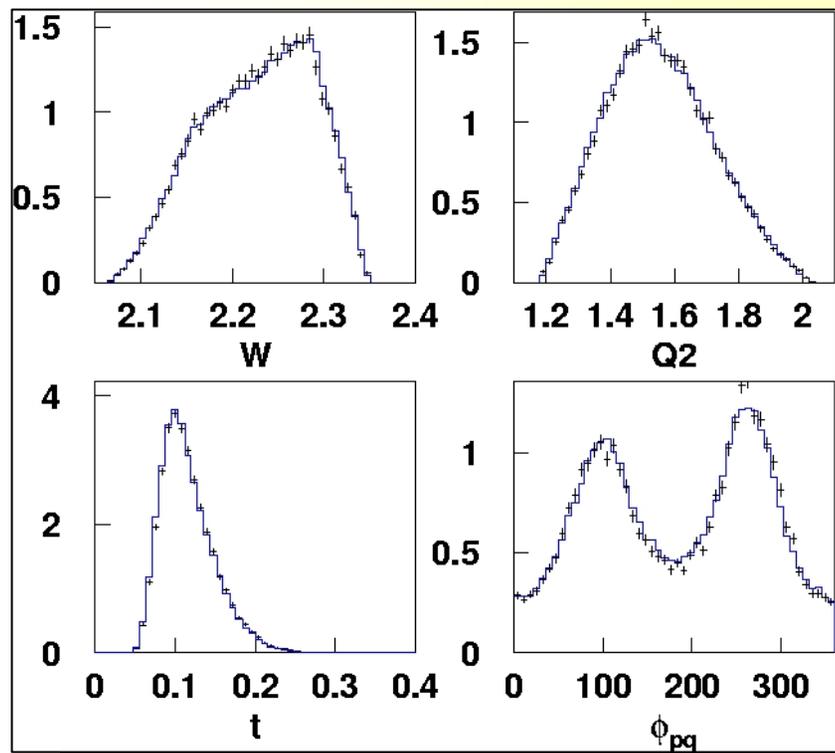


- t -bin closest to $t=m_\pi$ very sensitive to offsets
- Found that cross section significantly sensitive to Y'_{tar} acceptance
- Acceptance edges currently under study - in cross section extraction limit to well understood region

Acceptance
Cut

Cross Section Extraction

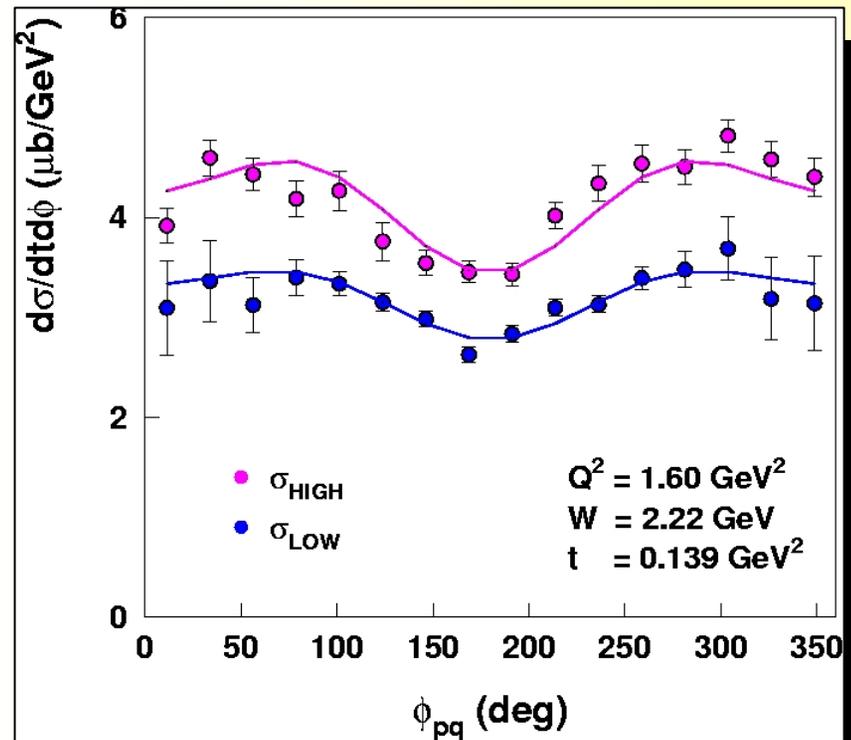
- Cross Section Extraction requires Monte Carlo Model of spectrometer optics and acceptance
- Compare Data to Hall C Monte Carlo - **SIMC**
 - **COSY** model for spectrometer optics
 - **Model for $H(e, e' \pi^+)$**
 - **Radiative Corrections, pion decay**
- Experimental cross section extracted by iterating model until achieve agreement with data



$$\sigma_{\text{exp}} = \frac{Y_{\text{exp}}}{Y_{\text{SIMC}}} \sigma_{\text{model}}$$

Cross Sections Unseparated

- Cross Section Extraction
 - Data binned in t and φ
 - Average W , Q^2 for each bin at both high and low epsilon
- Extract σ_L by simultaneous fit using measured azimuthal angle (φ_π) and knowledge of photon polarization (ϵ)

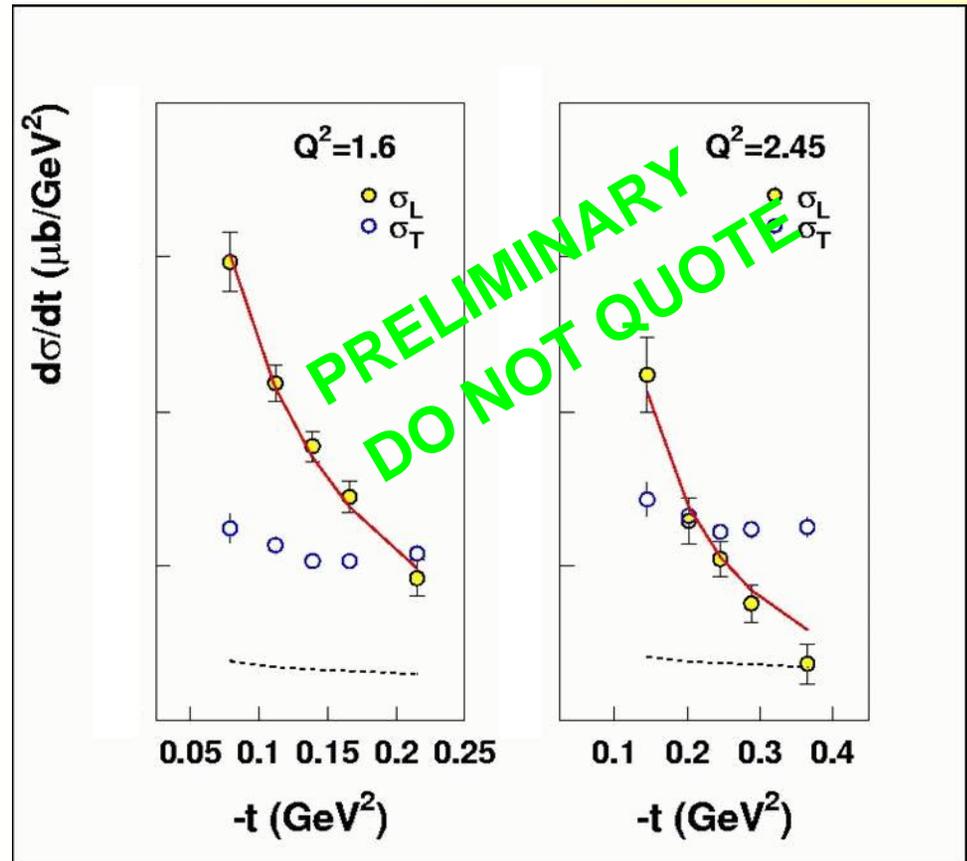


$$\frac{d^2\sigma}{dt d\varphi} = \epsilon \frac{d\sigma_L}{dt d\varphi} + \frac{d\sigma_T}{dt d\varphi} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt d\varphi} \cos\varphi_\pi + \epsilon \frac{d\sigma_{TT}}{dt d\varphi} \cos 2\varphi_\pi$$

Preliminary Results

- $F_{\pi-2}$ Separated cross sections
 - Y'_{tar} acceptance cut applied
 - Compare to VGL/Regge model with $\Lambda_{\pi}^2 = X.XXX$ $\Lambda_{\rho}^2 = 1.7$

Point-to-point Systematic	Error
Acceptance	3-4.5%
Radiative Corrections	1%
Kinematics	1%
Target Density	0.5%
Charge	0.5%
Model Dependence	0.5%
Cut Dependence	0.5%
Detection Efficiency	0.5%



- Statistical Error only

Preliminary F_π Results

- Increase in dynamic coverage in Q^2
- Datapoint at $Q^2=1.60 \text{ GeV}/c$ to check model dependence of mass pole extrapolation
- To Do:
 - (more) Acceptance Studies
 - Radiative Correction Tests
 - Model Dependence - model iteration
 - Kinematic uncertainties
 - Theory uncertainties
 - Pole dominance: π^+/π^- ratios

**PRELIMINARY
DO NOT QUOTE**

F_π at 12 GeV

- Significant progress on theoretical front expected in next 5 years - Lattice, GPD etc
- Experiments need higher energy electron beam to reach the kinematic region where pQCD expectation may be approached
- SHMS+HMS in Hall C will allow F_π to be measured up to $Q^2=6 \text{ GeV}^2$ - 12 GeV proposal
- Small Forward angle crucial for F_π experiment since need to reach low $-t$ values.

PRELIMINARY
DO NOT QUOTE

Summary

- F_π good observable to study transition region to pQCD
- Results from $F_{\pi-1}$ shows $Q^2 F_\pi$ clearly not asymptotic yet
 - π^-/π^+ suggests dominance of pion exchange
- $F_{\pi-2}$ results in a region of Q^2 where F_π calculations begin to diverge
 - Data will constrain models describing the treatment of soft physics at higher Q^2
- Studies of F_π at 12 GeV will allow us to reach the kinematic range where pQCD expectation may be approached